

# Application of Microbial Kinetics in Upflow Anaerobic Sludge Blanket Reactor

Vidya Singh

Research Scholar, Department of Chemistry, Motilal Nehru National Institute of Technology, Allahabad, U.P, India

**ABSTRACT :** A mathematical approach was used to simulate the granule size variation in upflow anaerobic sludge blanket (UASB) reactor under different operating condition like organic loading rate (O), polymer loading ( $P_L$ ), upflow velocity ( $V_{up}$ ), operation time ( $t_0$ ), density of water ( $\rho_w$ ) and density of granule ( $\rho_g$ ). The experimental results of different investigators on polymer loading, OLR, upflow velocity, operation time and granule density were collected and developed a mathematical model to the enhancement of granule size in UASB reactor. Using MATLAB software indices of power multiplier function obtained can be used to predict the granule size ( $D_g$ ) variations in UASB reactor. A microbial Monod kinetics was applied to determine the substrate removal kinetics of UASB reactor.

**KEYWORDS:** Monod model, non linear regression, organic loading rate, UASB

## I. INTRODUCTION

Microbial granulation is a complex process, involving different trophic bacterial groups and their physico-chemical and microbiological interactions. Granulation initiated by bacterial adsorption and adhesion to inert matters or inorganic particulates provides a better settling characteristics and granule stability [1, 2].

UASB process performance can be judged by evaluating its performance within as well as beyond the granulation period and or start-up phase, as the system behaviour is under highly transient conditions within the granulation period [2-5].

Successful performance of UASB reactor can be achieved within a short period, if granules are developed quickly within the sludge bed under the proper environmental and operating conditions within the reactor [6]. Granulation process is affected by various factors like organic loading rate, upflow velocity, settling velocity, sludge volume index (SVI), gas production rate, liquid flow rate, polymer loading, Percent COD removal and effluent COD concentration.

Granules may range from 0.1 to 5 mm in size or even higher than 5 mm and are differentiated from flocculated sludge by their high shear strength [3, 7]. Approximately 2-3 % of the granules in the reactors were reported in the size range of 0.5-4.5 mm by [8]. [9] have documented that about 14 % granules were observed larger than 4.0 mm in size in UASB reactor. After increment in the organic loading rate, the granule sizes were reduced due to shearing of granules caused by high flow velocity and possible washout of lighter microorganisms [2, 3, 10].

In the present work, the independent variables like polymer loading, organic loading rate, upflow velocity, operation time and granule density influencing the granule size in UASB reactor have been collected from the literatures. Further a mathematical model was developed by non linear regression using MATLAB2010a software for prediction of granule size in UASB reactor. Various statistical measures were done between predicted output and experimental data of granule size to check the accuracy of developed model. It is believed that the developed model and tested in the present study may prove useful in assessing the granule size in UASB reactor. An application of Monod kinetics was also expressed with its derivation.

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## II. DATA COLLECTION AND METHODOLOGY

In the analysis of granule size development in UASB reactor, the experimental results of [4] have been used. These experimental data were read either from the figures or taken directly from the tables provided in [4]. In [4] influent substrate concentration ( $S_0$ ) was maintained at 4 g COD/L in all the four reactors R1 to R4 and OLR was varied in the range of 730-16030 g COD/m<sup>3</sup>.d. Reactor R4 exhibited the best settleability, short start-up period and good methanogenic activity at all organic loading rates, so analysis of these reactors considered in this study.

## III. RESULTS AND DISCUSSION

### 3.1 Dimensionless approach

In the present work, a dimensionless approach using Buckingham  $\pi$  - theorem has been applied to developed model for granule size ( $D_g$ ) in UASB reactor. As evident from the literature, granulation process is dependent on several factors enumerated in the proceeding section and hence the granule size is considered to be dependent on several independent variables such as operation time ( $t_o$ ), COD loading rate (O), upflow velocity ( $V_{up}$ ), polymer loading ( $P_L$ ), acceleration (g), specific density of granule ( $\rho_g$ ) and specific density of water ( $\rho_w$ ). By using Buckingham  $\pi$  - method, found some relationship between dependent and independent variables, then make 4 dimensionless groups which are given below. Another attempt was made to develop a power multiplier function for prediction of granule size by raising the powers of each dimensionless groups and is expressed as:

$$D_g = [t_o \cdot V_{up}] \left[ \frac{P_L}{O t_o^3 \cdot V_{up}^3} \right]^a \left[ \frac{t_o \cdot g}{V_{up}} \right]^b \left[ \frac{\rho_g}{\rho_w} \right]^c \quad (1)$$

Where,  $D_g$  is a function containing each dimensionless term as power function used, and a, b and c are indices raised to the dimensionless groups formed in Eq. (1) used for prediction of granule size.

