A Novel Approach for Reactive Power Output Optimization in Wind Farm for the Reduction of Distribution Losses using Genetic Algorithm

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Abstract: In recent years there is increase in the generation of electricity by wind power. The numbers of small size wind farms used as DG sources located within the distribution system are rapidly increasing. In this paper, a novel approach for reactive power output optimization in wind farm for the reduction of distribution losses using genetic algorithm is incorporated. Wind farm made up with doubly fed induction generators (DFIG) is proposed as the continuous reactive power source to support system voltage control due to the reactive power control capability of the DFIG. The genetic algorithm method is utilized for comparison between the distribution losses of the system before the optimization technique and after implementing the optimization technique. Finally the three feeder distribution system is used as test case to evaluate the algorithm.

Keyword: Doubly fed Induction Generator, Grid connected wind farm, Genetic Algorithm, Asynchronous Generator

1. INTRODUCTION

Currently, there is an increasing concern over the environmental impact and sustainability of traditional fossil-fuelled power plants. Because wind energy is one of the most important and promising renewable energy resources in the world, leading to a growing penetration of the wind energy in electrical systems, in [1] proposed a wind farm made up with DFIG as a continuous reactive power source to support system voltage control due to the reactive power control capability of DFIG. The particle swarm optimization algorithm (PSO) is utilized to find the optimal reactive power output of wind farm. The main objective of the optimization is to minimize the total real power losses of the system and the deviation of the bus voltage in the proposed optimization algorithm, reactive power output of wind farm is utilized as the control variable for loss minimization and voltage profile improvement, in [2] studies the reactive power output optimization of wind farm, and the variability and intermittency of wind speed is considered. The multi-objective reactive power optimization model including network loss, average deviation of voltage system, is popular and widely used for wind power generation due to its several advantages.

The effectiveness of the proposed method is demonstrated on IEEE-57 bus system with wind, [3] the use of genetic algorithms for the resolution of the optimization problem of the voltages fall and the active losses in a power system including a wind power station by acting on the reactive productions of inductances and capacitors branches connected to the consuming nodes in [4] an improved Genetic algorithm (GA) for reactive power optimization in wind farm. Traditional GA has some drawbacks, such as slow convergence. The coding method, genetic operators, crossover and mutation probability, stopping criterion in iteration has been improved. The reactive power optimization method with improved GA is tested in a MATLAB based simulation model, in [5] developed a wind farm model and concluded that wind farms made up of double fed induction generators constitute an important tool from the voltage regulation point of view. Furthermore, the designed proportional distribution algorithm makes all the generators work under similar conditions and quite far from saturation, which means far from the reactive power generation limits in [6] the power capability limits of doubly fed asynchronous generators. These limits have been obtained by taking into account the maximum stator and rotor currents and the steady state stability limit of the generator, in [7] describe the development of a new algorithm for the solution of a multi-objective problem in power systems with wind farm using Particle Swarm Optimization. Basically, the purpose is to search an optimal operation point of system which allows simultaneous power factor remote control and loss minimization. In [8] described the reactive power capabilities of wind power generator and then discuss reactive power ancillary services issues related to the wind farms in the electricity market. Presently, the doubly fed induction generator (DFIG) system is popular and widely used for wind power generation due to its several advantages [9].
A detailed view of wind turbine power, energy and torque is given. Different types of generators used in wind farm are also discussed. In the end, an overview of wind power plants is also provided.

In present work, a test system is taken and a Wind farm with doubly fed induction generator is connected to one of its nodes. The active power output of the wind farm is used to find the maximum of reactive power capability limits. Then using Reactive power as a control variable, the optimum value of reactive power, for which the losses and voltage deviation are minimized, is determined by Genetic algorithm.

II. SYSTEM MODEL AND CONTROL

The model of DFIG consisting of a pitch controlled wind turbine and an induction generator [1]. The stator of the DFIG is directly connected to the grid, while the rotor is connected to a converter consisting of two back-to-back PWM inverters, which allows direct control of the rotor currents. Direct control of the rotor currents allows for variable speed operation and reactive power control thus DFIG can operate at a higher efficiency over a wide range of wind speeds and help provide voltage support for the grid. These characteristics make the DFIG ideal for use as a wind generator.

