



# Speed and Stator Resistance Estimation of Four Quadrant Vector Controlled IM Drives

Aswathy Vijay<sup>1</sup>, Binojkumar A.C<sup>2</sup>

Department of Electrical Engineering, Rajiv Gandhi Institute of Technology, Kottayam, India<sup>1,2</sup>

**ABSTRACT:** In this paper, Model Referencing Adaptive Controller (MRAC) based speed and stator resistance estimation of vector controlled induction motor drive is presented. Both MRACs utilize voltages and currents in synchronously rotating reference frame and do not require computation of fluxes. This technique is stable in all four quadrants of operation and also can be used for low speed and zero speed operation. The speed estimation algorithm (i.e., speed estimating MRAS) depends on stator resistance making it sensitive to stator resistance variation. This is compensated by another MRAC making the speed estimation algorithm independent of stator resistance. The proposed method is simulated in MATLAB/SIMULINK and simulation results are obtained.

**KEYWORDS:** Induction Motor, Model Referencing Adaptive Controller (MRAC), Stator resistance estimation, Vector control

List of symbols:

$v$	Stator voltage vector
$i$	Stator current vector
$v_{ds}, v_{qs}$	d and q-axis components of stator voltage
$i_{ds}, i_{qs}$	d and q-axis components of stator current
$\Phi_{dr}, \Phi_{qr}$	d and q-axis components of rotor flux
$\omega_e$	Synchronous speed of the motor
$\omega_{sl}$	Slip speed
$\omega_r$	Rotor speed
$L_s, L_r$	Stator and rotor inductances per phase
$R_s, R_r$	Stator and rotor resistances per phase
$\sigma = 1 - L_m^2 / L_s L_r$	Leakage factor
$L_m$	Magnetizing inductance

## I. INTRODUCTION

The Vector controlled induction motor (IM) drive is widely used in high performance industrial applications since it is simple and provides fast dynamics in terms of the torque response [1] as the independent control of flux and torque can be achieved. The rotor speed can be obtained either by using speed sensors or by estimation. The use of speed sensor [2]-[4] may encounter several problems like mounting, signal transmission, hazardous environment and reliability. The elimination of speed sensor results in reduction of cost and size of the drive, better noise immunity and less maintenance requirements and also increases reliability and robustness of the system. So, the speed estimation is more preferable than the speed sensing in industrial applications. On the other hand, parameter sensitivity, stability in the all four quadrants of operation including low and zero speed operation, and high computational effort can be the main drawbacks of sensor less control.

Various techniques are available for the estimation of speed for IM drive [1], [5]. These are mainly classified as: (i) Rotor flux based, (ii) Frequency signal injection based, (iii) Model Reference Adaptive System (MRAS) based,

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(iv) Observer based, (v) Artificial Intelligence (AI) based and (vi) Rotor slot harmonics based methods. Among all these methods, MRAS is simple, requires less computation time and has good stability [5]-[6].

Different types of model reference adaptive system (MRAS) are flux based [4], [7]-[8] back electromotive force (emf) based [10] and reactive power based [9]-[11]. Flux based MRAC and its improved methods [4], [7], [8] efficiently estimate rotor speed in all the four quadrants of operation but it has integrator related problems at very low speed, including zero speed. Back-emf based MRAS [10] is also inefficient at low speed since at low speeds back-emf is very low. A reactive power based MRAS [9]-[11] using instantaneous reactive power in the reference model and steady-state field-oriented reactive power in the adjustable model has no integrators and hence can be used at very low speed including zero speed. This method is independent of variation of stator resistance. But in the regenerating mode, the reactive power based MRAS is unstable.

Here MRAC called X-MRAC [12], [13], [14] which uses instantaneous value of cross product of  $v$  and  $i$  (i.e.,  $v \times i$ ) in the reference model and steady-state flux oriented value of the same in the adjustable model. This MRAC is stable in all the four quadrants, operates very well at low speed including zero speed, does not require flux computation and is very easy to implement. However, the formulation involves stator resistance which is compensated by another MRAS. This MRAC also requires only voltages and current in synchronously rotating reference frame for  $R_s$  estimation.

