Improved Diagnosis and Fault Tolerant Control Wind Power System Using Sliding Mode Observer

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Abstract: In this paper, we present a grid-connected wind turbine equipped with double-fed induction generator directly connected to the grid in the stator side and interconnected via a power converter in the rotor side. Then we present a fault tolerant control (FTC) based on sliding mode observer for stator winding fault of DFIG. We develop an algorithm that allows the passage from nominal controllers designed for healthy condition, to robust controllers designed for faulty condition. Simulation results have shown good performances of the system under these proposed approach strategies.

Keywords: Wind turbine; Doubly fed induction generator; Sliding mode observer; Inter-turn short-circuit; diagnosis; Fault tolerant control

I. INTRODUCTION

To produce electrical energy using a wind energy conversion system (WECS), various control strategies have been developed in the literature [1]. All this strategies have the goal to bring down the cost of electrical energy produced by the WECS and to converge the system for operating at unity power factor. The field oriented control strategy (FOC) has attracted much attention in the past few decades but it suffers from the problem of the machine parameters variations, which comes to compromise the robustness of the control device [2]. Indeed, the PI regulators coefficients used in FOC strategy, are directly calculated according to the parameters machine what entrain a poor robustness vs parameters variations [3,4]. Vector control methods for DFIG have been addressed in some literatures [5]. DFIG is essentially a wound rotor induction machine in combination with bi-directional back to back PWM converters, in which the stator windings are directly connected to the grid and the rotor windings are injected with variable voltages at slip frequency. The rotor side converter is used to control the rotor injection voltages and the grid side converter is used to maintain a constant voltage on the DC link voltage. A typical configuration of a wind turbine DFIG is shown in Figure 1. Decoupled d-q vector control is a common control strategy of wind turbine DFIG, which is mainly realized by controlling the rotor side converter. This controller is consisted of two stages with the first stage for active and reactive power control and the second stage for d and q control signals through this two-stage controller, active power and reactive power can be controlled separately according to their setting points. To generate the maximum power, the active power setting point should be adjusted with the rotor speed according to maximum power extraction control strategy. This control strategy is implemented in this work to control the rotor voltage signals and give the reference values of the active and reactive power when the operating condition changes. The fault detection and localization unit detects the occurrence of fault and determines its nature. This can be realized by analyzing the change of the stator or rotor resistance and then take the appropriate decision: accept the default or stop the machine and execute a curative maintenance. This paper proposes a novel adaptive estimation method developed, to design an adaptive sliding mode observer, parameters changes can be tackled by using this method. Through adjusting the error between the reference and adjustable models by sliding mode algorithm, the estimated rotor resistance can be obtained. So, the proposed FTC is a combination between an active and passive FTC. The advantage of this FTC is that when the fault is not tolerant an alarm signal will indicate that the operator’s intervention is necessary. The FTC control method is implemented by Matlab/simulink and several steady and dynamic experimental results are given [6].

The schema of the device studied is given in Figure 1.
II. DFIG MODELING

2.1.1. Model in a-b-c Coordinate Reference Frame

In the stator reference frame (αs-βs), the mechanical/electrical energy conversion process is described by the equations of DFIG are defined by:

\[
\begin{align*}
V_{\alpha s} &= R_s i_{\alpha s} + \frac{d\psi_{\alpha s}}{dt} \\
V_{\beta s} &= R_s i_{\beta s} + \frac{d\psi_{\alpha s}}{dt} \\
V_{\alpha r} &= R_s i_{\alpha r} + \frac{d\psi_{\alpha r}}{dt} + \omega \psi_{\beta r} \\
V_{\beta r} &= R_s i_{\beta r} + \frac{d\psi_{\beta r}}{dt} + \omega \psi_{\alpha r}
\end{align*}
\]

The electromagnetic torque can be expressed by:

\[
C_{em} = p \frac{M_{qr}}{L_s} (\psi_{\alpha s} i_{qr} - \psi_{qr} i_{\alpha r})
\]
In a stationary reference frame ($\alpha$-$\beta$s), the DFIG electrical equations written in the state-space can be expressed as follows:

$$\frac{dX}{dt} = AX + BU$$

$$Y = CX$$

(4)

With $X = \begin{bmatrix} i_{\alpha s} & i_{\beta s} & \Phi_{ar} & \Phi_{br} \end{bmatrix}^T$, $Y = \begin{bmatrix} i_{\alpha s} \\ i_{\beta s} \end{bmatrix}$ and

$$u = \begin{bmatrix} u_{\alpha s} & u_{\beta s} & u_{ar} & u_{br} \end{bmatrix}^T$$

$$A = \begin{bmatrix} A_{11} & A_{12} \\ A_{21} & A_{22} \end{bmatrix}, B = \begin{bmatrix} B_{11} & B_{12} \\ B_{21} & B_{22} \end{bmatrix}, I = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$ and $J = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$

