

# **Wind Power Potential Analysis Based on Different Methods Fitted in Weibull and Rayleigh Models for Wind Patterns in Juja and Naivasha**

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**ABSTRACT:** The wind speed characteristics of Juja, (altitude of 1416 m above sea level; 1° 10' S, 37° 7' E), Kenya was analysed at heights of 10 m and 30 m. The wind speed averages at 10 m and 30 m were found to be 2.54 m/s and 3.04 m/s, respectively. The wind shear exponents and roughness parameters were analysed and found to be 0.1652 and 0.0374 respectively. Weibull scale and shape parameters were obtained using Weibull-fit, Regression and the Maximum Likelihood. Wind speed modelling was done using the Weibull and Rayleigh probability distribution functions. Power densities for different methods were calculated. Results obtained from Juja site were compared with results acquired from Naivasha, St. Xavier site which is at an altitude of 2,086 m; 0° 43' 0" S, 36° 26' 0" E. The mean wind power densities for Juja (10 m and 30 m) and Naivasha (10 m) were 12.68 W/m<sup>2</sup>, 20.65 W/m<sup>2</sup> and 39.95 W/m<sup>2</sup> by Weibull model and 14.51 W/m<sup>2</sup>, 22.43 W/m<sup>2</sup> and 28.63 W/m<sup>2</sup> by Rayleigh model respectively. The Weibull-fit and Maximum Likelihood fitted best Juja site and Naivasha site respectively.

**KEYWORDS:** Wind power density, Wind distribution models, Wind direction, Wind speed

## **I. INTRODUCTION**

Growing global population along with fast depleting reserves of fossil fuels is influencing researchers to search for clean and pollution free sources of energy which are sustainable and cost-effective. Due to the negative environmental effects of non-renewable energy systems such as global warming and climate change, there is need to shift to renewable systems of energy. The renewable energy systems include; solar, geothermal, wind, waves, tidal and bio-energies. Wind energy is a never ending natural resource which has shown great potential in combating climatic change while ensuring clean and efficient energy, yet it is the most under exploited energy resource. Wind turbine technology has led to significant growth of wind power generation across the world. However, wind energy is more sensitive to variations with topography and wind patterns compared to solar energy. It can be harvested economically if the turbines are installed in a windy area through selecting the most suitable wind turbine. Wind speed forecasting is a critical factor in assessing wind energy potential and performance of wind energy conversion systems. Wind fluctuation demands a necessary model describing its variation thereby estimating the amount of energy as well as to optimize the design of the wind turbine [1]. The most suitable wind turbine model which needs to be installed in a wind farm is selected through careful wind energy resource evaluation. It is therefore important to choose an accurate distribution model which closely mimics the wind speed distribution at a particular site [2]. The development and utilization of wind energy in developing countries, particularly Africa, has been hindered by absence of adequate measurements and assessment studies to ascertain its potential viability for power generation [3].

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(A High Impact Factor, Monthly Peer Reviewed Journal)

Vol. 5, Issue 1, January 2016

## II. BACKGROUND

Juja, 1416 m above sea level ( $1^{\circ} 10' S$ ,  $37^{\circ} 7' E$ ) and about 35 km from Nairobi, is a region that has a rapidly growing population and a major University, Jomo Kenyatta University of Agriculture and Technology (JKUAT). On the other hand, Naivasha, 2,086 m ( $0^{\circ} 43' 0'' S$ ,  $36^{\circ} 26' 0'' E$ ), is an area congested with agricultural farms. These two areas require an alternative energy source to supplement existing convectional energy. Use of power generators during power outage leads to air pollution and hence the need for clean, reliable, sustainable and cost effective sources. Wind energy is among the least exploited with 25.5 MW from the two Ngong wind farm phases, though there are underway processes of establishing other wind plants in Kenya such as in Turkana [4].

Thorough wind speed analysis in this area is therefore critical. A research based on different methods brings out a better picture of the state of wind in a site. The power available in wind is basically dictated by the wind speed. To obtain power from the wind, the force of the wind is harvested by the rotors of a wind turbine. Basically, the force on the wind is converted to a torque [5]. The power of the wind is proportional to the cube of wind velocity, the rotor area and the air density. This relation is shown in equation 1. It is however worth noting that the nature of the terrestrial surface including artificial obstacles such as hills, trees and buildings affects the wind speed.