In the subsequent sections of this paper, the modeling of MRACs, complete system and simulation results are presented

## II. X MRAC BASED SPEED ESTIMATION

### A. X-MRAC

The structure of the X-MRAC is shown in Fig. 1. The cross product of voltage and current in synchronously rotating reference frame is used in the construction of this X-MRAC. This cross product is denoted by  $X$ , which is neither active power nor reactive power. In reference model, instantaneous value of  $X$  (i.e.,  $X_1$ ) is used whereas in adaptive model steady state value of  $X$  (i.e.,  $X_2$ ) under flux oriented condition is used. The error between the two,  $E = X_1 - X_2$  is fed to a PI controller which yields estimated rotor speed. This estimated speed is fed back to adaptive model so that error converges to zero.

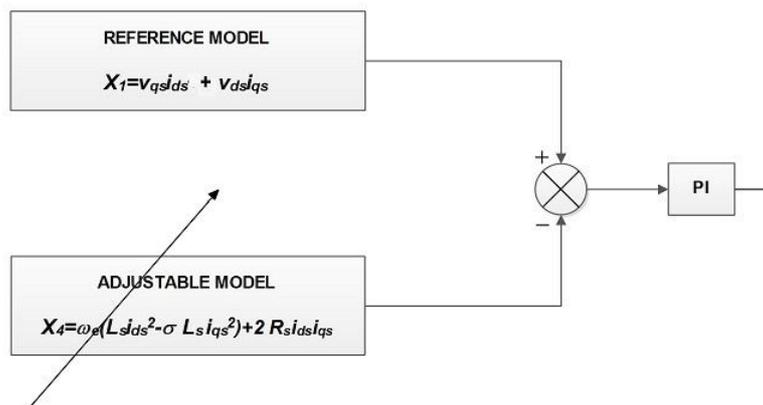


Fig.1. X-MRAC based speed estimation technique

### B. Construction of X-MRAC

The stator voltages of induction motor in the synchronously rotating reference frame can be expressed as follows

$$v_{qs} = R_s i_{qs} + \omega_e \sigma L_s i_{ds} + p \sigma L_s i_{qs} + \frac{L_m}{L_r} (\omega_e \phi_{dr} + p \phi_{qr}) \quad (1)$$

$$v_{ds} = R_s i_{ds} - \omega_e \sigma L_s i_{qs} + p \sigma L_s i_{ds} - \frac{L_m}{L_r} (\omega_e \phi_{qr} - p \phi_{dr}) \quad (2)$$

The instantaneous value of  $X$  (i.e.,  $v \times i$ ) is given by

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$$X_1 = v_{qs}i_{ds} + v_{ds}i_{qs} \quad (3)$$

Substituting eqns (1) and (2) in (3) X (i.e.,X<sub>1</sub>) becomes

$$X_2 = \left[ R_s i_{qs} + \omega_e \sigma L_s i_{ds} + p \sigma L_s i_{qs} + \frac{L_m}{L_r} (\omega_e \varphi_{dr} + p \varphi_{qr}) \right] i_{ds} + \left[ R_s i_{ds} - \omega_e \sigma L_s i_{qs} + p \sigma L_s i_{ds} - \frac{L_m}{L_r} (\omega_e \varphi_{qr} - p \varphi_{dr}) \right] i_{qs} \quad (4)$$

At steady state X (i.e.,X<sub>2</sub>) becomes

$$X_3 = \left[ R_s i_{qs} + \omega_e \sigma L_s i_{ds} + \frac{L_m}{L_r} (\omega_e \varphi_{dr}) \right] i_{ds} + \left[ R_s i_{ds} - \omega_e \sigma L_s i_{qs} - \frac{L_m}{L_r} (\omega_e \varphi_{qr}) \right] i_{qs} \quad (5)$$

For rotor flux orientation, the steady state value of X(i.e,X<sub>3</sub>) becomes

$$X_4 = \omega_e [L_s i_{ds}^2 - \sigma L_s i_{qs}^2] + 2R_s i_{ds} i_{qs} \quad (6)$$

The expression of X<sub>1</sub> is independent of rotorspeed. Hence,it is selected for the reference model. X<sub>2</sub>, X<sub>3</sub> or X<sub>4</sub>can be chosen as the adjustable model since they are dependent on the rotor speed (ω<sub>r</sub>).However, X<sub>4</sub> is selected in the adjustablemodel, as itdoes not require any flux estimation and any derivative operations. But the adjustable model of this MRAS is dependent on stator resistance which may changes during low speed operation. So the stator resistance has to be updated if there is any stator resistance variation.