### 3.2 Prediction of granule size ( $D_g$ )

In this modelling work; the indices a, b and c were determined by non-linear regression analysis by fitting the Eq. (1) using NLINFIT tool in MATLAB 2010a. Equation (1) has been tested on experimental data of [4] results are discussed in the succeeding sections.

a multiplier power function ( $D_g$ ) containing powers of each dimensionless terms of Eq. (1) is developed by simulating the granule size term (R.H.S term of Eq. (1)) with the experimental results of [4] using NLINFIT tool of MATLAB 2010a and the resulting non-linear best fit equations for R4 reactors are given below as equation (2) .

$$D_g = [t_o \cdot V_{up}] \left[ \frac{P_L}{O t_o^3 \cdot V_{up}^3} \right]^{0.073} \left[ \frac{t_o \cdot g}{V_{up}} \right]^{-0.292} \left[ \frac{\rho_g}{\rho_w} \right]^{0.110} \quad (2)$$

From equation (6) predicted data of granule sizes are observed, compare these output predicted values of granule size with experimental data of granule sizes and obtained percentage error are 15 %. Fig. 1 illustrates the agreement between the proposed non linear regression model outputs and the experimental data.

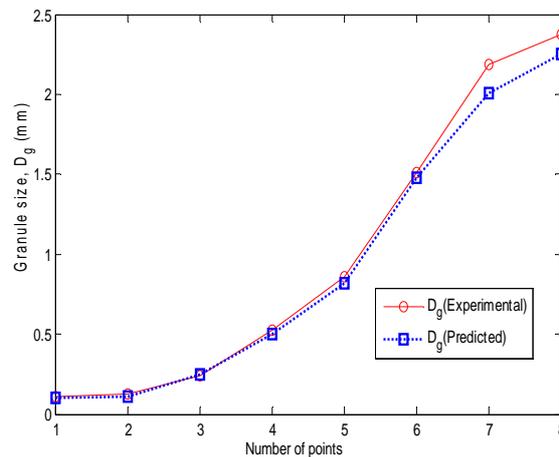


Fig.1. Agreement between the proposed model outputs and experimental data

From fig. 1 It can be seen that predicted output data of granule sizes were very close to experimental data of granule size, means a better fitting was predicted between observed output data and experimental values of granule sizes. Proposed model gives better results for prediction of granule sizes in UASB reactor.

**Table1. Descriptive statistics of the residuals errors in prediction of D<sub>g</sub> values**

Residual statistics	Calculation	Regression results
<b>SR</b>	$SR = \sum_{i=1}^n (D_e - D_p)$	<b>3.18E-04</b>
<b>AR</b>	$AR = \frac{1}{n} \sum_{i=1}^n (D_e - D_p)$	<b>3.97E-05</b>
<b>RSS</b>	$RSS = \sum_{i=1}^n (D_e - D_p)^2$	<b>1.43E-07</b>
<b>SEE</b>	$SEE = \sqrt{\frac{\sum_{i=1}^n (D_e - D_p)^2}{n - p}}$	<b>3.78E-04</b>
<b>R<sup>2</sup></b>	$R^2 = \frac{\sum_{i=1}^n (D_p - D_m)^2}{\sum_{i=1}^n (D_e - D_m)^2}$	<b>0.976</b>

D<sub>e</sub>, experimental granule size; D<sub>p</sub>, predicted Granule size; D<sub>m</sub>, mean granule size, n, no. Of experimental data point; SR, sum of Residuals of the errors; AR, average residuals of the errors; RSS residuals sum of squares; SEE, standard error of estimate.

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From Table 1 all statistical error estimates are low for analysis means observed predicted outputs are very close to experimental values. Predicted output granule sizes shows better fitting with experimental data of granule sizes, means proposed model for power multiplier function ( $D_g$ ) gives better results for prediction of granules sizes in UASB reactor.

### 3.3 Application of microbial monod kinetics

For a UASB reactor without biomass recycle, the rate of change of biomass and substrate in the system can be expressed as Eqs. (3,4)

$$\frac{dX_e}{dT} = \frac{Q \cdot X_i}{V} - \frac{Q \cdot X_e}{V} + \left( \frac{\mu_{\max} \cdot S_e}{K_s + S_e} \right) \cdot X_e - K_d \cdot X_e \quad (3)$$

$$-\frac{dS_e}{dT} = \frac{Q \cdot S_i}{V} - \frac{Q \cdot S_e}{V} - \frac{X_e}{Y} \left( \frac{\mu_{\max} \cdot S_e}{K_s + S_e} \right) \quad (4)$$

