

Control of Direct Current Electrical Machine: Stabilisation of Current and Speed by the Change of Voltage in the Armature for Direct Current in Excitation Winding

Biya Motto Frederic^{1*}, Tchuidjan Roger², Ndzana Benoit²

¹University of Yaounde, Yaounde, Cameroon

²National School of Engineering, Yaounde, Cameroon

Abstract: In the paper, we study the design basics of subordinate control system of direct current electric drive by the voltage change in armature with direct current in excitation winding. For the electrical transducer, we can use an electromechanical amplifier, a magnetic amplifier with rectifier that permit the regulation of output voltage through action on input signal.

Keywords: Stabilization; Armature voltage; Direct current; Electrical machine

I. INTRODUCTION

The electric circuit of electric drive with control on armature voltage is shown on Figure 1. The excitation winding LM is supplied from the current source $u_1 = u_N$, and the armature of electromotor M from the electrical transducer.

In the control system, we have the stabilization of armature current (electromagnetic moment), the speed and the position of functioning machine executive organ. The control information comes from current captors (CC) with Shunt (RS), Speed (BR) and Position (PC). The control system structure is built according to the principle of subordination control and is composed of current, speed and position loops [1].

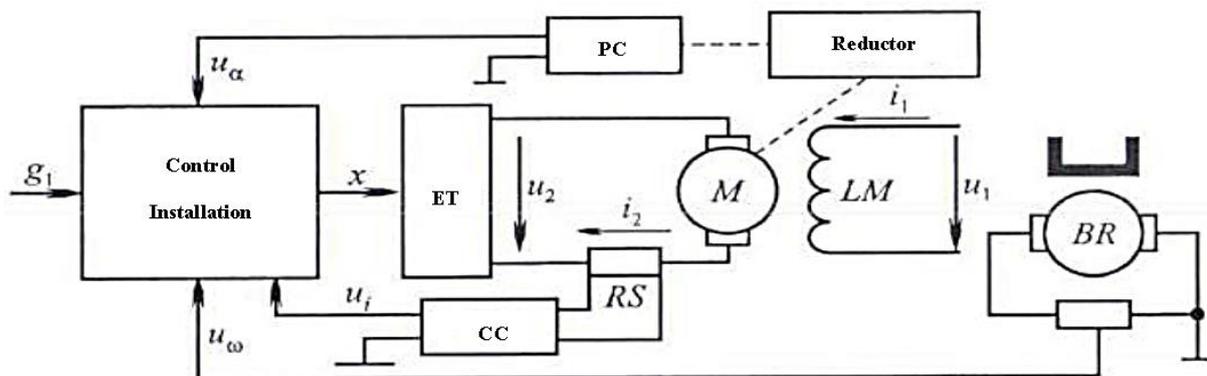


Figure 1: Electric circuit of direct current electric drive.

II. DESIGN OF CURRENT LOOP REGULATOR FOR THE ELECTROMOTOR ARMATURE

The formation of given dynamic characteristics of armature current will be done by the method of series correction. We form a control loop with regulator whose transfer function is W_{CR} (Figure 2) [2,3].

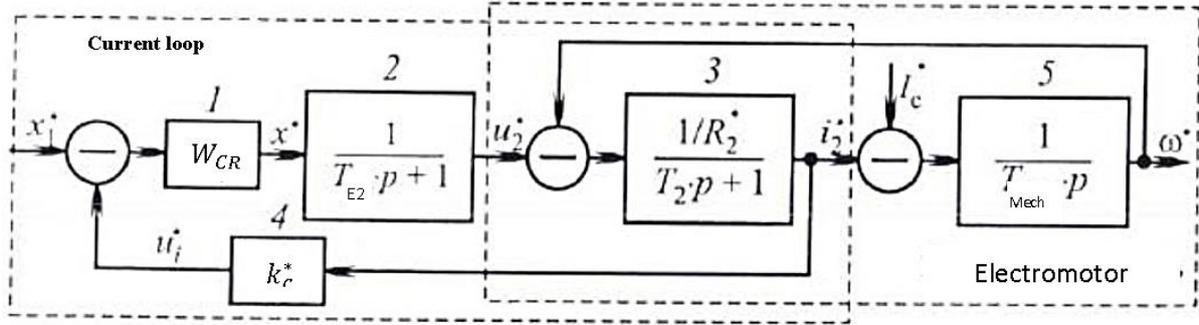


Figure 2: Control loop structural circuit: 1-Current regulator; 2-Electric transducer; 3-Electrical part of electromotor; 4-Current captor; 5-Mechanical part of electromotor.

