

International Journal of Advanced Research in Electrical, Electronics and Instrumentation Engineering

(An ISO 3297: 2007 Certified Organization)

Vol. 3, Issue7, July 2014

DOI: 10.15662/ijareeie.2014.0307002

Natural Space Vector Modulation in Six-Step Voltage Source Inverters

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ABSTRACT: This paper presents the existence of natural space vector modulation occurring between adjacent switching space vectors in quasi-square wave voltage source inverters. This natural space vector modulation is responsible for the hexagonal trajectory of the rotating resultant voltage space vector which is produced by the referral of the instantaneous line or phase voltage quantities to the drive's virtual magnetic axes. Space vector rotation, which gives rise to the hexagonal trajectory only occur between switching states when the instantaneous line or phase voltages are undergoing changes in magnitude. The theoretical approach undertaken to develop the concept of natural space vector modulation is also supported with experimental results and fully support the well-known theory of space vector modulation.

KEYWORDS: Natural, Space Vector Modulation, Voltage Source Inverter.

I.INTRODUCTION

Voltage source inverters (VSI) have been widely used in the production of three-phase non-sinusoidal quasi-square wave voltages and vector analysis has also been applied to the analysis of these inverters [1, 2]. The production of sinusoidal waveforms from these inverters has been accomplished with the familiar space vector modulation approach [3 – 5] which was applied to a three-phase unity power factor ac to dc converter by Busse and Holtz [6]. The space vector modulation (SVM) technique modulates the adjacent stationary switching space vectors of a quasi-square wave drive to produce a variable voltage and variable frequency sinusoidal output, with the rotating resultant voltage space vector displaying a circular trajectory. However, the trajectory of the resultant voltage space vector produced by a quasi-square inverter has been reported to be hexagonal in nature [2, 7] with little emphasis being placed onits origin. In addition, the choice of using line or phase quantities in the production of the resultant switching space vectors of a quasi-square wave drive and the magnetic axes with which they are referred, have not been elaborated on in the literature.

This paper examines the line and phase voltages and their corresponding switching space vectors produced by a quasi-square wave voltage source inverter. Virtual line and phase voltage magnetic axes are introduced and the relationship between line and phase voltage switching space vectors is presented. The process of natural modulation of adjacent switching space vectors of a quasi-square wave drive and the conditions for this natural modulation to occur is developed and supported with experimental results.

II. RELATED WORK

The foundation of vector representation of three-phase systems was laid by Park [8] and Kron [9], and the application of the vector method to the analysis of electrical machines was presented by Kovacs and Racz [10]. They developed transient mathematical models of electrical machines and displayed the physical phenomenon occurring in these machines. The vector method is now widely used in the analysis of voltage source space vector modulated inverters.

III. INVERTER SWITCHING STATES

A three-phase voltage source inverter with the capability of producing variable output voltage and frequency is shown in the digital signal processor (DSP) controlled dc-to-ac converter of Figure 1.



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The inverter consists of six transistors Q_1 to Q_6 , accompanied with their respective anti-parallel diodes D_1 to D_6 . Each inverter leg feeds the star connected balanced load from the collector-emitter connections labeled A, B and C. The inverter is fed with a supply voltage V_{dc} from the filter capacitor and a DSP is utilized to control the switching of the transistors. The operating constraints of this inverter must ensure that two transistors in an inverter leg are not turned on at the same time and the output current of the inverter must always be continuous. These constraints yield eight possible operating states of the inverter. Six of these states produce a non-zero output voltage and are called non-zero switching states, while the other two produce zero output voltage and are known as zero states [2, 7, 5, 11, 12]. The eight switching states are shown in Figure 2(a).

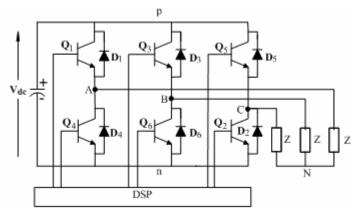


Figure 1 Three-phase Voltage Source Inverter

The switching sequence shown in (i) to (vi) of Figure 2(a), has been used to produce a three-phase output voltage from the inverter. The switching sequence begins with the upper switch of leg A and the lower switches of legs B and C turned on. Since the upper switches are connected to p, the positive of the filter capacitor and the lower switches to n, the negative of the filter capacitor, this state is designated as pnn. Each subsequent state is produced by switching the pair of transistors in one leg of the inverter.