### III. STATOR RESISTANCE ESTIMATION

The induction motor stator voltages in the synchronously rotating reference frame are given by equations (1) and (2) For a field oriented drive, the simplified expression of voltages atsteady state (i.e., derivative terms, p = 0) becomes:

$$v_{qs} = R_s i_{qs} + \left( \frac{L_m^2}{L_r} + \sigma L_s \right) \omega_e i_{ds} \quad (7)$$

$$v_{ds} = R_s i_{ds} - \omega_e \sigma L_s i_{qs} \quad (8)$$

Eliminating ω<sub>e</sub> from above equations

$$R_s = \frac{v_{ds}i_{ds} + \sigma v_{qs}i_{qs}}{\sigma i_{qs}^2 + i_{ds}^2} \quad (9)$$

The above expression is independent of speed. So stator resistance can be estimated usingvoltages and currents in synchronously rotating reference as shown in Fig.2.



Fig.2.MRAC based stator resistance estimation technique



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TABLE I  
INDUCTION MACHINE RATINGS AND PARAMETERS

Symbol	Meaning	Value
-	Rated Shaft Power	1.3kW
-	Line to Line voltage	400V
-	Rated Speed	1430rpm
P	Pole pair	2
$L_s$	Stator Self Inductance	0.6848H
$L_r$	Rotor Self Inductance	0.6848H
$L_m$	Magnetising Inductance	0.6705H
$R_s$	Stator Resistance	5.71 $\Omega$
$R_r$	Rotor Resistance	4.0859 $\Omega$
J	Machine Inertia	0.011Kg-m <sup>2</sup>

### A. Step Change of Rotor Speed and Zero Speed Operation

The response of the IM for a step change in reference speed and zero-speed operation is shown in Fig.4. The actual speed tracks the reference speed satisfactorily. Fig.4 (a) shows that the estimated speed is very close to the actual rotor speed. Flux orientation is not disturbed, as depicted in Fig.4 (b)

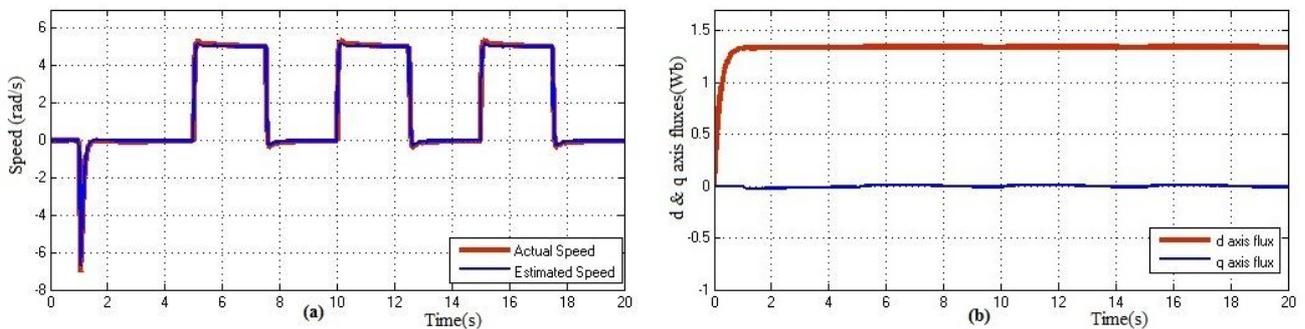


Fig.4 (a) Actual speed and estimated speed [rad/s] versus time[s], (b) d-axis and q-axis flux [Wb] versus time[s]

### B. Ramp Response

The response of the IM to a ramp signal is shown in Fig.5. The estimated speed follows the actual speed as shown in Fig.5 (a) which in turn is matching with the input ramp signal applied. In all these operations, the flux orientation is well maintained and can be seen from Fig.5 (b). The results confirmed stable operation in forward and reverse-motoring modes.