The current loop must assure the stabilization of current (moment) on a level, given by input signal x_1^* .

2.1. Proportional-Integral Current Regulator

Let us define a simplified method for determination of transfer function of armature current regulator. We assume that the mechanical time constant is sufficiently high and is greater than the time constant of armature current and electric transducer. That is why a variation of speed ω does not influence the dynamics of armature current.

That assumption gives the possibility not to consider the internal feedback of electromotor on speed and we can consider that elements 2 and 3 of the structural circuit in Figure 2 are linked in series and form the control object of current loop. Thus the current control loop object has the following transfer function:

$$W_{oc2} = \frac{1}{T_{E2}P + 1} * \frac{1/R_2^*}{T_2P + 1}$$

The choice of transfer function of series correction element current regulator w_{CR} will be executed such that assuring standard dynamic characteristics that will create hopeful transfer function, equation (1):

$$W_h = \frac{1/K_c^*}{2 * T_\mu^* * P^2 + 2 * T_\mu * P + 1} \quad (1)$$

The transfer function of current regulator (2):

$$W_{CR} = \frac{1/K_c^*}{W_{oc2} * 2T_\mu^* * P * (T_\mu P + 1)} = K_{r2} + \frac{1}{T_r2 * P} \quad (2)$$

$$T_\mu = T_{E2}; K_{r2} = R_2 * T_2 / (2K_c^* * T_\mu) \quad \text{and} \quad T_r2 = 2 * K_c^* * T_\mu / R_2$$

The current loop with current regulator whose transfer function is defined by equation (2) will create transient process a little bit different from the etalon.

Let us consider the static control error provoked by neglecting the internal feedback of electromotor on speed.

By using the structural circuit of control current loop (Figure 2) we have $x^* = (x_1^* - K_C^* i_2^*) \cdot W_{CR}$

The equation for the armature current will be : $i_2^* = W_y \cdot x_1^* + W_B \cdot I_C^*$ (3)

Where $W_y = \frac{T_2 P + 1}{K_C^*} / Y(P)$ is the current loop transfer function on control signal X_1^* ;

$W_B = 2 \cdot \varepsilon \cdot (T_\mu P + 1) / Y(P)$ Is the current loop transfer function on perturbation signal I_c^* ;

$$\varepsilon = T_\mu / T_M ; \quad \varepsilon = T_\mu / T_M = R_2^* \cdot T_{Mech}$$

The characteristic polynom of transfer functions is $Y(P) = (T_2 P + 1) \cdot (2T_\mu^2 P^2 + T_\mu P + 1) + 2 \cdot \varepsilon (T_\mu P + 1)$

If we assume that $P = 0$ in equation (3), we have:

$$i_2^* = \frac{x_1^*}{K_C^* \cdot (1 + 2\varepsilon)} + \frac{2\varepsilon \cdot i_C^*}{(1 + 2\varepsilon)}$$

From that equation, the static error on control signal is:

$$\Delta i_2^* = \frac{x_1^*}{K_C^*} - x_1^* / K_C^* \cdot (1 + 2\varepsilon) = \frac{x_1^* \cdot 2\varepsilon}{K_C^*} \cdot (1 + 2\varepsilon)$$

From the errors expressions, we see that their value is determined $\varepsilon = T_\mu / T_M$

2.2. Proportional Intergral – Integral Current Regulator

For high value of $\varepsilon = T_\mu / T_M$ errors of loop current can be significant. We can obtain astatic control system with current if we consider internal feedback of electromotor on speed. In that case, the current control loop object is the transfer function.

