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# Analysis of n<sup>th</sup> Power Law MOSFET Model

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**ABSTRACT:-** In this paper, a simple general yet realistic MOSFET model named n<sup>th</sup> power law MOSFET model for I-V characteristic of MOSFET in linear and saturation region is proposed. Model can express I-V characteristics of short channel MOSFET'S at least down to 0.12-µm channel length and resistance inserted MOSFET. The model evaluation time is about 1/3 of the evaluation time of the SPICE MOS LEVEL-1model. The model parameter extraction is done by solving single variable equations .solution can be done within a second, being different from the fitting procedure with expensive numerical iterations employed for the conventional models. Model plays a role of a bridge between a complicated MOSFET current characteristics and circuit behaviour in the deep sub -micrometer region.

**KEY WORDS:** MOSFET, Parameter Extraction, Sub-Micrometer.

#### **I.INTRODUCTION**

Analytical *I-V* models are necessary for the design of integrated circuits. The analytical treatment of MOSFET circuit is primarily done by Shockley model but this model, is not so much accurate, because it shows negligible effect for velocity saturation carriers and short channel effect. There have been many attempts to accurately model the characteristics of these transistors, including complicated empirical models used for SPICE simulations. After that analytic treatment of MOSFET is done by various precise MOS model like, spice level3 model, BSIM, etc. But, some of these takes more time in evaluating model, some needs a special system with a hardware/software combination to extracting model parameters. Some of these need expensive numerical iteration procedure to extract model parameters and extracted model parameters are not able to give satisfactory results. However, to fill the gap between the Shockley and more precise model a new model, named as *n*th-power model, preserving high accuracy is introduced for circuit analysis. The *n*th-power model (Sakurai and Newton, 1990; Sakurai and Newton, 1991), which assumes a non-integer *n*th-power relation between current and voltage, is the best model to extract parameters. The *n*th-power law MOSFET model but much more accurate in linear and saturation region.

Model parameter extraction is done by solving single variable equations and can be done with in second. An analytical treatment of circuit operation can be carried out by using this model, which helps to understand circuit behaviour in sub micrometer region. Here this model is not compared with the other precise model, but it is placed just above the Shockley model.

The model is presented in Section II and the model parameter extraction procedure is described in Section III. Section IV is dedicated to the results when the model is implemented in spice and followed by conclusion in Section V.

#### **II. MODEL DESCRIPTION**

The proposed model equations are as follows. I<sub>D</sub> is the drain current

$V_{TH} = V_{T0} + \gamma (\sqrt{2\phi_F} - V_{BS} - \sqrt{2\phi_F})$	(1)
$V_{DSAT} = K (V_{GS} - V_{TH})^m$	(2)
$I_{DSAT} = (W/L_{EFF}) \cdot B \cdot (V_{GS} - V_{TH})^n$	(3)
$I_D = I_{D5} = I_{DSAT} \cdot (1 + \lambda v_{DS})$ ; Where $\lambda = \lambda_0 - \lambda_1 \cdot v_{BS}$	(4)

 $\{V_{DS} \ge V_{D SAT}: \text{ saturated region}\}$ 

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$$I_D = I_{D3} = I_{D5} (2 - V_{DS}/V_{DSAT}) V_{DS}/V_{DSAT}$$

(5)

 $\{V_{DS} < V_{D SAT}: Linear region\}$ 

Where  $V_{GS}$ ,  $V_{DS}$  and  $V_{BS}$  are gate-source, drain-source, and bulk-source voltages, respectively. W is a channel width and  $L_{EFF}$  is an effective channel length.  $V_{TH}$  denotes a threshold voltage,  $V_{DSAT}$  a drain saturation voltage, and  $I_{DSAT}$ , drain saturation current.  $V_{T0}$ ,  $\gamma$ , and  $2\varphi_F$  are parameters which describe the threshold voltage. Parameters K and m control the linear region characteristics while B and n determine the saturated region characteristics.  $\lambda_0$  and  $\lambda_1$  are related to the finite drain conductance in the saturated region. The subscript 3 and 5 for  $I_D$  denotes a triode and a pentode operating region, respectively, and they are totally different from  $I_{D,3}$  and  $I_{D,5}$ .

#### **III.EXTRACTION PROCEDURE**

Select points 1 to 7 in I-V characteristics suitably as shown in below figure 1 from[1], then we have  $I_{D,1}$ -  $I_{D,7}$ ,  $V_{DS,1}$ -  $V_{DS,7}$  and  $V_{GS,1}$ -  $V_{GS,7}$ .



Fig 1.Selected point for model parameters extraction Now, we can find the parameters value by the formulas as given below:-

$$\lambda_{0} = (I_{D,2} - I_{D,1}) / (I_{D,1}V_{DS,3} - I_{D,2}V_{DS,2})$$

$$I_{Z3} = I_{D,3} / (1 + \lambda_{0}V_{DS,3}) \quad I_{Z4} = I_{D,4} / (1 + \lambda_{0}V_{DS,4}) \qquad I_{Z4} = I_{D,5} / (1 + \lambda_{0}V_{DS,5})$$
(6)
(7)

Then,  $V_{T0}$  can be obtained by solving the following equation. The bisection method is the best choice for the solution since it finds out the root without fail within ten iterations.