Several methods and Probability Density Functions (PDFs) have been used in literature to describe wind speed characteristics. The methods include Weibull-fit, Regression, Standard deviation, Maximum Likelihood, Chi-square among others while PDFs include Weibull, Rayleigh, bimodal Weibull, lognormal and gamma among others [2]. The tabulations and mathematical formulas of these relationships are well described and explained in the procedures of analysing the bulk wind speed data. This paper analyses wind speed using different methods modelled using Weibull and Rayleigh models for Juja and correlates them with results from Naivasha, St. Xavier site within a period of three months.

## III. MATERIALS AND METHODS

The study was carried out in Juja at 10 m and 30 m heights in order to measure wind speeds and directions at the two heights above the ground. A mask of required length was constructed using metallic circular tubes. Anemometers (Ultrasonic wind sensors) were clamped on the mask at 10 m and 30 m in order to measure wind speeds and directions at these heights above the ground. The sensors were connected to transmitting devices (clamped on metallic rods) using insulated cords. The transmitters were linked with two Ultrasonic data loggers programmed so as one received data from 10 m and the other from 30 m centres. The data (diurnal averaged wind speed/direction and temperature) was stored in computer memory (disc) awaiting processing. The averages of wind parameters were obtained daily for three months. The wind shear exponents,  $\alpha$  surface roughness  $z_0$ , Weibull scale parameter  $c$ , shape parameter  $k$  and power densities were determined. Wind power potential was modelled using Weibull and Rayleigh distributions functions. The results were compared to acquired results from Naivasha, for the same months.

### Theory

The analysis of wind parameters was done using the following procedures;

#### Power available in the wind

Wind power,  $P$ , extracted from the wind of speed  $v$  using wind turbines with blades of cross-section area  $A$  is given by

$$P = \frac{1}{2} \rho A v^3 \dots\dots\dots 1$$

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Where;

$$\rho = \frac{P}{RT} \dots\dots\dots 1a ;$$

$P$  is air pressure,  $R$  gas constant and,  $T$  temperature in degrees Kelvin.

The wind velocity at the rotor plane is the average of upstream and downstream wind speeds. Maximum useful power is given by Betz's constant  $\approx 0.59$ .

### The power law

Wind speed near the ground changes with height; this involves an equation that forecasts wind speed at different height by using the available wind speed data. The most commonly used equation for the variation of wind speed with height is the power law [6] is;

$$v_2 = v_1 \left( \frac{h_2}{h_1} \right)^\alpha \dots\dots\dots 2$$

Where  $v_1$  (m/s) is the actual wind speed recorded at height  $h_1$  (m), and  $v_2$  (m/s) is the wind speed at  $h_2$  (m). The exponent  $\alpha$  depends on the surface roughness and atmospheric stability. Wind shear exponent, a difference in wind speed and direction vertically has been determined for various types of terrains [7].

Roughness length,  $z_0$  which is used to characterize shear and the height above the ground is not constant [8] and thus equation 2 can be modified to yield equation 3.

$$v_2 = v_1 \frac{\ln\left(\frac{h_2}{z_0}\right)}{\ln\left(\frac{h_1}{z_0}\right)} \dots\dots\dots 3$$

### Wind probability distributions

Two of the commonly used functions for fitting a field data probability distribution in a given location over a certain period of time are the Weibull and Rayleigh distribution models [9]. The Weibull probability density function,  $f_R(v)$  is given as;

$$f_R(v) = \frac{k}{c} \left( \frac{v}{c} \right)^{k-1} \exp\left(-\left(\frac{v}{c}\right)^k\right) \dots\dots\dots 4$$

The Rayleigh  $f_R(v)$  distribution is a special case of the Weibull distribution in which the shape parameter  $k=2$ . The probability density functions of the Rayleigh distribution is therefore given by;

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$$f_R(v) = \frac{2v}{c^3} \exp\left(-\left(\frac{v}{c}\right)^2\right) \dots\dots\dots 5$$

Methods of Obtaining Weibull Parameters

### Maximum Likelihood (MLH)

The parameters k and c (m/s) can be estimated by using the Maximum Likelihood Method [10, 11] as;

$$k = \left( \frac{\sum_{i=1}^n v_i^k \ln(v_i)}{\sum_{i=1}^n v_i^k} - \frac{\sum_{i=1}^n \ln(v_i)}{n} \right)^{-1} \dots\dots\dots 6$$

$$c = \left( \frac{1}{2} \sum_{i=1}^n v_i^k \right)^{\frac{1}{2}} \dots\dots\dots 7$$