$$i_2^* = W_{11} \cdot x_1^* + W_{11} \cdot I_C^*$$

The equation for the current regulator's transfer function is:

$$W_{CR} = \frac{1/K_C^*}{w_{11} \cdot 2 \cdot T_\mu P (T_\mu P + 1)} = K_{r_2} + \frac{1}{T_{r_2} P} + \frac{1}{T_{r_2} \cdot T_M \cdot P^2} \quad (4)$$

$$\text{Where } T_\mu = T_{E2} ; K_{r_2} = \frac{R_2^* \cdot T}{2 \cdot K_c^* \cdot T_\mu} ; T_{r_2} = \frac{2 \cdot K_2^* \cdot T_\mu}{R_2^*} ; T_M = R_2^* \cdot T_{Mech}$$

Thus, current regulator is composed of three components: proportional part, integral regulator of first order and integral regulator of second order.

The transfer functions of current loop on control X_1^* and perturbation I_c^* signals are defined as follows, equation (5):

$$W_y = \frac{i_2^*}{x_1^*} = \frac{1/K_C^*}{2 \cdot T_\mu^2 \cdot P^2 + 2 \cdot T_\mu P + 1} \quad (5)$$

$$W_B = \frac{i_2^*}{I_c^*} = \frac{2(T_\mu P + 1)T_\mu P}{(2T_\mu^2 P^2 + 2T_\mu P + 1) + T_M T_2 P^2 + T_M P + 1}$$

In those expressions, if we assume $P=0$ in the established regime armature current $i_{2M}^* = \frac{x_1^*}{K_c^*}$ is proportional to the control signal I_c^* and does not depend on resistance current I_c^* .

2.3. Two-Loop Current Regulator

To obtain an astatic control system with current is possible by building a second loop of current, whose control object is the first loop. The transfer function of first current loop W_y can be approximated by first order element:

$$w_y = i_2^* / x_1^* \approx \frac{1}{K_c^*} / (2T\mu P + 1)$$

Then the second loop regulator on technical optimum will be integral:

$$w_{CR2} = \frac{1/K_c^*}{w_y * 2T\mu_1 P * (T\mu_1 P + 1)} = \frac{1}{4T_\mu P}, \text{ where } T\mu_1 = 2T\mu$$

The structural circuit for two-loop control system of armature current is shown on Figure 3.

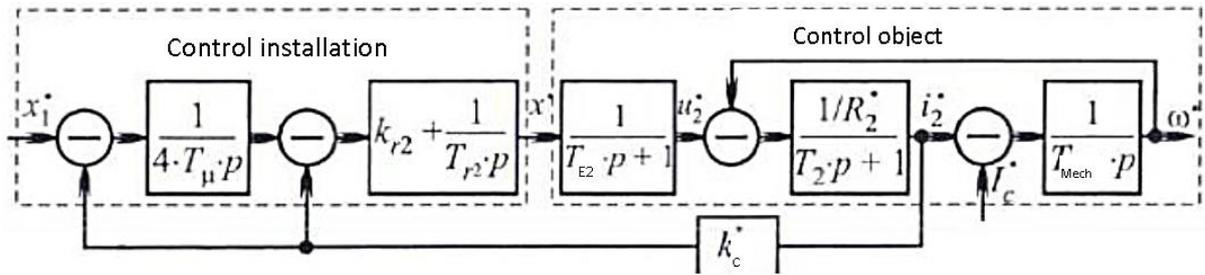


Figure 3: Two-loop control system of armature current.

III. LIMITATION OF ELECTROMOTOR ARMATURE CURRENT

The maximal value of armature current I_{max} should be limited from the views of assuring given static and dynamic loads of the electric drive mechanism and reliable functioning of collector mechanism [4].

The limitation of current at a given level I_{max}^* can be done by limitation of input signal of current loop x_1^* .

If the maximal value I_{max}^* is known, then the value x_{1max}^* is found through the expression of regulation characteristic $x_{1max}^* = K_C^* I_{max}^*$

We consider $x_{1max}^* = 1$, therefore the transfer coefficient of current captor in per – units $K_C^* = \frac{1}{I_{max}^*}$.