The sequence from states (i) to (vi) and back to (i) of Figure 2(a) is produced by switching transistors in legs B, A, C, B, A and C. Since there are six active switching states in a cycle, then each switching state spans for T/6 seconds, where T is the period of the output line voltage waveform.

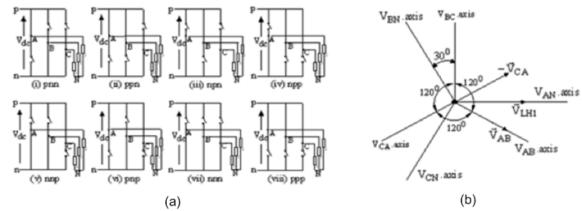


Figure 2. (a) Eight Switching States of the Voltage Source Inverter (b) Line and Phase Voltage VirtualMagnetic Axes and ResultantLine SSVs for State pnn.

IV. LINE VOLTAGE SWITCHING SPACE VECTORS

A system of three-phase line voltages is produced by the inverter, when the switching states are executed in the sequence from Figures. 2(a)(i) to 2(a)(vi) to form a cycle of operation. The line voltages produced are represented by



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 V_{AB} , V_{BC} , and V_{CA} , each being 120° out of phase with the other in the given sequence. The line voltages produced by the switching state in Figure 2(a)(i) are given by:

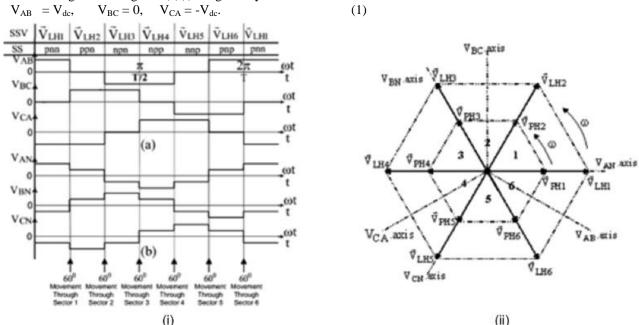


Figure 4 (i) Inverter Output Voltage Waveforms. (a) Quasi-Square Wave Line Voltage Waveforms(b) Six-Step Phase Voltage Waveforms. Figure 4(ii). Line and Phase Switching Space Vectors and Virtual Magnetic Axes

As stated by Kovacs [13], the resultant line voltage vector of a three-phase system of voltages fed to a three-phase stator of a motor is given by:

$$\vec{V}_{L} = \frac{2}{3} (\vec{V}_{AB} + \vec{V}_{BC} + \vec{V}_{CA})$$
 (2)

Similarly, the resultant line voltage vector of a three-phase system of voltages delivered by the three-phase stator of a generator is also given by Eq. (2). The resolution of \vec{V}_L , along the line voltage magnetic axes, produces the instantaneous line voltages of the three-phase system. Taking Eq. 2 to represent the resultant line voltage vector produced by the three-phase voltage source inverter of Figure 1, and representing the vectors in Eq. (2) by their instantaneous values and the spatial position of the line voltage virtual magnetic axes results in

$$\vec{V}_{L} = \frac{2}{3} \left(V_{AB} e^{-j30} + V_{BC} e^{j90} + V_{CA} e^{j210} \right)$$
 (3)

where V_{AB} , V_{BC} , and V_{CA} , are the instantaneous line voltage magnitudes and exp(-j30), exp(j90) and exp(j210) are the respective spatial position of the line voltage virtual magnetic axes of the three-phase system produced by the voltage source inverter. Substituting the instantaneous voltages of Eq. (1) in Eq. (3) yields:

$$\vec{V}_{LH1} = \frac{2}{\sqrt{3}} V_{dc} \tag{4}$$

The line and phase voltages virtual magnetic axes of the three-phase system of voltages, produced by the three-phase inverter of Figure 1, line voltage vectors, and their resultant for switching state pnn are shown in Figure 2(b).