 $f_{v}(V_{T0}) = \log(I_{z3} / I_{z4})\log\{(V_{GS, 4} - V_{T0}) / (V_{GS, 5} - V_{T0})\} - \log(I_{z4} / I_{z5})\log\{(V_{GS, 3} - V_{T0}) / (V_{GS, 4} - V_{T0})\}$ =0 (8)  $n = \log(I_{z3} / I_{z4}) / \log \{(VGS, 3 - V_{T0}) / (VGS, 4 - V_{T0})\}$ (9)  $B=I_{z3}/(V_{GS,3}-V_{T0})^{r}$ (10) $E_6 = I_{D6} / B (VGS, 6 - V_{T0})^n (1 + \lambda_0 V_{DS, 6})$  $E_7 = I_{D7}/B(VGS, 7-V_{T0})^n(1+\lambda_0 V_{DS, 7})$ (11) $V_{DSAT, 6} = V_{DS, 6} (1 + \text{sqrt} (1 - E_6)) / E_6$  $V_{DSAT.6} = V_{DS.7}(1 + sqrt(1 - E_7))/E_7$ (12) $m = \log(V_{DS,6}/V_{DS,7}) / \log \{(V_{GS,6}-V_{T0})/(V_{GS,7}-V_{T0})\}$ (13) $K = V_{DSAT,6} / (V_{GS,6} - V_{T0})^m$ (14) $\lambda_1$  can be calculated by from the following equation  $\lambda_0 - \lambda_1 V_{BS,10} = (I_{D,11} - I_{D,10})/(I_{D,11} V_{DS,11} - I_{D,10} V_{DS,10})$ (15) $I_{D,8}/(1+\lambda_0 V_{DS,8}-\lambda_1 V_{DS,8} V_{BS,8}) = K (V_{GS,8}-V_{TH,8})^n$  $(V_{GS 9} - V_{TH 9})^n$  $(1 + \lambda_0 V_{DS 9} -$ Κ  $\lambda_1 V_{DS9}$  $V_{BS9}$ o/ = I<sub>D.</sub> (16)

After obtaining  $V_{TH, 8}$ , and  $V_{TH, 9}$  by solving the above equations which is just a manipulation of the expressions,  $2\phi_F$  is obtained by solving the following equation with the bisection method:-



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 $f_{p}(2\phi_{F}) = (\sqrt{2\phi_{F} - V_{BS,8}} - \sqrt{2\phi_{F}})(V_{TH,9} - V_{T0}) - (\sqrt{2\phi_{F} - V_{BS,9}} - \sqrt{2\phi_{F}})(V_{TH,8} - V_{T0})$ 

## IV. APPLICATION OF MODEL FOR A MOSFET

Now, we test this model by applying it to our calculated data for a MOSFET. But, we have limitation of sweeping only to voltages, so we cannot use different  $V_{BS}$  values, i.e. we cannot calculate  $\lambda_1$ ,  $\gamma$ , and  $2\varphi$ . Circuit diagram:-

In fig.1 a circuit diagram has been shown for output characteristics of MOSFET. Using LT- SPICE, a SPICE level 1 model has been used for output characteristics and voltage parameter is used as shown in diagram.



Fig.1 Circuit diagram of MOSFET using spice level 1 model parameters.



EXPERIMENTAL Ids Vs Vds:-

 $Fig.2 I_{DS} V_S V_{DS}$  characteristic.

In fig.2 we are sweeping  $V_{gs}$  from 0-5v and V<sub>ds</sub> from 0-5v and I-V characteristics are shown in fig. For different values of Vgs(1,2,3,4,5v).

Parameters are extracted Choosing appropriate values on the above I-V and calculated values are mentioned below:-



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 $\begin{array}{ll} \lambda_0 &= .04 \\ V_{T0} {=} .04 \\ n &= 1.98 \\ B &= .0664 \\ m &= 0.432 \\ K &= 1.46 \end{array}$ 

Using these parameters the graph has been modelled as shown in fig.3.

I-V characteristics of MOSFET using this model



Fig.3 Modelled  $I_{DS} V_S V_{DS}$  characteristic.

## **V.COMPARISON**



Fig.4 comparison of  $I_{DS} V_S V_{DS}$  characteristics for experimental and modelled plot.



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## **VI. CONCLUSION**

The proposed paper shows the implementation of nth power low MOSFET Model. It takes very less time for calculating the parameters because of the simplicity of model with linear equations. It is well suited for analytical treatment of circuit behaviour. This model is not to competing with the existing more precise models but can be used to provide a simple model which is placed just above the Shockley model. Using  $3^{rd}$  generation model we can achieve better results as comparison to  $1^{st}$  and  $2^{nd}$  generation models.

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