The element of armature current limitation is non-linear. The relation between input signal x_2^* and output signal x_1^* can be described in the equation (6):

$$x_1^* = x_2^* \text{ for } |x_2^*| < 1 \text{ and } 1 \text{ for } |x_2^*| \geq 1 \quad (6)$$

The limitation of armature current element is established at the entrance of current loop, as shown in Figure 4.

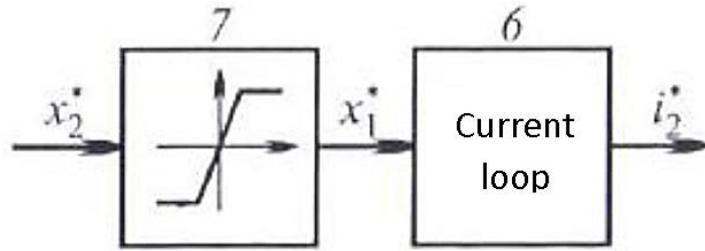


Figure 4: Current loop 6 and current limitation element 7.

IV. DESIGN OF REGULATOR FOR ARMATURE ROTATION SPEED OF ELECTROMOTOR

For regulation of armature rotation speed, we build speed control loop (Figure 5) [5]. This loop is assured by a convenient choice of speed regulator transfer function W_{sr} . The transfer coefficient of speed captor is chosen in such a way that the maximal speed corresponds with basic control system signal U_B . In that case $K_S^* = \frac{1}{\omega_{max}^*}$

For the choice of transfer function of speed regulator 8 we assume that the current limiter 7 functions on the linear part of characteristic "Input – Output" and the signal $x_1^* = x_2^*$. The regulation object of speed loop is the mechanical part of electromotor 5 and current loop 6 (Figure 5)

The transfer function of current loop is defined by the choice of current regulator and it has etalon aspect (1) at mechanical part of electromotor:

$$W_{so} = \frac{1/K_c^*}{(2T_\mu^2 P^2 + 2T_\mu + 1) \cdot T_{Mech} P} \approx \frac{1/K_c^*}{(2T_\mu P + 1) \cdot T_{Mech} P}$$

The transfer function of speed regulator is chosen such that it has standard transfer function of speed loop aspect, equation (7):

$$W_h = \frac{1/K_c^*}{2T_\mu^2 P^2 + 2T_\mu P + 1} \quad (7)$$

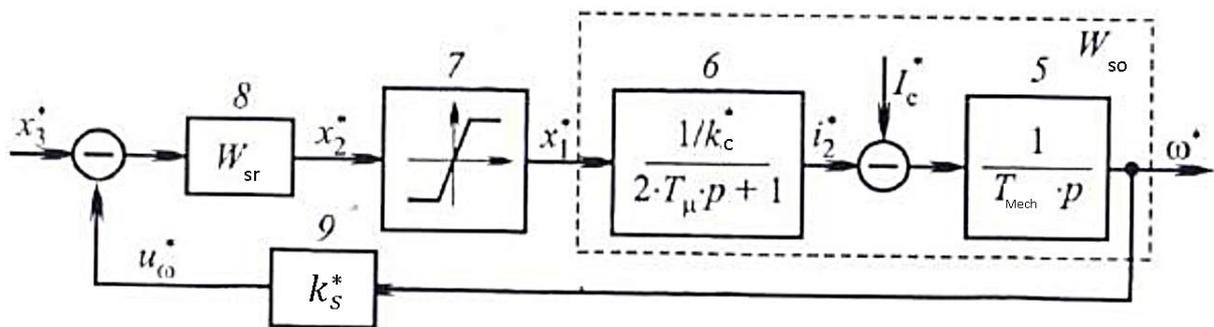


Figure 5: Structural circuit of armature rotation speed loop. 5- mechanical part of electromotor. 6 - current loop; 7- current limiter; 8- speed regulator; 9- speed captor.