### Weibull-fit

The shape and scale parameters as per Weibull-fit are as follows [11].

$$c = \frac{v_m}{\Gamma\left(1 + \frac{1}{k}\right)} \dots\dots\dots 8$$

$$k = \left( \frac{\sigma_v}{v_m} \right)^{-1.090} \dots\dots\dots 9$$

Where  $\sigma_v$  is standard deviation and  $v_m$ , the mean wind speed.

$$v_m = \left( \frac{\sum_{i=1}^n f_i v_i}{\sum_{i=1}^n f_i} \right) \dots\dots\dots 10$$

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$$\sigma_y = \left[ \frac{\sum_{i=1}^n f_i (v_i - v_m)^2}{\sum_{i=1}^n f_i} \right]^{\frac{1}{2}} \dots\dots\dots 11$$

### Regression

The cumulative probability function of the Weibull distribution [12] is given by;

$$F(v) = 1 - \exp \left[ - \left( \frac{v}{c} \right)^k \right] \dots\dots\dots 12$$

To determine k and c requires a good fit of the equation above to the recorded discrete cumulative frequency function. By taking the natural logarithm of both sides of equation 12 twice gives;

$$\ln \langle -\ln[1 - F(v)] \rangle = k \ln(v) - k \ln c \dots\dots\dots 13$$

Plotting  $\ln \langle -\ln[1 - F(v)] \rangle$  against  $\ln(v)$  Presents straight line whose gradient is  $k$  and the y-intercept is  $-k \ln c$  from which  $C$  can be calculated.

### Wind Power Density Function

The evaluation of wind power per unit area  $P_v$  is of fundamental importance in assessing wind power projects [13, 16].

The formula for  $P_v$  is given by;

$$P_v = \frac{1}{2n} \sum_{i=1}^n \rho (v_i^3) \dots\dots\dots 14$$

Where the wind speed at stage  $i$ , is  $v_i$ ,  $n$ , the number of non-zero wind data points and  $\rho$ , is air density. The  $\rho$  depends on altitude, air pressure and temperature and is approximated to be  $1.225 \text{ kg/m}^3$  at Juja. The expected monthly or annual wind power density per unit area of a site based on Weibull Probability Density Function  $P_w$  [12] can be expressed as follows;

$$P_w = \frac{1}{2} \rho c^3 \Gamma \left( 1 + \frac{3}{k} \right) \dots\dots\dots 15$$

Where  $c$  is the Weibull scale parameter (m/s) given by equation 8 and  $\Gamma$ , the gamma function.

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## Statistical Analysis of Wind Power Density Based on the Weibull and Rayleigh Models

The two significant parameters  $k$  and  $c$  are closely related to the mean value of the wind speed  $v_m$  [14]. By extracting  $c$  from equation 15 and setting  $k = 2$ , the power density for the Rayleigh model ( $P_R$ ) is found to be;

$$P_R = \frac{3}{\pi} \rho (v_m)^3 \dots\dots\dots 16$$

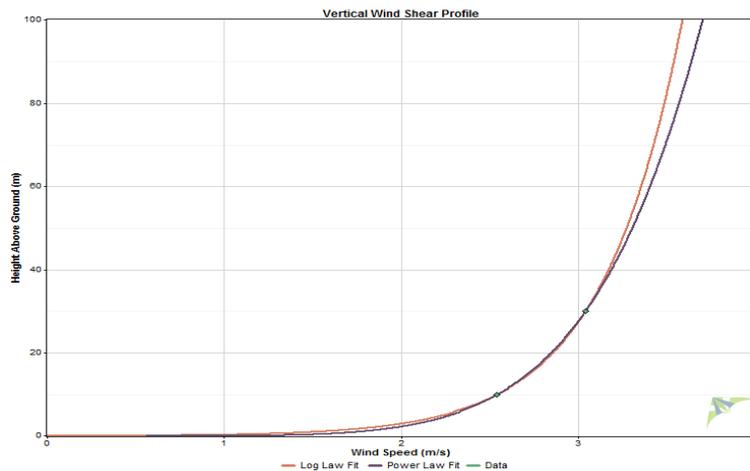
Where:

$$V_m = c \Gamma\left(\frac{3}{2}\right) = 0.88623c \dots\dots\dots 17$$

### IV. RESULTS AND DISCUSSION

#### Wind Shear

Average diurnal wind speeds, wind directions, and temperatures were obtained for three months. The average wind speeds for Juja at 10 m and 30 m heights were 2.54 m/s and 3.04 m/s respectively. Wind shear exponent and roughness parameters for Juja were 0.1652 and 0.0374 respectively. These parameters are in line with Linacre and Geerarts 1999, [7]. The wind shear profile was obtained by use of Windographer software (figure 1). Diurnal variation for the whole period of three months is shown by figure 2.