A. DFIG Capability Limits Curve

The stator active and reactive power can be expressed as a function of stator current and rotor current [1]

\[ P_s^2 + Q_s^2 = (3U_s I_s)^2 \]  
\[ P_s^2 + (Q_s + 3 \frac{U_s}{X_s})^2 = (3 \frac{X_m U_s I_R}{X_s})^2 \]

In the PQ plane, (1) represents a circumference centred at the origin with radius equal to the stator rated apparent power. Equation (2) represents a circumference centred at \([-3U_s^2/X_s, 0]\) and radius equal to \(3X_m U_s I_R / X_s\). Therefore, given the stator and rotor maximum allowable currents \(I_{s\text{max}}\) and \(I_{r\text{max}}\), the DFIG capability limits are obtained.

Fig.1 shows the composed curve for the DFIG capability limits. Additionally, the steady state stability limit of the DFIG is taken into account, which represented as vertical line at \([-3U_s^2/Xs, 0]\) , coordinate. It’s obvious that the DFIG reactive power capability mainly depend on the rotor maximum allowable current \(I_{r\text{max}}\). In Fig.1. The DFIG can be able to operate at any point in the intersecting area within the given limits. From this figure, one can observe that when the available active power is far from its maximum, the amount of available reactive power is high.

![Fig.1: DFIG capability limits curve](image_url)

The large reactive power control capability of the DFIG making it possible to use DFIG as the continuous reactive power source to support system voltage control.

B. Wind Farm Model

In this paper, a wind farm model is developed with a DFIG wind turbines connected in parallel. As a result, the total active and reactive power output of the wind farm equal to the sum of the active and reactive power generated by each of the DFIG wind turbine in the wind farm:
\[ P_{WF} = \sum_{i=1}^{N} P_{gi} \] (3)

\[ Q_{WF} = \sum_{i=1}^{N} Q_{gi} \] (4)

Where \( P_{WF} \) represents the active power output of the windfarm, \( Q_{WF} \) represents the reactive power output of the windfarm, \( P_{gi} \) represents the generated active power of each DFIG and \( Q_{gi} \) represents the generated or absorbed reactive power of each DFIG.

In this paper, it’s assumed that the wind speed at each DFIG is the same and all of the available active power inwind farm is fed into the distribution network.

### III. PROBLEM FORMULATION

In this section, wind farm reactive power output optimization has been modelled as a multi objective, non-differentiable optimization problem. In the proposed optimization algorithm, the objective function consists of two terms: 1) the real power losses of the system, 2) the deviation of the bus voltage.

\[
\text{min} f_1(\bar{X}) = \lambda_1 \sum_{i=1}^{N} R_i \frac{P_{gi}^2 + Q_{gi}^2}{|V_i|^2} + \lambda_2 \max |V_i - V_{rat}| \tag{5}
\]

Owing to the DFIG operational requirements, the minimization of the objective function is subjected to the following constraints:

1) Distribution power flow equations:

\[
P_i + P_{WF_i} = P_{Di} + V_i \sum_{j=1}^{N_{bij}} V_j (G_{ij} \sin \delta_{ij} + B_{ij} \sin \Theta_{ij}) \tag{6}
\]

\[
Q_i + Q_{WF_i} = Q_{Di} + V_i \sum_{j=1}^{N_{bij}} V_j (G_{ij} \sin \delta_{ij} - B_{ij} \sin \Theta_{ij}) \tag{7}
\]

2) DFIG active capability limits:

\[
P_{gi,\text{min}} \leq P_{gi} \leq P_{gi,\text{max}} \tag{8}
\]

3) DFIG reactive capability limits:

\[
Q_{gi} \leq \left[ \left( \frac{3 X_{S} U_{S} I_{R}}{X_{S}} \right)^2 - \left( P_{gi} \right)^2 \right] - \frac{3 U_{S}^2}{X_{S}} - Q_{gi} \leq \left[ \left( \frac{3 X_{S} U_{S} I_{R}}{X_{S}} \right)^2 - \left( P_{gi} \right)^2 \right] + \frac{3 U_{S}^2}{X_{S}} \tag{9}
\]

4) Node voltage magnitude limits:

\[
V_{\text{min}} \leq V_i \leq V_{\text{max}} \tag{10}
\]

5) Distribution line limits:

\[
|P_{ij,\text{line}}| < P_{ij,\text{line},\text{max}} \tag{11}
\]

6) Radial structure of the network.