It must be noted that the three-phase voltage source inverter of Figure 1 has no magnetic axes as in the case of a three-phase generator. However, since both systems produce three-phase voltages, the voltage source inverter of Figure 1 can be considered to possess virtual phase and line voltage magnetic axes, similar to those of a three-phase generator. Since



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the instantaneous phase and line voltages are located along the magnetic axes of a three-phase stator [13, 14], then, the instantaneous phase and line voltages of the voltage source inverter of Figure 1 will lie along its virtual magnetic axes as shown in Figure 2(b). The application of the above procedure to the other five non-zero and the two zero switching states in Figure 2(b), produces the line voltage switching space vectors, \vec{V}_{LHK} as shown in Table 1, where k=1,2....6. The three-phase inverter line voltage waveforms and the resulting line voltage switching space vectors obtained from Table 1 are shown in Figures4(i) and Figure 4(ii) respectively.

Table 1 VSI Switching States, Line Voltages, Phase Voltages, Line SSVs, and Phase SSVs

SS	V_{AB}	V_{BC}	V_{CA}	SSVs	Vector	V _{AN}	$V_{\rm BN}$	V _{CN}	SSVs	Vector
nnn	0	0	0	0	\vec{V}_0	0	0	0	0	\vec{V}_0
pnn	V_{dc}	0	-V _{dc}	$\frac{2}{\sqrt{3}}V_{dc}$	$ec{V}_{ ext{LH1}}$	$\frac{2}{3}V_{dc}$	$-\frac{1}{3}V_{dc}$	$-\frac{1}{3}V_{dc}$	$\frac{2}{3}V_{dc}$	$ec{V}_{ ext{PH1}}$
ppn	0	V_{dc}	-V _{dc}	$\frac{2}{\sqrt{3}}V_{dc}e^{j60}$	$\vec{V}_{ ext{LH2}}$	$\frac{1}{3}V_{dc}$	$\frac{1}{3}V_{dc}$	$-\frac{2}{3}V_{dc}$	$\frac{2}{3}V_{dc}e^{j60}$	$ec{V}_{ ext{PH2}}$
npn	-V _{dc}	V_{dc}	0	$\frac{2}{\sqrt{3}}V_{dc}e^{j120}$	$\vec{V}_{ ext{LH3}}$	$-\frac{1}{3}V_{dc}$	$\frac{2}{3}V_{dc}$	$-\frac{1}{3}V_{dc}$	$\frac{2}{3}V_{dc}e^{j120}$	$ec{V}_{ ext{PH3}}$
npp	-V _{dc}	0	V_{dc}	$\frac{2}{\sqrt{3}}V_{dc}e^{j180}$	$ec{V}_{ ext{LH4}}$	$-\frac{2}{3}V_{dc}$	$\frac{1}{3}V_{dc}$	$\frac{1}{3}V_{dc}$	$\frac{2}{3}V_{dc}e^{j180}$	$ec{V}_{ ext{PH4}}$
nnp	0	-V _{dc}	V_{dc}	$\frac{2}{\sqrt{3}}V_{dc}e^{-j120}$	$ec{V}_{ ext{LH5}}$	$-\frac{1}{3}V_{dc}$	$-\frac{1}{3}V_{dc}$	$\frac{2}{3}V_{dc}$	$\frac{2}{3}V_{dc}e^{-j120}$	$ec{V}_{ ext{PH5}}$
pnp	V_{dc}	-V _{dc}	0	$\frac{2}{\sqrt{3}}V_{dc}e^{-j60}$	$ec{V}_{ ext{LH6}}$	$\frac{1}{3}V_{dc}$	$-\frac{2}{3}V_{dc}$	$\frac{1}{3}V_{dc}$	$\frac{2}{3}V_{dc}e^{-j60}$	$ec{V}_{ ext{PH6}}$
ppp	0	0	0	0	\vec{V}_8	0	0	0	0	\vec{V}_8