**Figure 1:** Wind shear profile

The wind profile was a plot of vertical height above the ground against wind speed for the months (March to May, 2015). The curves are in line with vertical wind speed profile by [8].

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## Diurnal variation of average wind speeds and directions

Diurnal variation of average wind speeds was obtained by use of Microsoft Excel and was as per figure 2.

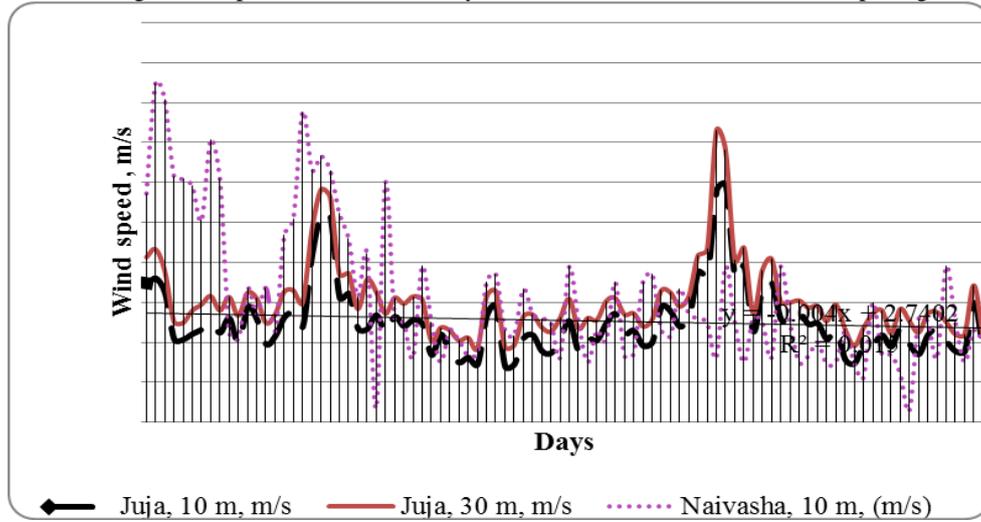


Figure 2: Diurnal variation of wind speeds, March - May, 2015

The two sites had low wind speeds of wind class 1, though wind speeds in March and at the beginning of May, were slightly higher as observed in figure 2. This can be attributed to higher temperatures which led to increase in pressure gradient. The diurnal profile portrays higher wind speeds in Naivasha than Juja site for the three months. Since the wind flow patterns are modified by the earth's terrain, bodies of water and vegetative cover which determine the degree of roughness, [5, 13] higher wind speeds in Naivasha can be attributed to the effect of the lake Naivasha and channelling effect of the Rift valley and the hills.

## WindRose Diagrams

WindRose diagrams were used to analyse wind direction as shown by figure 3. Most Juja wind was between east north east (ENE) and east south east (ESE) while that of Naivasha was between south east (SE) and south west (SW).