With

$$A_{11} = \begin{bmatrix} -1 & \frac{L_m^2}{\sigma \tau_s \tau_r \sigma L_s L_r} \\ 0 & 0 \end{bmatrix}$$
\[ A_{12} = \begin{bmatrix} \frac{L_m}{\tau_s \sigma L_s L_r} & \frac{wL_m}{\sigma L_s L_r} \\ \frac{wL_m}{\sigma L_s L_r} & \frac{L_m}{\tau_s \sigma L_s L_r} \end{bmatrix} \]

\[ A_{21} = \begin{bmatrix} \frac{L_m}{\tau_s} \\ 0 \end{bmatrix}, \quad A_{22} = \begin{bmatrix} -\frac{1}{\tau_s} & -w \\ \frac{w}{\tau_s} & -1 \end{bmatrix} \]

\[ B_{11} = \begin{bmatrix} \frac{1}{\sigma L_s} \\ 0 \end{bmatrix}, \quad B_{12} = \begin{bmatrix} -\frac{L_m}{\sigma L_s L_r} & 0 \\ \frac{L_m}{\sigma L_s L_r} & 0 \end{bmatrix} \]

\[ B_{21} = \begin{bmatrix} 0 \\ 0 \end{bmatrix}, \quad B_{22} = \begin{bmatrix} 1 & 1 \\ 1 & 1 \end{bmatrix} \]

Where, \( R_s \) and \( R_r \) are the stator and rotor resistance, respectively. \( L_s, L_r \) and \( L_m \) are the stator and rotor full inductance, the magnetization inductance, respectively.

The electromagnetic torque equation becomes [7]:

\[ C_e = \frac{3}{2} p \frac{L_m}{L_r} \left( \Phi_{\alpha r} i_{\beta s} - \Phi_{\beta r} i_{\alpha s} \right) \]  

(5)

### III. VECTOR CONTROL OF DFIG

In order to establish a vector control of DFIG, we recall here its modelling in the Park frame. The equations of the stator voltages and rotor of the DFIG are defined by equation (1 and 2).
The equations of stator and rotor flux are given as follows [8]:

\[
\begin{align*}
\psi_{ds} &= L_s i_{ds} + M_{sr} i_{dr} \\
\psi_{qs} &= L_s i_{qs} + M_{sr} i_{qr} \\
\psi_{dr} &= L_s i_{dr} + M_{rs} i_{ds} \\
\psi_{qr} &= L_s i_{qr} + M_{rs} i_{qr}
\end{align*}
\]

The electromagnetic torque can be expressed by:

\[
C_{em} = p \frac{M_{sr}}{L_s} (\psi_{dr} i_{qr} - \psi_{qr} i_{dr})
\]

The principle of vector control with stator flux oriented of the DFIG is shown in Figure 3. The stator flux vector will be aligned on the ‘d’ axis and the stator voltage vector on the ‘q’ axis, this last constraint is favorable to obtain a simplified control model.

![Figure 3: Stator voltage and flux vectors in the axis system.](image)

The electromagnetic torque equation becomes:

\[
C_{em} = p \frac{M_{sr}}{L_s} \psi_{dr} i_{qr}
\]

Assuming the grid is connected to the DFIG is stable, the flux \( \psi_{ds} \) becomes constant. The choice of this reference makes the electromagnetic torque and the active power produced by the machine. Dependent only of ‘q’ axis rotor current components [9].
In the same reference, the tensions can obtain by equations:

\[
\begin{align*}
    V_{ds} &= 0 \\
    V_{qs} &= V_s = \omega_s \psi_{ds} = \omega_s \psi_{d'}
\end{align*}
\]  

(12)

Using the previous simplifications, the stator flux equations can be written by:

\[
\begin{align*}
    \psi_s &= L_s I_{ds} + M_{sr} I_{dr} \\
    0 &= L_s I_{qs} + M_{sr} I_{qr}
\end{align*}
\]  

(13)

The equations linking the stator currents to the rotor currents are deduced below:

\[
\begin{align*}
    I_{ds} &= \frac{\psi_s - M_{sr} I_{dr}}{L_s} \\
    I_{qr} &= \frac{-M_{sr} I_{qr}}{L_s}
\end{align*}
\]  