### IV. GA BASED REACTIVE POWER OUTPUT OPTIMIZATION

The beginnings of genetic algorithms can be traced back to the early 1950s when several biologists used computers for simulations of biological systems. However, the work done in late 1960s and early 1970s at the University of Michigan under the guidance of John Holland led to genetic algorithms as they are known today. GA vocabulary is being borrowed from natural genetics. The idea behind genetic algorithms is to do what nature does. Genetic algorithms (GAs) are stochastic algorithms whose search methods inspired from phenomena found in living nature. The phenomena incorporated so far in GA models include phenomena of natural selection as there are selection and the production of variation by means of recombination and mutation, and rarely inversion, diploid and others. Most Genetic algorithms work with one large pneumatic population, i.e. in the recombination step each
individual may potentially choose any other individual from the population as a mate. Then GA operators are performed to obtain the new child offspring; the operators are:

1) Selection
2) Crossover
3) Mutation

An algorithm is developed to find the optimum value of reactive power output of wind farm and objective function. First the model of the test system is developed in MATLAB/ SIMULINK. Then the simulation results of the test system are used to find the objective function and optimum reactive power. The reactive power output of the wind farm is used as a control variable in Genetic algorithm and an initial population is generated randomly within control variable bounds. Then objective function for each individual is calculated using the result of load flow analysis. The results are then stored after meeting the termination criteria. The algorithm is amalgamation of Genetic algorithm. In Genetic algorithm population is initialized and when it satisfied the constraints by means of mutation and crossover, it assign a new generation which set the value for Reactive power for the given iteration and load flow is run by means of selection. By following this process of crossover, mutation and generation several times the objective function will reach at its minimum value. The Algorithm is explained in steps as:

Step1. Initialize the system Data and GA control parameters
Step2. Input wind speed and calculate reactive power limit by active power output.
Step3. Calculate initial power flow, generate initial population.
Step4. Initial population distributes uniformly
Step5. Selection, crossover, mutation
Step6. Calculate fitness function.
Step7. Meet the termination criterion. If not, go to step 5 otherwise go to step 8.
Step8. Record the results.

V. SIMULATION RESULTS

For modelling of a dynamic system, the system should be fully defined. After building each component, integrate them into a complete model of the system. A three feeder distribution system is used as shown in the Fig. 2 with a base voltage of 0.69 KV. Total system load is 28.7MW and 17.3MVAR. A small wind farm comprising 10 DFIG wind turbines of 900kW, with a power installed of 9MW is connected at node 12 through a rated 23/0.69 kV transformer.

The performance parameters of the studied DFIG wind turbine are given in Table 1

<table>
<thead>
<tr>
<th>Table 1</th>
<th>DFIG PERFORMANCE PARAMETERS</th>
<th>Table 2</th>
<th>DFIG ELECTRIC PARAMETERS</th>
</tr>
</thead>
<tbody>
<tr>
<td>Parameter</td>
<td>Value</td>
<td>Parameter</td>
<td>Value</td>
</tr>
<tr>
<td>Rated capacity</td>
<td>900KW</td>
<td>Stator resistance per phase</td>
<td>.0067Ω</td>
</tr>
<tr>
<td>Cut in wind speed</td>
<td>4m/s</td>
<td>Stator leakage reactance per phase</td>
<td>.0300 Ω</td>
</tr>
<tr>
<td>Cut out wind speed</td>
<td>25m/s</td>
<td>General turns ratio</td>
<td>.3806</td>
</tr>
<tr>
<td>Rated wind speed</td>
<td>12.5m/s</td>
<td>Mutual reactance</td>
<td>2.3161 Ω</td>
</tr>
<tr>
<td>Rated voltage</td>
<td>.69KV</td>
<td>Rotor resistance per phase</td>
<td>.0399 Ω</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Rotor leakage reactance per phase</td>
<td>.3490 Ω</td>
</tr>
</tbody>
</table>
The electric parameters of the studied DFIG wind turbine are given in Table 2.