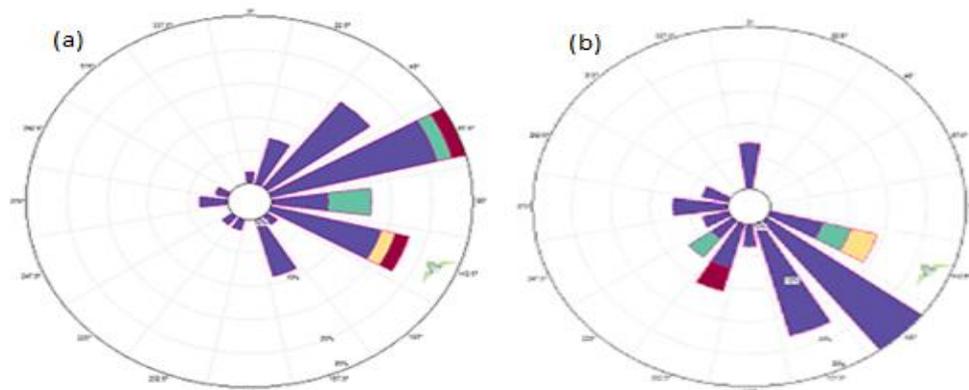


Figure 3: Overall WindRose (a) WindRose for Juja (b) WindRose for Naivasha

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The windRose diagrams in figure 3 are almost unidirectional. This implies that horizontal axis turbines are appropriate for power generation in the two sites. This can minimize cost due to absence of a yaw.

### Weibull Parameters, Probability Density Functions and Power Densities

The wind speeds were used to determine Weibull shape parameters (k), scale parameters (c), (table 1), and wind power densities, (table 2) for different methods. Windographer software and Microsoft Excel were used to determine and generate the parameters and Probability Distribution Functions (PDFs).

**Table 1: Weibull parameters for different methods**

Method	At a height of 10 m(Juja site)		At a height of 30 m (Juja site)		Naivasha (St. Xavier)	
	c (m/s)	k	c (m/s)	k	c (m/s)	k
Weibull-fit	2.811	2.937	3.646	3.394	4.209	2.390
Regression	2.937	2.773	2.937	2.773	2.718	1.810
MLH	2.394	1.261	2.652	0.943	2.635	0.943

Actual power densities for 10 m and 30 m in Juja and 10 m, in Naivasha were 14.5 W/m<sup>2</sup>, 30.9 W/m<sup>2</sup> and 58.5 W/m<sup>2</sup> respectively. The mean wind power densities for Juja (10 m and 30 m) and Naivasha (10 m) were 12.68 W/m<sup>2</sup>, 20.65 W/m<sup>2</sup> and 39.95 W/m<sup>2</sup> by Weibull model and 14.51 W/m<sup>2</sup>, 22.43 W/m<sup>2</sup> and 28.63 W/m<sup>2</sup> by Rayleigh model respectively. Error analysis was done using equation 18.

$$Error(\%) = \frac{P_{(W,R)} - P_{(M,R)}}{P_{(M,R)}} \dots\dots\dots 18$$

Where  $P_{(W,R)}$  in (W/m<sup>2</sup>) is the mean power density calculated from either the Weibull or Rayleigh function used in the calculation of the error and  $P_{(M,R)}$  is the wind power density for probability density distribution derived from field data values which serve as the reference mean power density.

**Table 2: Wind power densities**

Month	Wind Power Density (W/m <sup>2</sup> )											
	At 10 m(Juja site)				At 30 m(Juja Site)				At 10 m(Naivasha site)			
	W	E <sub>w</sub>	R	E <sub>R</sub>	W	E <sub>w</sub>	R	E <sub>R</sub>	W	E <sub>w</sub>	R	E <sub>R</sub>
Weibull-fit	13.81	-0.05	16.88	0.16	22.44	-0.27	36.85	0.19	36.54	-0.38	56.70	0.03
Regression	13.73	-0.06	16.21	0.08	18.81	-0.39	19.26	-0.38	18.42	-0.69	15.27	-0.74
MLH	10.50	-0.28	10.43	-0.28	20.70	-0.33	14.18	-0.54	64.90	0.10	13.91	-0.76

Percentage errors ranged from -38 to 19 %, -74% to 8% and -76% to 10% by Weibull-fit, Regression and MLH respectively as shown in table 2. Weibull-fit has the minimum deviation from actual power densities for the two sites during the study period. The Weibull parameters were dependent on method of analysis.