The line voltage switching space vectors produced by the three-phase quasi-square waves of Figure 4(i)(a), are all of constant magnitude $(2/\sqrt{3})V_{dc}$ and each exist for a time equal to about T/6 seconds, where T is the period of the waveforms. The six non-zero resultant line voltage space vectors are represented by the general expression:

$$\vec{V}_{LHk} = \frac{2}{\sqrt{3}} V_{dc} e^{j\frac{(k-1)\pi}{3}}$$
 for $k = 1, 2, ... 6$ (5)

V.ROTATION OF LINE VOLTAGE SPACE VECTORS

The line voltage switching space vectors \vec{V}_{LHK} shown in Figure 4(ii) are stationary space vectors, each occupying a fixed position in space. Figure 4(i)(a) shows that each switching space vector is active for about T/6 seconds and they are produced in the sequence \vec{V}_{LH1} , \vec{V}_{LH2} through \vec{V}_{LH6} . The fall of V_{AB} from V_{dc} to zero and the rise of V_{BC} from zero to V_{dc} , results in the decay of switching space vector \vec{V}_{LH1} and the growth of switching space vector \vec{V}_{LH2} . Assuming that the rate of fall of V_{AB} is equal to the rate of rise of V_{BC} , the natural rotation of the resultant voltage space vector within sector 1 can be examined. Since the production of switching space vector \vec{V}_{LH2} follows that of \vec{V}_{LH1} and is accomplished by the switching of the two transistors in leg \vec{B} of the inverter, only waveforms V_{AB} and V_{BC} will be examined in the interval of concern, because waveform V_{CA} is unaffected by the leg \vec{B} switching. Figure 6(a) examines the V_{AB} and V_{BC} waveforms for the above interval.



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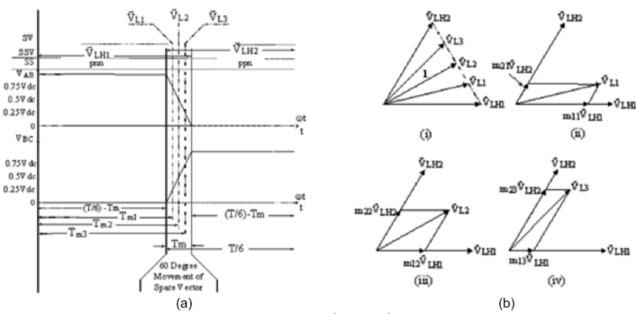


Figure 6(a). V_{AB} and V_{BC} Waveforms for Production of \vec{V}_{LH1} and \vec{V}_{LH2} During Linear Fall of V_{AB} and Rise of V_{BC} Figure 6(b). Switching and Rotating Space Vectors (i) SSVs and Three Rotating Space Vectors During T_{min} Sector 1 (ii) Components of \vec{V}_{L1} (iii) Components of \vec{V}_{L2} (iv) Components of \vec{V}_{L3}

For the interval examined in Figure 6(a), line voltage V_{CA} is unchanged and its value is $-V_{dc}$. Three values of line voltages V_{AB} and V_{BC} have been recorded in the time interval T_m of Figure 6(a), when these voltages are changing from their old to new values. For times indicated by T_{m1} , T_{m2} and T_{m3} , all taken in T_m , the corresponding line voltages are:

$$\begin{split} & \text{Time} = T_{m1,} \quad V_{AB} = 0.75 V_{dc} \quad V_{BC} = 0.25 V_{dc}, \quad V_{CA} = -V_{dc} \\ & \quad \text{Time} = T_{m2,} \quad V_{AB} = 0.5 V_{dc} \quad V_{BC} = 0.5 V_{dc}, \quad V_{CA} = -V_{dc} \\ & \quad \text{Time} = T_{m3,} \quad V_{AB} = 0.25 V_{dc} \quad V_{BC} = 0.75 V_{dc}, \quad V_{CA} = -V_{dc} \end{split} \tag{6}$$

