

The Synergistic Effect of La And Yb on the Microstructure and Mechanical Properties of Al-Cu-Mg Alloy

Xiuliang Zou^{1,2}, Lanjian Yu^{1,2}, Zijian Cheng^{1,2}, Hong Yan^{1,2*}

¹School of Advanced Manufacturing, Nanchang University, Nanchang 330031, China

²Key Laboratory of Light Alloy Preparation & Processing in Nanchang City, Nanchang 330031, China

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***For Correspondence:**

Hong Yan, School of Advanced

Manufacturing, Nanchang University,

Nanchang 330031, China

E-mail: hyan@ncu.edu.cn

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ABSTRACT

The Al-4.6Cu-1.6Mg alloys with different contents of La and Yb were fabricated by ultrasonic assisted casting in this study. The synergistic effect of La and Yb additions on the microstructure and mechanical properties of Al-4.6Cu-1.6Mg alloys was systematically studied. The results showed that adding La and Yb into Al-4.6Cu-1.6Mg alloys had an obvious grain refining effect and could form new two phases of $\text{Al}_6\text{Cu}_6\text{La}$ and $\text{Al}_{7.4}\text{Cu}_{9.6}\text{Yb}_2$. The Al-4.6Cu-1.6Mg-0.6 (La+Yb) alloy exhibited the optimal microstructure and mechanical properties. Compared to Al-4.6Cu-1.6Mg alloy, the grain was obviously refined. According to the calculated results, the grain refining effect was attributed to the heterogeneous nucleation and compositional undercooling. Additionally, the yield strength, ultimate tensile strength and elongation of Al-4.6Cu-1.6Mg-0.6 (La+Yb) alloy were 181.2 MPa, 264.5 MPa and 6.3%, which were 41.2%, 45.1% and 75.0% higher than those of the unmodified alloy, respectively. The strength mechanisms of Al-4.6Cu-1.6Mg-0.6 (La+Yb) alloy were ascribed to the refinement strengthening, solid solution strengthening and second phase strengthening, in which the refinement strengthening was the main strength mechanism.

Keywords: Microstructure; Mechanical properties; Al-4.6Cu-1.6Mg-0.6 (La+Yb) alloy; Grain refining; Strengthening mechanisms

INTRODUCTION

Due to their high strength, good machinability and excellent heat and damage resistance performance, Al-Cu-Mg alloys have been extensively used in aerospace industry and automobile manufacturing [1-3]. However, the application of casting Al-Cu-Mg alloys has been greatly limited because of the coarse second phases and dendritic structures [4,5].

Accordingly, in order to meet the increasingly strict manufacturing requirements, it is very necessary to further enhance comprehensive performance of Al-Cu-Mg alloys. It is well known that adding Rare Earth (RE) elements into aluminum alloys can significantly improve their microstructure and mechanical properties [6,7]. Up to now, a number of scholars have studied the effects of RE elements, such as La, Er, Ce, Sc, Y and Yb on the microstructure and mechanical properties of various aluminum alloys [8-13].