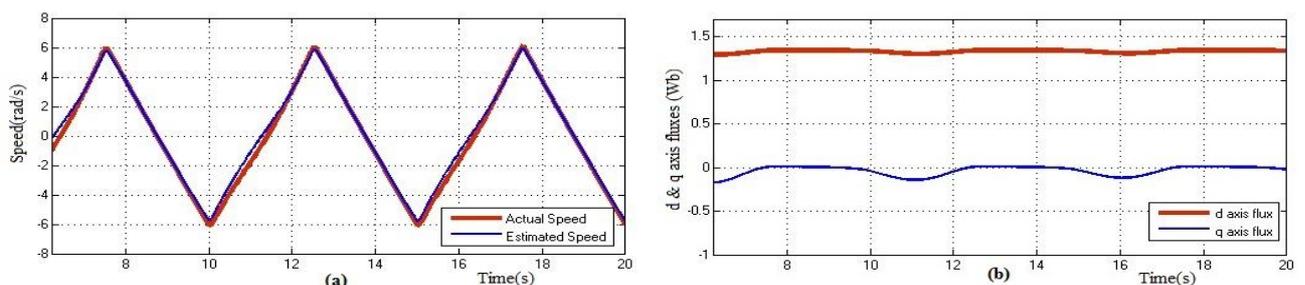


Fig.5. (a) Actual speed and estimated speed [rad/s] versus time[s], (b) d-axis and q-axis flux [Wb] versus time[s]

### C. Low Speed Operation

The performance of the estimator at a low speed of 1rad/s is shown in Fig.6. The estimated speed and the actual speed are shown in Fig.6 (a). The flux orientation is maintained, as shown in Fig.6 (b).

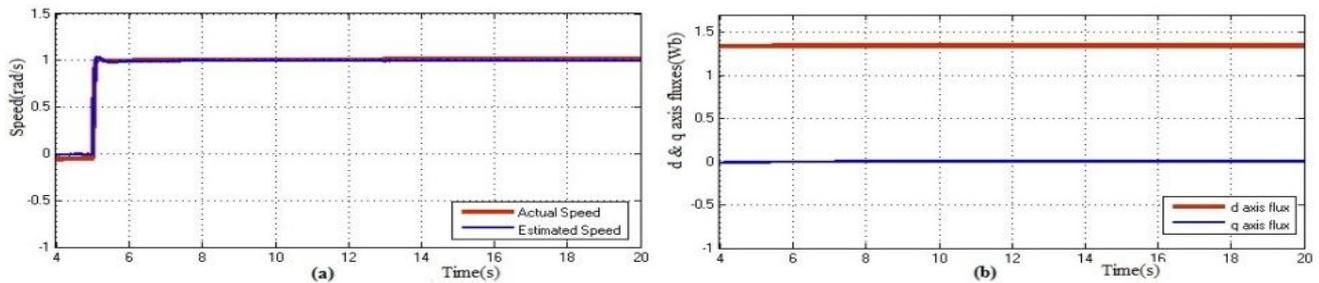


Fig.6. (a) Actual speed and estimated speed [rad/s] versus time[s], (b) d-axis and q-axis flux [Wb] versus time[s]

### D. Regenerative Operation

1) *Second quadrant operation:* The second quadrant operation can be seen from Fig.7. The load torque is kept positive at 5 N-m and reference speed is changed from positive to negative and then back to positive which shows the transition of the estimator from motoring to regenerating mode and back. The estimated speed, actual speed follows the reference speed as seen from Fig.7(a). The flux orientation is kept same from Fig.7(b)

2)