The resultant line voltage vectors at times T_{m1} , T_{m2} and T_{m3} are obtained by substituting Eqs. (6), (7) and (8) into Eq. (3) and are given by:

$$\vec{V}_{L1} = 1.0408 V_{dc} e^{j13.9}$$
 (9)

$$\vec{V}_{L2} = 1.0 V_{dc} e^{i30} \tag{10}$$

$$\vec{V}_{L3} = 1.0408 V_{dc} e^{j46.1} \tag{11}$$

The two adjacent switching space vectors in this transitional time T_m are \overline{V}_{LH1} and \overline{V}_{LH2} , where:

$$\vec{V}_{LH1} = 1.1547 V_{dc} e^{j0}$$

$$\vec{V}_{LH2} = 1.1547 V_{dc} e^{j60}$$
(12)

The five space vectors in Eqs. (9), (10), (11), (12), and (13) when plotted in the complex plane is shown in Figure 6(b)(i). The three space vectors are \vec{V}_{L1} , \vec{V}_{L2} and \vec{V}_{L3} in Figure 6(b)(i) can be resolved along the switching space

vectors are \vec{V}_{LH1} and \vec{V}_{LH2} as shown in Figures 6(b)(ii) to 6(b)(iv) respectively.

The two switching space vectors are \vec{V}_{LH1} and \vec{V}_{LH2} are active during this time interval T_m , when V_{AB} is falling linearly and V_{BC} is rising linearly as shown in Figure 6(a). Hence, the resultant voltage space vectors \vec{V}_{L1} , \vec{V}_{L2} and \vec{V}_{L3} that are produced in the interval T_m , must comprise of fractions of switching space vectors \vec{V}_{LH1} and \vec{V}_{LH2} . This is reflected in Figures 6(b)(ii) to 6(b)(iv), where the fractions of \vec{V}_{LH1} and \vec{V}_{LH2} used in the production of resultant voltage space vectors \vec{V}_{L1} are indicated by $_{m1i}\vec{V}_{LH1}$ and $_{m2i}\vec{V}_{LH2}$ respectively, where i = 1...3. Hence, the switching space vectors \vec{V}_{LH1} and \vec{V}_{LH2} are modulated naturally during the interval T_m to produce a resultant voltage space vector that rotates through the angle $\omega t = 60^0$ formed by sector 1. It must be noted that during the time intervals $T/6 - T_m$ that accounts for almost 60^0 along the line voltage waveforms, the line voltages are of constant magnitude V_{dc} , and the switching space vectors produced



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are fixed in space for that time. It is only during the short time interval of T_mwhen the line voltage magnitudes are changing, that rotation of the resultant voltage space vector occurs as shown in Figure 6(a). Hence, the 60° movement along the line voltage waveforms is represented by the 60° sectors forming the hexagon of Figure 4(ii), and the time taken by the resultant voltage space vector to traverse this 60° sector is denoted by $T_{\rm m}$. Therefore, space vector rotation only occurs when the voltages from which they are produced are undergoing changes in magnitude. During one cycle of operation, the resultant line voltage space vector \vec{V}_L rotates through 360° and having a trajectory of the line voltage hexagon of Figure 4(ii), when the voltage source inverter of Figure 1 is driving a balanced star-connected unity power factor load.

Figure 7(a) is an oscilloscope picture showing the fall of line voltage V_{AB} and the rise of V_{BC} during T_m , while, Figure 7(b) shows a picture of the trajectory of resultant line voltage space vector $\overline{V}_{\rm L}$.

The theory of space vector modulation as presented in [3-5] performs forced modulation on the adjacent switching space vectors to achieve a circular trajectory of the resultant voltage space vector in the production of sinusoidal voltages from quasi-square wave line voltage waveforms. However, the production of a hexagonal trajectory produced by the resultant voltage vector of a quasi-square wave inverter, reveals that adjacent stationary switching space vectors were modulated naturally due the fall and rise of line voltages, thereby producing a rotating resultant voltage vector whose trajectory is a hexagon.