Specially, as the most economic light RE element, La has been attracted extensively attention and widely used in recent years. Zheng et al., investigated the effect of trace La addition on the α -Al grain and eutectic Si as well as mechanical properties of Al-Si alloys [14]. They observed that 0.06 wt.% La addition was sufficient to achieve the best modified effect for the microstructure and mechanical properties of the Al-Si alloys. And, they also concluded that La refined α -Al grain by reducing the wetting angle and modified the eutectic Si by changing the growth method of eutectic Si. Also demonstrated the similar effects on the refinement mechanism of the α -Al grains and modification behavior of the $\text{Al}_{13}\text{Fe}_4$ phase in the Al-Fe-La alloy [15]. Besides, they found that adding La into Al-Fe alloys could achieve simultaneous improvements of their strength and plasticity. Meanwhile, as one of the most effective heavy RE elements, Yb has also received widespread concerns. Wang et al., explored the influence of Yb addition on the microstructure and mechanical properties of Al-Ni alloy [16]. They indicated that trace Yb addition decreased the SDAS of α -Al grain and refined the Al_3Ni phase, which resulted in the improvement of mechanical properties of the alloy. Xiong et al., reported the microstructure and mechanical properties of ADC12 alloy with different Yb additions [17]. The results showed that 0.8 wt.% Yb addition obtained the optimal mechanical properties, due to refining coarse α -Al dendrites and modifying the morphology of the β -Fe and eutectic Si phases. As can be noted from the reported literature, the effects of La or Yb on the microstructure and mechanical properties of aluminum alloys were studied individually. Related study indicated that the modification effect of mixed RE was better than that of single RE, and mixed RE had a synergistic superposition [18]. However, as far as we know, there are few literature about the combined effect of La and Yb on the microstructure and mechanical properties of aluminum alloys, especially for Al-Cu-Mg alloys. Additionally, the refinement mechanisms of RE are complex and have still not formed unified conclusion yet. At present, the accepted refinement mechanisms of RE mainly include compositional undercooling and heterogeneous nucleation theories [18-22]. For heterogeneous nucleation theory, the formation of RE intermetallics can serve as effective nucleation substrates, which contributes to increase nucleation rate, thus refining α -Al grains. For compositional undercooling theory, RE atoms enrich at solid-liquid interface front during the solidification process, which can generate compositional undercooling and hinder the continuous growth of α -Al grains, thus refining the grains. However, whether the refinement mechanisms of La and Yb on Al-Cu-Mg alloys can be elaborated by the compositional undercooling or heterogeneous nucleation theories lack the in-depth study and need to be further confirmed. Moreover, the strengthening mechanisms of La and Yb on Al-Cu-Mg alloys are still unclear. Hence, it is necessary to study the combined effect of La and Yb on the microstructure and mechanical properties of Al-Cu-Mg alloys.

In this work, Al-4.6Cu-1.6Mg alloys with different contents of La and Yb were fabricated by ultrasonic assisted casting. And, the combined effect of La and Yb on the microstructure and mechanical properties of Al-4.6Cu-1.6Mg alloys was studied. Moreover, the refinement mechanisms of La and Yb on the α -Al grains were discussed in details. Furthermore, the strengthening mechanisms of La and Yb on Al-4.6Cu-1.6Mg alloys were quantitatively analyzed.

MATERIALS AND METHODS

Materials preparation

In this experiment, Al-4.6Cu-1.6Mg alloys, Al-10% La and Al-10%Yb master alloys were used as raw materials. Firstly, Al-4.6Cu-1.6Mg alloys placing into graphite crucible were melted in a resistance furnace at 750°C. After degassing and removing the slag, the Al-10% La and Al-10% Yb master alloys wrapped by aluminum foil were added into melt. Then, the melt was held at 720°C for 30 min in order to ensure that the master alloys were completely melted. Next, the high-energy ultrasonic vibration with the ultrasonic power of 2.8 kW and ultrasonic frequency of 20 kHz was applied to the melt for 10 min. After removing the slag, the melt was poured in to a permanent metal mold preheated to 200°C. Finally, the Al-4.6Cu-1.6Mg alloys with different contents of La and Yb were obtained. Table 1 presents the chemical composites of the experimental alloys analyzed by Inductively Coupled Plasma-Atomic Emission Spectroscopy. During the whole experiment, argon gas was applied to protect the melt from oxidation as shown in Table 1.

Table 1. Chemical composites of the experimental alloys (wt.%).

Alloy	Cu	Mg	Si	Fe	Mn	La	Yb	Al
Al-4.6Cu-1.6Mg	4.62	1.63	0.1	0.18	0.3	-	-	Bal.
Al-4.6Cu-1.6Mg-0.3 (La+Yb)	4.58	1.57	0.1	0.15	0.4	0.16	0.13	Bal.
Al-4.6Cu-1.6Mg-0.6 (La+Yb)	4.57	1.62	0.1	0.19	0.3	0.29	0.32	Bal.
Al-4.6Cu-1.6Mg-0.9 (La+Yb)	4.61	1.61	0.1	0.21	0.4	0.47	0.44	Bal.