(14)

In park reference, the stator active and reactive power of an induction machine are expressed as:

\[
\begin{align*}
    P_s &= V_{ds} I_{ds} + V_{qs} I_{qs} \\
    Q_s &= V_{qs} I_{ds} + V_{ds} I_{qs}
\end{align*}
\]  

(15)

By replace the equation (14) and (15) in (16), the active and reactive powers can be written as a function of rotor currents as follows [10-12]:

\[
\begin{align*}
    P_s &= -V_s \frac{M_{sr}}{L_s} I_{qr} \\
    Q_s &= V_s \psi_s - V_s \frac{M_{sr}}{L_s} I_{dr}
\end{align*}
\]  

(16)

The rotor voltages can be written as a function of rotor currents as follows:

\[
\begin{align*}
    V_{dr} &= R_r I_{dr} + \left( L_r - \frac{M_{sr}^2}{L_s} \right) \frac{d}{dt} I_{dr} + g \omega_s \left( L_r - \frac{M_{sr}^2}{L_s} \right) I_{qr} \\
    V_{qr} &= R_r I_{qr} + \left( L_r - \frac{M_{sr}^2}{L_s} \right) \frac{d}{dt} I_{qr} + g \omega_s \left( L_r - \frac{M_{sr}^2}{L_s} \right) I_{dr} + g \omega_s \frac{M_{sr} V_s}{\omega_s L_s}
\end{align*}
\]  

(17)

After applying the Laplace transformation to the equations (16) and (17) gives:
IV. MODELLING OF DFIG WITH STATOR INTER–TURN FAULT

A DFIG model in a-b-c coordinate reference frame is derived to describe the inter-turn short circuit fault at any level in any single phase of rotor. In this model, the fault position parameter $f$ is defined as below for three cases that fault occurs in phase ‘a’, ‘b’ and ‘c’, respectively.

$$f_a = [1\ 0\ 0]^T, f_b = [0\ 1\ 0]^T, f_c = [0\ 0\ 1]^T$$

The fault level parameter $\gamma$ denotes the fraction of the shorted winding.

For modelling this defect, we assume that a number of turns « $\gamma$ » from among those « a » is short circuited. This section of turns short circuit is defined by coefficient « $\gamma$ » between the number of turns short - circuited and the total number of turns of the phase « a », this coefficient is introduced in the mathematical model governing the operation of the machine. The modeling of the DFIG with fault is to introduce resistance « $fR$ » in parallel with the turns short circuit in phase infected (Figure 4).

A voltage will be induced in mesh short-circuit, the voltage induced circulating current in the shorted turns called fault current, This latter has a proportional relationship with the fault resistance and induced voltage.

Therefore the inductance and resistance of the faulty phase change and the mutual inductance between this phase and all other windings of the machine well be changed. The new form of the equations of stator voltages is then rewritten as follows [13]:

$$[V_s] = [R_s][I_s] + \frac{d[y_{s}]}{dt}$$

Figure 4: Stator winding configuration with the inter-turn short circuit fault in phase ‘a’.
The stator resistance matrix can be rewritten as follows:

\[
\begin{bmatrix}
(1-\gamma)R_s & 0 & 0 & \gamma R_s \\
0 & R_s & 0 & 0 \\
0 & 0 & R_s & 0 \\
0 & 0 & 0 & \gamma R_s \\
\end{bmatrix}
\]  

(19)

However, we keep the matrix of stator voltages unchanged [14-16].

If we mean by «\(\gamma\)» fraction of the number of shorted turns of phase «a», then we have a healthy portion of a fraction \(1-\gamma\) of turns and we suppose the phases "b" and "c" healthy. We will have the new inductance stator matrix following:

\[
\begin{bmatrix}
(1-\gamma)^2 & (1-\gamma) & (1-\gamma) \\
0 & 1 & 0 \\
0 & 0 & 1 \\
(1-\gamma)^2 & 0 & 0 \\
\end{bmatrix}
\]

(20)

Therefore, the matrix of mutual inductances is:

\[
\begin{bmatrix}
(1-\gamma) \cos(\theta_r) & (1-\gamma) \cos \left( \theta_r + \frac{2\pi}{3} \right) & (1-\gamma) \cos \left( \theta_r - \frac{2\pi}{3} \right) \\
(1-\gamma) \cos \left( \theta_r - \frac{2\pi}{3} \right) & \cos(\theta_r) & \cos \left( \theta_r + \frac{2\pi}{3} \right) \\
(1-\gamma) \cos \left( \theta_r + \frac{2\pi}{3} \right) & \cos \left( \theta_r - \frac{2\pi}{3} \right) & \cos(\theta_r) \\
\gamma \cos(\theta_r) & \gamma \cos \left( \theta_r + \frac{2\pi}{3} \right) & \gamma \cos \left( \theta_r - \frac{2\pi}{3} \right) \\
\end{bmatrix}
\]

(21)

Rotor inductance matrix remains equal to that of the healthy cases.