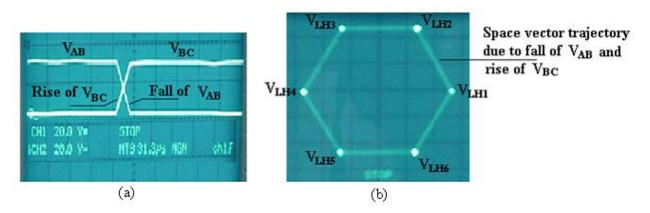


Figure 7. Space Vector Rotation Due to Natural Modulation of SSVs. (a) Fall and Rise of Line Voltage Waveforms V_{AB}and V_{BC}Respectively (b) Trajectory of Line Voltage SSVs by Natural Modulation of Adjacent SSVs

VI.PHASE VOLTAGE SPACE VECTOR

The load phase voltages V_{AN} , V_{BN} and V_{CN} , for the eight switching states in Figure 2(a) are obtained using the three line voltages produced for each state. These phase voltages are recorded in Table 1 and their waveforms are plotted in Figure 4(i)(b). Examination of the phase and line voltage waveforms in Figure 4(i) reveals that the phase voltage lags the line voltage by 30°, thus resulting in the 30° phase shift between the line and phase voltage virtual magnetic axes of Figure 2(b). In addition, the phase voltage waveforms of Figure 4(i)(b) are six-step voltage waveforms, since there are six voltage steps in a cycle. Employing [13], the resultant phase voltage vector of a three-phase system is given by,

$$\vec{V}_{P} = 2/3(\vec{V}_{AN} + \vec{V}_{BN} + \vec{V}_{CN}). \tag{14}$$

Representing the vectors in Eq. (14) by their instantaneous values and the spatial position of the phase voltage virtual
$$\begin{split} &\text{magnetic axes yields,} \\ &\vec{V}_P = 2/3 (V_{AN} + V_{BN} \, e^{j120} \, + V_{CN} \, e^{j240}). \end{split}$$

$$\vec{V}_{P} = 2/3(V_{AN} + V_{BN}e^{j120} + V_{CN}e^{j240}).$$
 (15)

where V_{AN}, V_{BN} and V_{CN} are the instantaneous phase voltage magnitudes and e^{j120} and e^{j240} are the respective spatial position of the phase voltage virtual magnetic axes. Substituting the instantaneous phase voltages of Table 1 in Eq. (15) yields,



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$$\vec{V}_{PHk} = \frac{2}{3} V_{dc} e^{\frac{j(k-1)\pi}{3}} k = 1, 2, ...6$$
 (16)

for the six non-zero resultant phase voltage switching space vectors. The resultant phase voltage switching space vectors obtained from Figure 2(a) are shown in Figure 4(ii) and presented in Table 1.

From Table 1, it is observed that the line voltage switching space vectors are $\sqrt{3}$ times their phase counterparts, but both line and phase voltage switching space vectors occupy the same position in space, however, their virtual magnetic axes are displaced by 30° from each other. This indicates that either line or phase voltage analysis can be performed and conversion from one to the other is effected by a factor of $\sqrt{3}$. This is reflected in the resultant line and phase voltage switching space vectors of Eqs. (5) and (16).

VII. CONCLUSION

This paper presented the existence of natural space vector modulation, which is responsible for space vector rotation within the sectors of the hexagon produced by the resultant voltage space vector of a quasi-square wave or six-step voltage source inverter drive. The existence of this natural space vector modulation was supported with experimental results. The issue of virtual magnetic axes was also presented as a means of producing the resultant voltage space vector of a voltage source inverter drive. It was shown that the well known space vector modulation technique, utilizing adjacent switching space vectors to synthesize variable voltage and frequency sinusoidal waveforms from a voltage source inverter, obtained its origin from the natural modulation process that occurred in a quasi-square wave or six-step voltage source inverter drive.

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BIOGRAPHY



Ronald De Four received his PhD, MPhil and BSc degrees in Electrical and Computer Engineering from The University of the West Indies, St. Augustine, Trinidad. Presently, he is a Lecturer in the Department of ECE, UWI, Trinidad. His area of interest include power electronics, variable speed drives and solar power systems.



Tariq Wadi was born in Trinidad, in 1979. He received both his BSc degree in 2008 (first class) and his MSc degree in 2012 (with distinction) in Electrical and Computer Engineering from The University of the west indies. His current research interests include Brushless DC motor control, induction motor, and renewable energy.