Material characterization

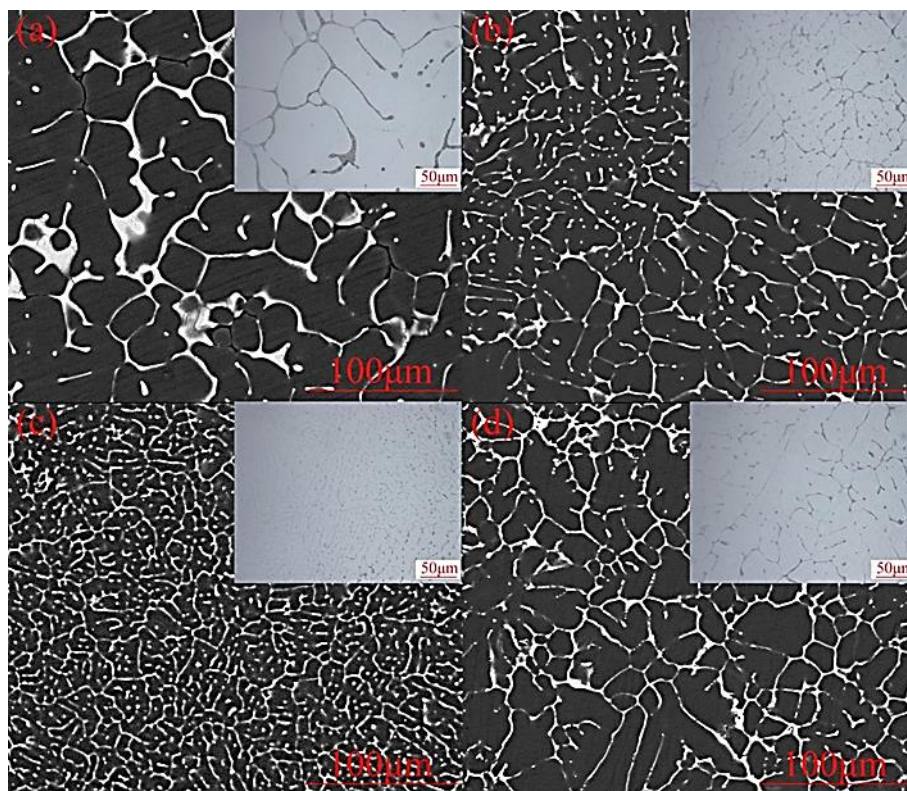
The microstructure and fracture surfaces were characterized by scanning electron microscopy (SEM, Tescan-Vega3) equipped with Energy Dispersive X-ray Spectroscopy (EDS). The phase composition was identified by X-ray diffraction (XRD, D8 ADVANCE). The solidification behavior of the alloys was analyzed by differential scanning calorimeter (DSC, DSC404F3). The RE intermetallics in the Al-Cu-Mg-0.6 (La+Yb) were observed by transmission electron microscopy (TEM, TalosF200X). The mean diameter of α -Al phases and secondary dendrite arm spacing (SDAS) were measured by Image Pro Plus 6.0 software. The tensile samples were machined into tensile bars, which the gauge length was 40 mm and the diameter was 6 mm. The tensile tests were conducted on an UTM5105 machine at a strain rate of 0.001 s⁻¹. In order to guarantee the reliability of measure results, more than three samples were tested for each condition.

RESULTS AND DISCUSSION

Microstructure

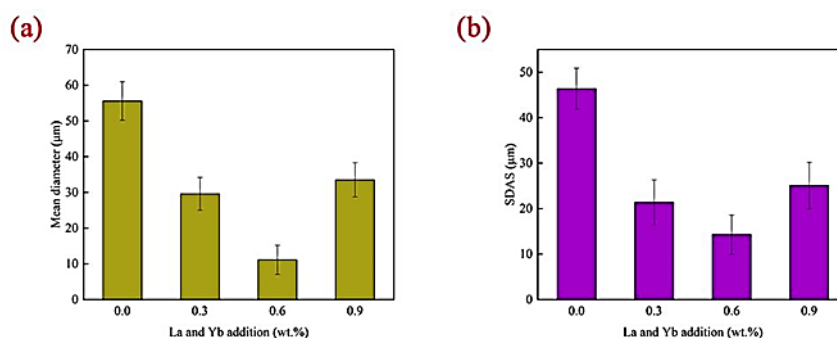
The microstructures of Al-4.6Cu-1.6Mg alloys with different contents of La and Yb are displayed in Figure 1. Without the addition of La and Yb, the coarse α -Al dendrites are clearly observed, as depicted in Figure 1a. As the La and Yb addition reaches 0.3 wt.%, the content of coarse α -Al dendrites significantly decreases (Figure 1b). When the La and Yb addition increases up to 0.6 wt.%, the mean diameter of α -Al phases become finest (Figure 1c). While the La and Yb addition continues to increase, the α -Al dendrites begin to become coarse, as displayed in Figure 1d.