If we assume $T_{\mu 1} = 2T_\mu$, then speed regulator transfer function will be a proportional element in equation (8):

$$W_{sr} = \frac{1/K_c^*}{W_{so} \cdot 2T_{\mu 1} \cdot P(T_{\mu 1} P + 1)} = \frac{K_c^* T_{Mech}}{K_S^* \cdot 4T_\mu} = K_{sr}^* \quad (8)$$

Using the structural circuit of speed loop:

$$[x_3^* - k_s^* \cdot \omega^*] \cdot W_{sr} \cdot W_{so} - I_c^* = T_{Mech} \cdot P \cdot \omega^*, \text{ Or } \omega^* = W_{slc} \cdot x_3^* - W_{slp} \cdot I_c^* \quad (9)$$

$$\text{Where } W_{slc} = \frac{1 / K_s^*}{8T_\mu^3 P^3 + 8T_\mu^2 P^2 + 4T_\mu P + 1}$$

$$;$$

$$W_{slp} = \frac{(2T_\mu^2 P^2 + 2T_\mu P + 1) \cdot 4T_\mu / T_{Mech}}{8T_\mu^3 P^3 + 8T_\mu^2 P^2 + 4T_\mu P + 1}$$

The transfer functions of speed loop on control and perturbation signal respectively.

If we assume on equation (9) $P=0$, then we have static electromechanical characteristic of electric drive with proportional speed regulator, equation (10):

$$\omega^* = x_3^* / K_s^* - (4T_\mu / T_{Mech}) \cdot I_c^* \quad (10)$$

For $I_c^* = 0$, we have static characteristic of electric drive with proportional speed regulator, equation (11):

$$\omega^* = x_3^* / K_s^* \quad (11)$$

The static error for $I_c^* = 1$ is $\Delta\omega^* = -(4T_\mu / T_{Mech})$ In open loop, static error for nominal load $\Delta\omega_0^* = -R_2^*$.

From the expressions of static errors for closed and open loop systems, it appears that in closed loop system, the static error $\Delta\omega^*$ decreases for $4T_\mu / T_M$ times, when $T_M = R_2^* T_{Mech}$ is the electromechanical time constant.

V. DESIGN OF ADAPTIVE SPEED REGULATOR

The proportional speed regulator gives static error. If the level of error $\Delta\omega^* = -4T_\mu / T_{Mech}$ does not satisfy the technological process conditions, then we need to use an integral speed regulator. We therefore build a second speed loop [6].

The structural circuit of second speed loop is shown on Figure 6.

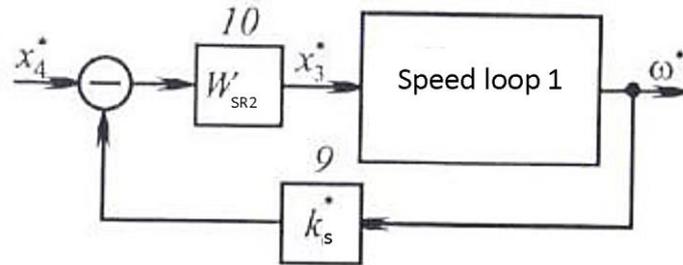


Figure 6: Structural circuit of second speed loop: 9-speed captor; 10- second speed loop regulator the first speed loop that has the transfer function.

$W_{slc} \approx \frac{1/K_s^*}{4T_\mu P + 1}$ is the control object of the second speed loop. If the hopeful transfer function for second

speed loop is $W_h = \frac{1/K_s^*}{2T_\mu^2 P^2 + 2T_{\mu_2} P + 1}$

Then the transfer function of second speed regulator is:

$$W_{sr2} = W_{sr2} = \frac{1/K_s^*}{W_{slc} * 2T_\mu P * (T_{\mu_2} P + 1)} = \frac{1}{8T_\mu P} \quad (12)$$

An integral element with $T_{\mu_2} = 4T_\mu$

From Figure 6 we have $x_3^* = (x_4^* - k_5^* \cdot \omega^*) * W_{sr2}$

By replacing that expression in (9), we find the Laplace representation of armature rotation speed, equation 9:

$$\omega^* = W_{slc2} * x_4^* - W_{slp2} * I_c^* \quad (13)$$

Where W_{slc2} , W_{slp2} transfer functions of speed loop ω^* on control signal x_4^* and on perturbation signal I_c^* respectively.