V. SLIDING MODE OBSERVER

Many schemes have been developed to estimate parameter of DFIG from measured terminal quantities. One of these estimation systems are based on sliding mode technique. In order to obtain a better estimation, it is necessary to have dynamic representation based on the stationary (\(\alpha, \beta\)) reference frame. Since machine voltages and currents are measured in a stationary frame, it is also convenient to express these equations in stationary (\(\alpha, \beta\)) reference frame. We use the state-space form using stator currents and rotor fluxes as expressed in the previous section. The idea is that the error between the actual and observed stator currents converges to zero, which guarantees the accuracy of the rotor...
flux observer. So, we define a sliding surface $S=[S_1\ S_2]$ as to converge to zero the two sliding variables (i.e. $S_1=0$, $S_2=0$) [17-20] (Figure 5).

![Principle of sliding mode observer](image)

Figure 5: Principle of sliding mode observer.

The model of the observer is written:

$$\frac{d\hat{X}}{dt} = A\hat{X} + BU + G\text{sign}(Y - \hat{Y})$$

$$\hat{Y} = C\hat{X}$$

$$X = [i_{\alpha s}\ i_{\beta s}\ \Phi_{\alpha r}\ \Phi_{\beta r}]', \quad Y = \begin{pmatrix} i_{\alpha s} \\ i_{\beta s} \end{pmatrix}$$

With

$$u = \begin{pmatrix} u_{\alpha s} \ u_{\beta s} \ u_{\alpha r} \ u_{\beta r} \end{pmatrix}'$$

$$A = \begin{pmatrix} -\frac{R_s}{\sigma L_s} + \left(\frac{R_s L_m^2}{\sigma L_s^2}\right) & L_m & \frac{R_s}{L_r} (I - \omega J) \\ \frac{L_m R_r}{L_r} I & -\frac{R_r}{L_r} (I - \omega J) \end{pmatrix}$$

$$\hat{A} = \begin{pmatrix} -\frac{R_s}{\sigma L_s} + \left(\frac{R_s L_m^2}{\sigma L_s^2}\right) & L_m & \frac{R_s}{L_r} (I - \hat{\omega} J) \\ \frac{L_m R_r}{L_r} I & -\frac{R_r}{L_r} (I - \hat{\omega} J) \end{pmatrix}$$

$$B = \begin{pmatrix} \frac{1}{\sigma L_s} I \\ \frac{L_m}{\sigma L_s L_r} I \\ 0_{2\times2} \end{pmatrix}, \quad C = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{pmatrix}$$
We put

\[ a = \frac{1}{\sigma L_s} \left( R_s + R_r \frac{L_m^2}{L_i} \right), \quad b = \sigma L_s L_r, \quad \sigma = 1 - \frac{L_m^2}{L_s L_r} \]

\[ I_s = \left[ \text{sign}(S_1) \text{sign}(S_2) \right]^T \quad \text{and} \quad \begin{cases} x_1 - \dot{x}_1 \\ x_2 - \dot{x}_2 \end{cases} \]

\( S_1, S_2 \) represent the sliding surfaces.

The gains: \( q_1, \lambda_{11}^T, \lambda_{21}^T, \lambda_{31}^T, \lambda_{41}^T, \lambda_{51}^T \) are calculated to ensure the asymptotic convergence of errors estimation. They are given by:

\[
\begin{bmatrix}
\lambda_{11}^T \\
\lambda_{21}^T
\end{bmatrix} = D^{-1} \begin{bmatrix}
\delta_1 & 0 \\
0 & \delta_2
\end{bmatrix}
\]

\[ D = \frac{1}{a^2 + (kpx_5)^2} \begin{bmatrix}
a & -kpx_5 \\
kpx_5 & a
\end{bmatrix} \]

\[
\begin{bmatrix}
\lambda_{31} & \lambda_{32} \\
\lambda_{41} & \lambda_{42}
\end{bmatrix} = \begin{bmatrix}
-c & -px_5 \\
px_5 & -c
\end{bmatrix} \begin{bmatrix}
q_3 & 0 \\
0 & q_4
\end{bmatrix} \begin{bmatrix}
\delta_1 & 0 \\
0 & \delta_2
\end{bmatrix}
\]

(23)

\[
\begin{bmatrix}
\lambda_{51} \\
\lambda_{52} \\
\delta_1 \\
\delta_2
\end{bmatrix} = a \begin{bmatrix}
x_2 \\
x_1
\end{bmatrix}
\]

The residual signal is calculated as \( \tilde{r} = [y - \hat{y}] \) follows, and we define as the detection threshold (lower limit), which is set according to some pre-specified (expected) system performances. The objective is to determine the mechanism adaptation of the speed and the rotor resistance. The structure of the observer is based on the DFIG model in stator reference frame.