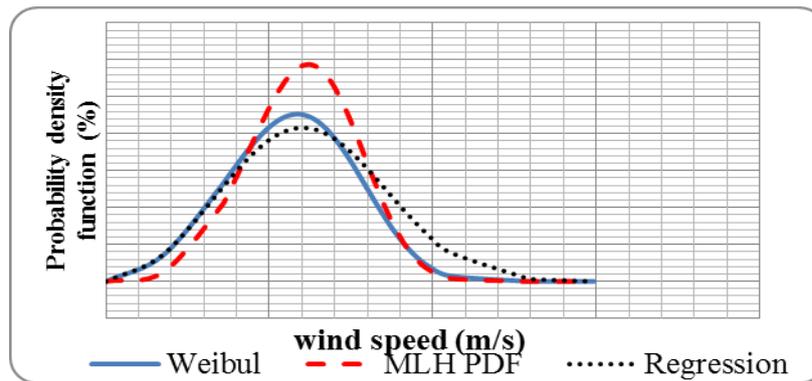
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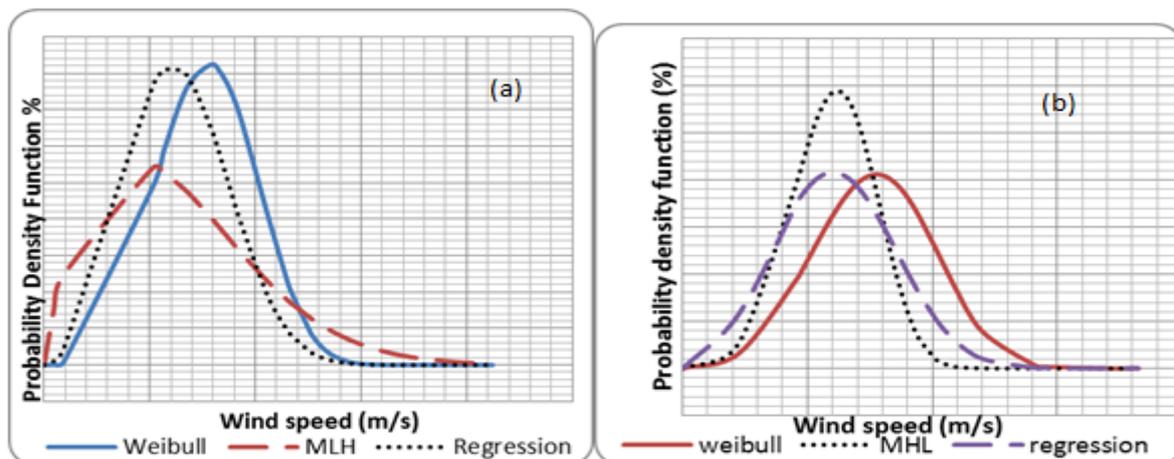
### Probability Distribution Functions (PDFs)

The Probability Distribution Functions generated from Weibull parameters obtained from different methods are as per figures 4 and 5 (a) and (b). The area under each PDF curve represents power density.



**Figure 4:** Probability Distribution Functions (PDF) s, 10 m, Juja

The curves portray that different methods of analysis yielded different values of power densities for the same site. This can be attributed to conditions under which each method was established.



**Figure 5:** Probability Distribution Functions (PDF) s, (a) 10 m, Naivasha (b) 30 m, Juja

The results on power density showed Weibull-fit being the method of best fit for Juja and Maximum Likelihood for Naivasha by Weibull distribution model while Regression fits Juja best and Weibull-fit, Naivasha, by Rayleigh model. This implies that power density, for any selected site, should be obtained using different methods in order determine the actual state of wind in the site.

### V. CONCLUSION

The sites had low wind speed averages ranging from 0.3 m/s to 3.54 m/s which resulted to low power density of wind class 1. The Weibull scale parameters  $c$  and shape parameters  $k$  ranged from 2.394 m/s to 4.209 m/s and 0.943 to 2.937

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respectively. The mean wind power densities for Juja (10 m and 30 m) and Naivasha (10 m) were 12.68 W/m<sup>2</sup>, 20.65 W/m<sup>2</sup> and 39.95 W/m<sup>2</sup> by Weibull model and 14.51 W/m<sup>2</sup>, 22.43 W/m<sup>2</sup> and 28.63 W/m<sup>2</sup> by Rayleigh model respectively. The results indicated that different methods of analysis yield different values of power density and that method of best fit is dependent on locality/ altitude as per Paitoon, 2010s' [15] findings. From the windRose analysis, most winds for Juja site were found to be in the North East and East South East directions while those for Naivasha were between South East and south west directions. The two sites were found capable of power generation by use of small horizontal axis wind turbines such as ModernVestas turbines with cut-in speed of 2.5 m/s. The generated power can be used for activities such as battery charging and water pumping.

## ACKNOWLEDGEMENTS

I acknowledge BRIGHT PROJECT, Phy.Dept (JKUAT), Prof. Nyende, Saoko C., Samuel M. and Ngei Katumo.

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