We have;

$$W_{slc} = \frac{1/K_s^*}{(8T_\mu^2 P^2 + 4T_\mu P + 1)^2};$$

$$W_{slp2} = 32 \frac{(2T_\mu^2 P^2 + 2T_\mu P + 1) * T_\mu^2 * P}{(8T_\mu^2 P^2 + 4T_\mu P + 1)^2 * T_{Mech}}$$

If we assume in equation (13) that $P=0$, we have the expression for electromechanical characteristic of electric drive with proportional speed regulator $\omega^* = x_4^* / K_s^*$. The static error is therefore equal to zero.

The dynamic error of speed stabilization is characterized by transient characteristic (Figure 7), created by the transfer function $W_{slp2} * T_{Mech} / T_\mu$.

The maximal speed drop for nominal load $\Delta\omega^* = -3,82 T_\mu^* / T_{Mech}$ is reached for $t=5,9 T_\mu^*$

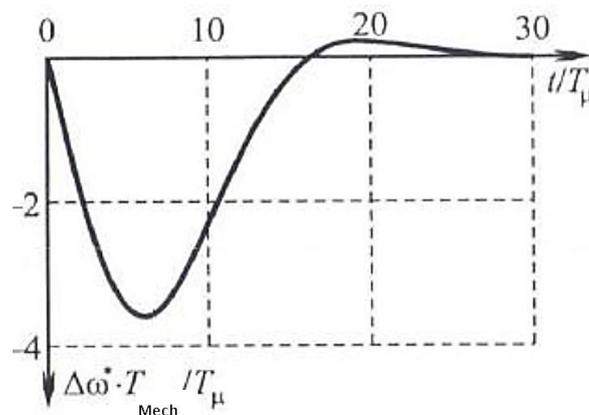


Figure 7: Transient characteristic created by transfer function $W_{slp2} * T_{Mech} / T_\mu$.

For obtention of astatic current stabilization system, we need a regulator whose integral stabilisator is a second order one. For the armature current limitation in the input of control current loop, we need to install an element of input signal limitation.

For formation of etalon dynamic processes with control of armature rotation speed of direct current electrical machine with independent excitation, we need to build control loop with proportional regulator.

Speed stabilization static error depends on load current. In closed loop system with proportional regulator for nominal load, the static error decreases by $4T_{\mu} / T_M$ times compared to open loop system. For the obtention of astatic system of speed stabilization, we need an adaptive speed regulator

VII. REFERENCES

- [1]. YSE Ali; Noor SBA; Uashi SM; Hassan MK; Microcontroller for DC Motor Speed Control. IEEE 2003; 7803-8208.
- [2] Nandkishor PJ; Ajay PT; Speed Control Of DC Motor Using Analog PWM Technique. International Journal of Engineering Research & Technology 2012; 1: 1-16.
- [3] Milivojevic N; Mahesh K; Yusuf G; Stability Analysis of FPGA-Based control of Brushless DC Motors and Generators Using Digital PWM Technique. IEEE Transactions on Industrial Electronics 2012; 59: 1.
- [3] Hong W; Vikram K; Internet-Based Remote Control of a DC Motor using an Embedded Ethernet Microcontroller
- [4] Abu ZA; Mohd Nasir T; A study on the DC Motor Speed Control by UsingBack-EMF Voltage. Asia sense sensor 2003; 359-364
- [8] Chia AY; Yen S; Digital Pulsewidth Modulation Technique for a synchronous Buck DC/DC Converter to Reduce Switching Frequency. IEEE Transactions on Industrial Electronics 2012; 59.
- [5] Zhen Y; Space-vector PWM with TMS320C24x using hardware and software determined switching patens,” SPRA524. Texas Instruments 1999; 4-5.
- [6] A text book by mazidi and Mazidi and Ayla