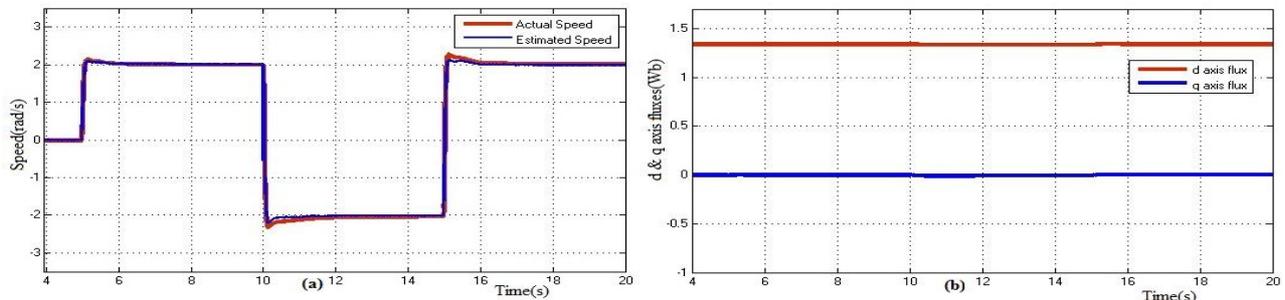


Fig.7. (a) Actual speed and estimated speed [rad/s] versus time[s], (b) d-axis and q-axis flux [Wb] versus time[s]

3) *Fourth quadrant operation:* The fourth quadrant operation can be seen from Fig.8. The load torque is kept at -2 N-m and reference speed is changed from negative to positive and then back to negative which shows the transition of the estimator from motoring mode to regenerating mode and back. The estimated speed, actual speed follows the reference speed as seen from Fig.8 (a). The flux orientation is kept same from Fig.8(b)

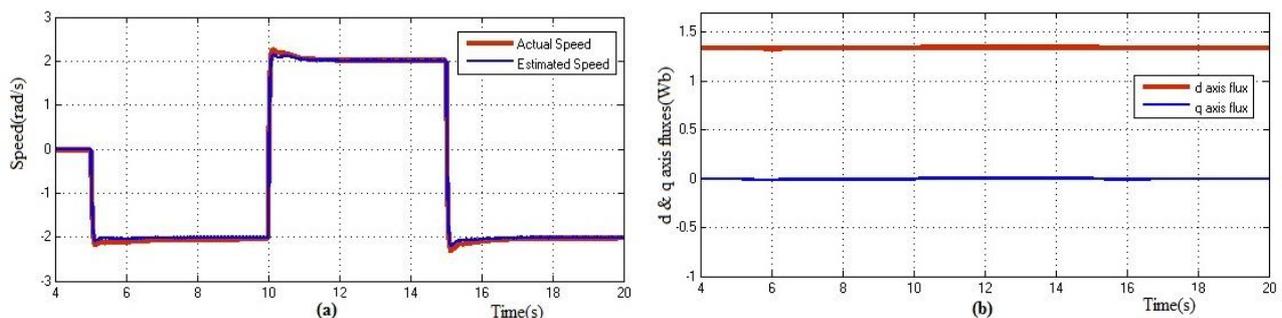


Fig.8. (a) Actual speed and estimated speed [rad/s] versus time[s], (b) d-axis and q-axis flux [Wb] versus time[s]

### E. Performance under Resistance Variation

1) *Motoring Mode:* Algorithm is tested for low speed operation considering  $R_s$  variation under constant torque as shown in Fig (9). Stator resistance is varied to twice its original value in the form of ramp as shown in Fig 9(a). The estimated speed, actual speed is following the reference speed as shown in Fig. 9(b). Torque is kept constant at 2 N-m.