The rotor resistance estimation can be written as follows:
With: $\lambda$ is a positive scalar.

VI. SIMULATION RESULTS

The simulation behaviour of DFIG that we present in this part will help analyze the outputs variables with stator active and reactive power imposition to maximize the developed for both conditions with and without stator interturn short circuit fault applied as a wind turbine generator. The technique presented in the previous sections has been implemented in the MATLAB/simulink. The simulation test involves the wind speed variation and the reactive power reference constant equals to zero, as shown in the Table 1.

6.1. Health Operation

Several tests have been performed to check the accuracy of the proposed model in the first step, the DFIG is tested and simulated in a healthy operation with a rotor speed of 1440 rpm. The wind speed applied to the machine then active and reactive power developed as shown in Figures 6-11.

<table>
<thead>
<tr>
<th>t (s)</th>
<th>0</th>
<th>4</th>
<th>7</th>
</tr>
</thead>
<tbody>
<tr>
<td>V(m/s)</td>
<td>12</td>
<td>14</td>
<td>13</td>
</tr>
<tr>
<td>Qsref (var)</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
</tbody>
</table>

Table 1: Variation of wind speed

Figure 6: Speed of healthy DFIG and its reference with variation of wind speed.

Figure 7: Electromagnetic torque.
6.2. Inter-turn Stator Fault Operation of the DFIG

In this part, we present simulation results for the DFIG operation with stator inter-turn short circuit fault. The inter-turn fault is introduced in winding of stator phase "a". The degree of short-circuit and the time of its application is presented in Table 2.

<table>
<thead>
<tr>
<th>t (s)</th>
<th>0</th>
<th>1</th>
</tr>
</thead>
<tbody>
<tr>
<td>g (%)</td>
<td>0.1</td>
<td>5</td>
</tr>
</tbody>
</table>

Table 2: Degree of short-circuit and the time of its application.

We present simulation results for the DFIG operation with stator inter-turn short circuit fault. The inter-turn fault is introduced in winding of stator phase "a". We note that the performances of DFIG reduced when the increase of the fault dergre that influences on the equilibrium of the three stator phases and therefore the equilibrium of the stator currents which affects the power output, this increase is due to the presence of short-circuit fault. Their responses present a deformations after augmentation of stator and rotor short-circuit fault degree to 5% à time t=1s.
Figure 9: Rotation speed and observed rotor resistance of the DFIG.

Figure 10: Stator reactive and active powers of faulty DFIG with wind speed variation.
VII. CONCLUSION

In this paper a new method has been presented to modeling of doubly-fed induction generator (DFIG) based wind turbine, and a new scheme of sliding mode observer of Double Fed Induction Generator, based on the estimation of the value of the rotor resistance. The estimation of the rotor resistance is based on the use of the error between real and estimated value of DFIG in faulty condition, this will have to improve the performances of robustness and stability and precision for the sliding mode observer. The results show that the proposed, even in presence of rotor resistance variation. The FTC control strategy has been validated steady-state conditions by Matlab/simulink.

Wind Turbine Parameters
Rated power: $P_s=7500$ W
Moment of the inertia: $J = 0.31125$ kg.m$^2$
Wind turbine radius: $R = 3$ m
Gear box ratio: $G = 5.4$
Air density: $\rho = 1.25$ kg/m$^3$

DFIG Parameters
Rated power: 7500 W
Mutual inductance: $L_m = 0.0078$ H
Stator leakage inductance: $L_s = 0.0083$ H
Rotor leakage inductance: $L_r= 0.0081$ H
Stator resistance: $R_s = 0.455$ $\Omega$
Rotor resistance: $R_r = 0.62$ $\Omega$
Number of pole pairs: $P = 2$
Moment of the inertia: $J = 0.31125$ kg.m$^2$
Viscous friction: $f_v=0.00673$ kg.m$^2$.s$^{-1}$
VIII. REFERENCES