Figure 1. Microstructures of Al-4.6Cu-1.6Mg alloys with different contents of La and Yb: a) 0 wt.%; b) 0.3 wt.%; c) 0.6 wt.%; d) 0.9 wt.%.



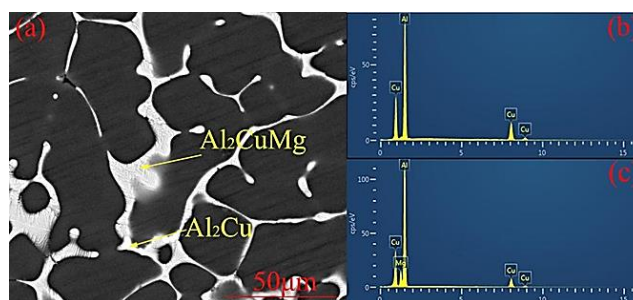
Similarly, the change trend of SADS is the same as that of α -Al dendrites with different contents of La and Yb. The mean diameter of α -Al phases and SADS in the Al-4.6Cu-1.6Mg alloys with different contents of La and Yb are illustrated in Figure 2. It can be seen that La and Yb addition can achieve obviously grain refinement as shown in Figure 2.

Figure 2. (a) mean diameter of α -Al phases and (b) SADS in the Al-4.6Cu-1.6Mg alloys with different contents of La and Yb.



The SEM image and EDS spectra of unmodified Al-4.6Cu-1.6Mg alloy are shown in Figure 3. It can be noted from Figure 3a that the microstructure of as-cast Al-4.6Cu-1.6Mg alloy is composed of α -Al matrix and grain boundary eutectic phases including block-shaped phase and grid-like phase. As depicted in Figure 3b, the EDS result reveals that the stoichiometry of block-shaped phase is 77.15 at.% Al and 22.85 at.% Cu. Combining with the XRD results, it can be seen that the block-shaped phase is Al_2Cu phase. As exhibited in Figure 3c, the EDS result indicates that the stoichiometry of grid-like phase is 77.02 at.% Al, 12.44 at.% Cu, 10.54 at.% Mg, which is close to the stoichiometry of the Al_2CuMg phase. Thus, the microstructure of as-cast Al-4.6Cu-1.6Mg alloy mainly consists of α -Al matrix, Al_2Cu and Al_2CuMg phases as shown in Figure 3.

Figure 3. SEM image and EDS spectra of unmodified Al-4.6Cu-1.6Mg alloy: a) SEM image; b) EDS result of block-shaped phase; c) EDS result of grid-like phase.



Besides the phases mentioned above, some new phases appear in the microstructure of Al-4.6Cu-1.6Mg-0.6 (La+Yb) alloy. Figure 4 shows the SEM image and corresponding element mappings of the microstructure in Al-4.6Cu-1.6Mg-0.6 (La+Yb) alloy. It can be seen from Figures 4d-4f that the element distributions of Cu, La and Yb are almost the same. Combining XRD result and previous studies [23,24], new two kinds of phases of $\text{Al}_6\text{Cu}_6\text{La}$ and $\text{Al}_{7.4}\text{Cu}_{9.6}\text{Yb}_2$ may be formed in Al-4.6Cu-1.6Mg-0.6 (La+Yb) alloy. Based on the results of calculated formation enthalpies of infinite diluted solution, a strong interaction exists between Cu and La, Yb atoms [25,26], which shows that La, Yb and Cu atoms have favourable chemical affinity, thus resulting in that $\text{Al}_6\text{Cu}_6\text{La}$ and $\text{Al}_{7.4}\text{Cu}_{9.6}\text{Yb}_2$ phases may be formed when adding La and Yb into the Cu-containing aluminum alloy. Additionally, Mg element is basically dissolved in the α -Al matrix, as shown in Figure 4.

Figure 4. A SEM image and b, c, d, e and f corresponding element mappings of the microstructure in Al-4.6Cu-1.6Mg-0.6 (La+Yb) alloy.