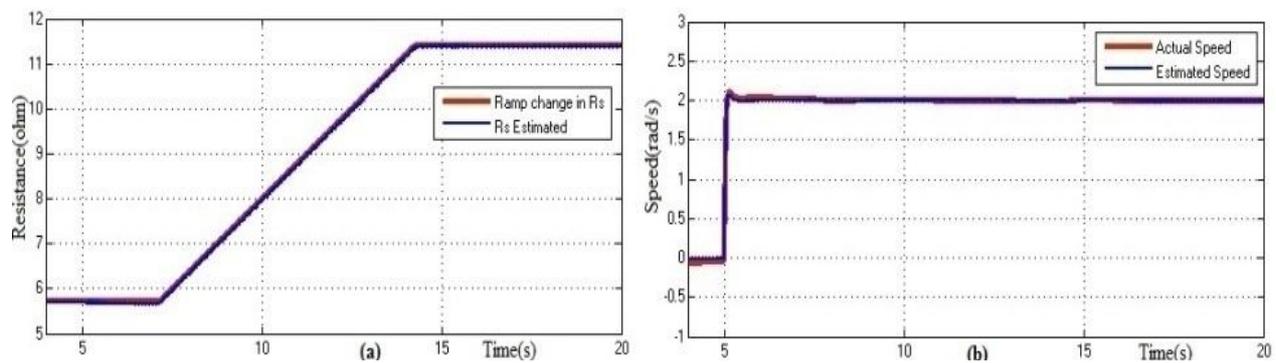


Fig.9. (a) Resistance variation[Ω] versus time[s], (b)Actual speed and estimated speed [rad/s] versus time[s]

2) *Regenerative mode:* Motor speed is changed from +2 rad/s to -2rad/s keeping the torque constant at 5 N-m. The drive is operated in motoring mode up to 10s. Thereafter, it enters in the regenerating mode of operation. The estimated rotor speed is shown in Fig. 10(a). At 14s,  $R_s$  is changed to twice of its original value as shown in Fig. 10(b). The estimator stills works successfully.

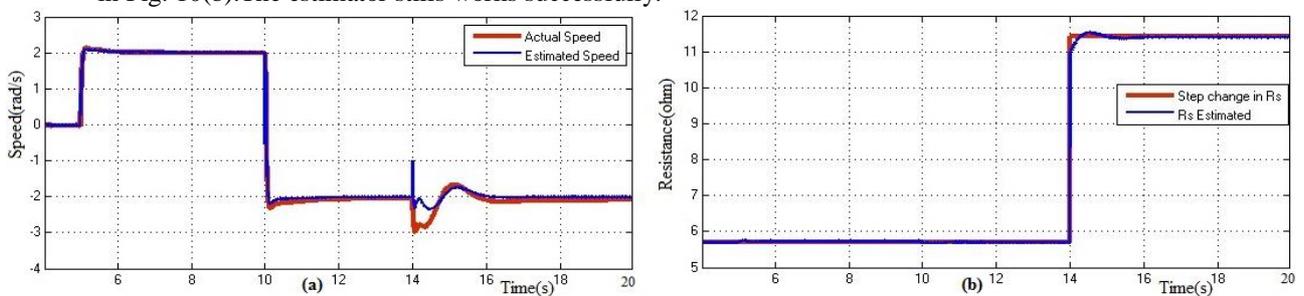


Fig.10. (a)Actual speed and estimated speed [rad/s] versus time[s], (b)Resistance variation[Ω] versus time[s]

3) *Performance under load and  $R_s$  variations:* Here drive is operated at a speed of 5 rad/sec as shown in Fig. 11(a). A load torque of 2 N-m is applied initially as shown in Fig. 11(b). Now between 7.25s-14.25s  $R_s$  is varied to twice of its original value in ramp form Fig. 11(c). During  $R_s$  variation (i.e., at 10s) load is increased to 5N-m. So from above results it is observed that the drive is stable even load changes during  $R_s$  variation.