![Fig. 2 Single line diagram of three feeder system](image)

**A. Available Active and Reactive Power in Wind Farm**

Fig.3 shows the wind speeds on the wind turbines considered in the simulation. Then the active power output of DFIG is obtained by means of the power curve. Considering the DFIG capability limits curve described in Fig.1, the maximum limits of available reactive power for each generated active power of DFIG wind turbine can be calculated.

![Fig.3. Curve of wind speed](image)  ![Fig.4. Active and reactive available power in wind farm](image)

Fig.4 shows the active and reactive available power in wind farm. From Fig.4, it can be observed that wind farm made up DFIG wind turbine can generate more reactive power when the available active power decreases. It's followed that the wind farm can contribute more significantly to the maintenance of the grid voltage at low speed.

**B. Results of Optimization**

The Reactive power output of the DFIG is used as control variable in Genetic algorithm. The objective function which includes minimization of losses and improvement of voltage profile is calculated by means of Genetic algorithm. The Table 3 shows the input values for the optimization toolbox in MATLAB while Table-4 shows the results after optimization through genetic algorithm. Whereas the plot of best fitness, best individual, max constraint and range are drawn by MATLAB Optimization Toolbox.
### TABLE 3

**INPUT VALUES FOR GA TOOL USED IN MATLAB**

<table>
<thead>
<tr>
<th>Number of variables</th>
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</tr>
</thead>
<tbody>
<tr>
<td>Lower Bounds</td>
<td>[0.58]</td>
</tr>
<tr>
<td>Upper Bounds</td>
<td>[9]</td>
</tr>
<tr>
<td>Mutation</td>
<td>uniform with rate 0.05</td>
</tr>
<tr>
<td>Current iteration</td>
<td>51</td>
</tr>
<tr>
<td>Generations</td>
<td>100</td>
</tr>
<tr>
<td>Crossover</td>
<td>0.5</td>
</tr>
<tr>
<td>Selection function</td>
<td>stochastic function</td>
</tr>
<tr>
<td>Elite count</td>
<td>2</td>
</tr>
<tr>
<td>Initial range</td>
<td>[0;1]</td>
</tr>
</tbody>
</table>

### TABLE 4

**RESULTS FROM GA**

<table>
<thead>
<tr>
<th>DFIG at node</th>
<th>Losses (MW)</th>
<th>Optimum reactive power (MVAR)</th>
<th>Objective function</th>
</tr>
</thead>
<tbody>
<tr>
<td>12</td>
<td>0.43368</td>
<td>1.93409</td>
<td>0.02412</td>
</tr>
</tbody>
</table>

Comparison between the power losses of the system when the power factor of the wind farm is kept constant at 0.98 and power losses of the system after optimization are shown in Fig. 5.

![Fig. 5: Power losses of the distribution system](image1)

Comparison between the minimum nodal voltage of the system when the power factor of the wind farm is kept constant at 0.98 and nodal voltage of the system after optimization is shown in Fig. 6.

![Fig. 6: Minimum nodal voltage of the distribution system](image2)

### VI. CONCLUSIONS

In this paper, a novel approach for reactive power output optimization control of wind farm is proposed. In this new approach, reactive power output of wind farm is utilized as the control variable for losses minimization and voltage profile improvement. The optimal reactive power output of wind farm is efficiently obtained by taken in account DFIG reactive capability limits in the simulations. At last from the results obtained using genetic algorithm, it can be concluded that wind farm can constitute an important continuous reactive power source to support system voltage control.
VII. ACKNOWLEDGEMENT

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REFERENCES


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