The ratio of the total biomass in the reactor to biomass wasted per given time represents the average time called as mean cell resistance time. The relationship between the specific growth rate and the rate limiting substrate concentration can be expressed as:

$$\mu = \frac{\mu_{\max} \cdot S}{K_s + S} \quad (5)$$

The kinetic parameters  $Y$  and  $K_d$  for monod model can be obtained by as shown below:

$$\frac{(S_i - S_e)}{\theta \cdot X} = \frac{1}{Y} \left( \frac{1}{\theta_c} \right) + \frac{1}{Y} K_d \quad (6)$$

$$\frac{\theta \cdot X}{(S_i - S_e)} = \frac{K_s}{K} \frac{1}{S_e} + \frac{1}{K} \quad (7)$$

By equation 5 shows substrate removal rate based on substrate mass balance in a biological reactor, linear equation 6 is obtained, by which synthetic coefficient  $K$ ,  $K_s$  are achieved. Where,  $Q$  is inflow discharge to reactor(L/d),  $V$  is reactor volume (L),  $S_i$  effluent substrate concentration (g COD/L),  $S_e$  effluent substrate concentration (g COD/L),  $X$  is influent biomass concentration (g VSS/L),  $X_i$  is influent biomass concentration (G VSS/L),  $X_e$  is effluent biomass concentration (g VSS/L),  $Y$  is yielding coefficient (g VSS/g COD),  $K_d$  is endogenous decay coefficient (d-1),  $\mu$  is specific growth rate,  $\mu_{\max}$  is maximum specific growth rate (d-1),  $K_s$  is half velocity constant (g COD/L),  $K$  is maximum substrate consumption rate per microorganism mass (g COD/g VSS.d),  $\theta$  is hydraulic retention time (d) and  $\theta_c$  is solid retention time (d).

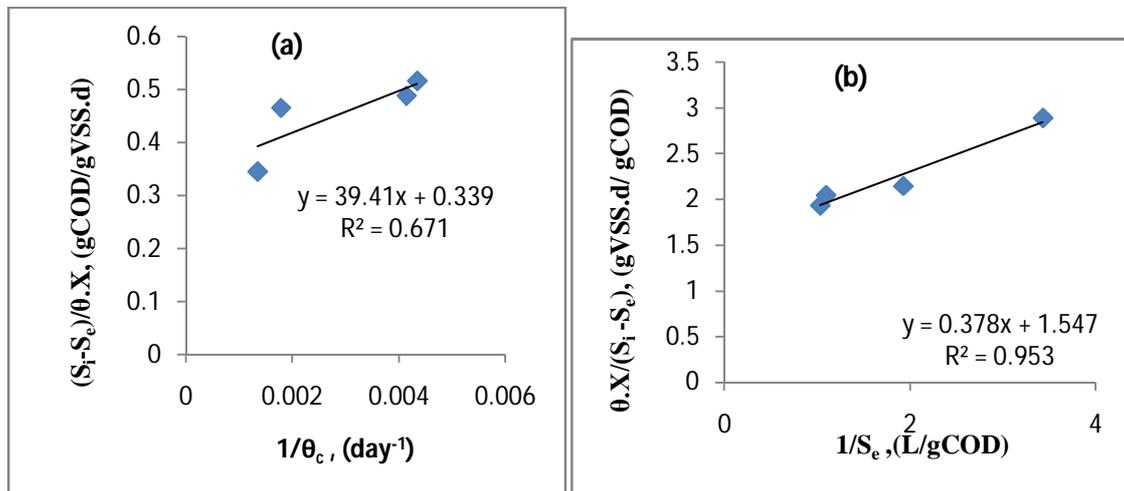


Fig 2. Diagram of determining synthetic coefficients of Y,  $K_d$ , K and  $K_s$  in monod model

Considering the linear equations 6 by plotting  $(S_1 - S_0)/\theta \cdot X$  in front of  $1/\theta_c$ , figure 2 (a) is obtained, by which synthetic coefficient Y and  $K_d$  were 0.0253 g VSS/g COD and 0.00847 d<sup>-1</sup> with correlation coefficient ( $R^2$ ) of 0.671. Also based on figure 2 (b) that is plotting  $\theta \cdot X / (S_1 - S_0)$  in front of  $1/S_0$  by linear equation 7, synthetic coefficients K,  $K_s$  are 0.646g COD/g VSS. d and 0.244 g COD/L with correlation coefficient ( $R^2$ ) of 0.953.

#### IV. CONCLUSION

In mathematical approach six independent variables operation time, organic loading rate, polymer loading, upflow velocity, specific density of granule and specific density of water are considered, which dependent on granule size in UASB reactor. From these dependent and independent variables make four dimensionless groups by using dimensionless approach Buckingham  $\pi$  - theorem. Indices of power multiplier function obtained by using NLINFIT tool of MATLAB2010a and simulate the granule size, which are close to the experimental data of granule size. A Monod type kinetic model with a correlation coefficient of 0.671 and 0.953 was also found to be suitable for expressing the microbial kinetics of the UASB reactor.

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