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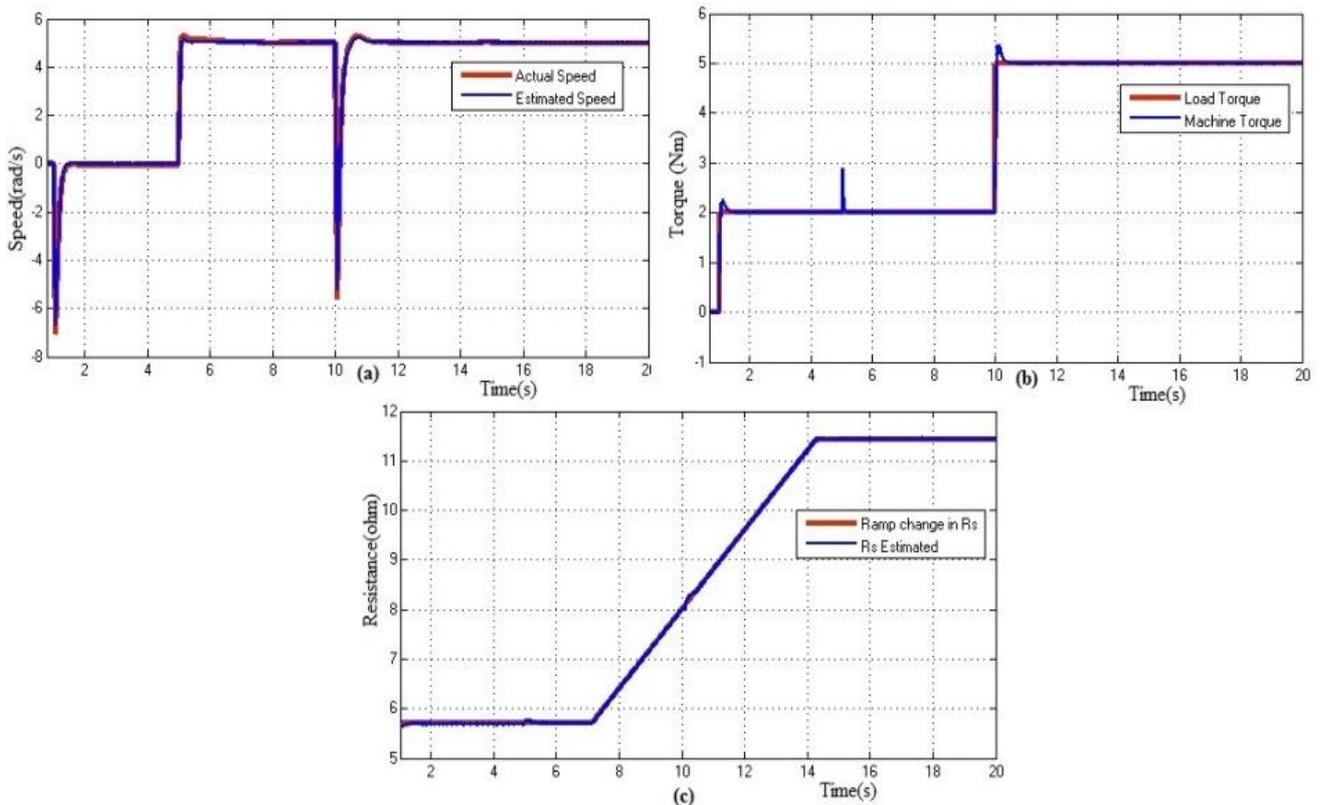


Fig.11.(a)Actual speed and estimated speed [rad/s] versus time[s],(b) Machine torque and load torque[Nm] versus time[s],(c)Resistance variation[Ω] versus time[s]

## VI. CONCLUSION

This paper has presented X-MRAC based speed estimation with stator resistance updation. The X-MRAC based speed estimation technique is stable in all four quadrants of operation and also suitable for low speed and zero speed operation. The adjustable model of X-MRAC depends on stator resistance making the technique sensitive to stator resistance variation. However, another MRAC may be added to X-MRAC based speed estimation to compensate for the variation in stator resistance. Moreover from the simulation results using a 1.3-kW induction motor drive system, it is shown that the speed sensorless drive, that require stator resistance information, can offer better performance with the inclusion of  $R_s$  estimation technique. An experimental prototype is under progress.

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### BIOGRAPHY



Aswathy Vijay received the B.Tech degree in Electrical and Electronics Engineering from Amal Jyothi College of Engineering, Kanjirapally, Kerala in the year 2012. Currently she is pursuing her M.Tech in Industrial Drives and Control from Rajiv Gandhi Institute of Technology, Kottayam, Kerala, India.



A.C Binoj Kumar received the B.Tech degree from Rajiv Gandhi Institute of Technology, Kottayam, Kerala in 1998 and the M.Tech degree from College of Engineering, Thiruvananthapuram, India in 2001. Currently he is working as Assistant Professor in the Department of Electrical Engineering, Rajiv Gandhi Institute of Technology, Kottayam, India. His research interests include pulse-width modulation techniques and electrical drives.