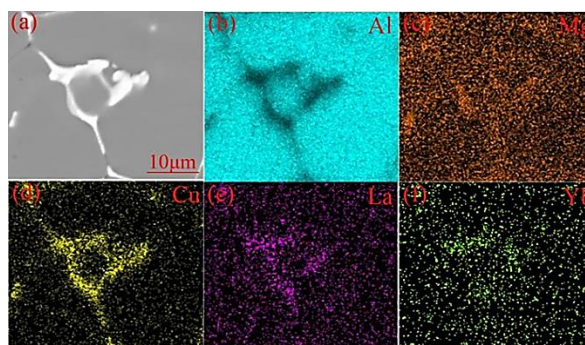
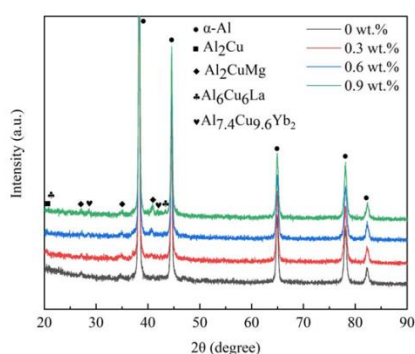


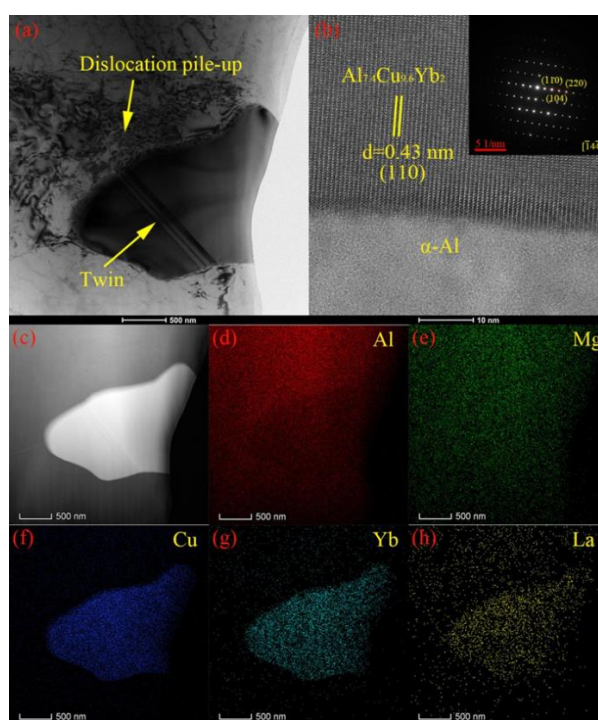
Figure 5 is XRD patterns of Al-4.6Cu-1.6Mg alloys with different contents of La and Yb. It can be observed that all alloys are mainly composed of α -Al matrix, Al_2Cu and Al_2CuMg phases. Compared to unmodified Al-4.6Cu-1.6Mg alloy, two kinds of new phases of $\text{Al}_6\text{Cu}_6\text{La}$ and $\text{Al}_{7.4}\text{Cu}_{9.6}\text{Yb}_2$ are observed in the modified alloys. And, the quantity of $\text{Al}_6\text{Cu}_6\text{La}$ and $\text{Al}_{7.4}\text{Cu}_{9.6}\text{Yb}_2$ phases increase with the increase of La and Yb addition as shown in Figure 5.

Figure 5. XRD patterns of Al-4.6Cu-1.6Mg alloys with different contents of La and Yb.



To further confirm the formation of $\text{Al}_6\text{Cu}_6\text{La}$ and $\text{Al}_{7.4}\text{Cu}_{9.6}\text{Yb}_2$ phases, a detailed TEM observation was conducted. Figure 6 illustrates the bright field TEM images, Selected Area Electron Diffraction (SAED) patterns, High-Resolution Transmission Electron Microscopy (HRTEM) images and EDS mapping analysis of Al-4.6Cu-1.6Mg-0.6 (La+Yb) alloy. A irregular blocky particle with twin structure can be observed, as shown in Figure 6a. And, the average size of the particle is found to be $\sim 1.5 \mu\text{m}$. Based on the SAED pattern, it is observed that the diffraction spots are in accordance with the diffraction spots incident by $\text{Al}_{7.4}\text{Cu}_{9.6}\text{Yb}_2$ phase from the direction of $[-14\bar{4}]$, as shown in Figure 6b. Therefore, the phase can be identified as $\text{Al}_{7.4}\text{Cu}_{9.6}\text{Yb}_2$ phase (trigonal system, $a=b=0.8691 \text{ nm}$, $c=1.2698 \text{ nm}$, with space group R-3m). As shown in the HRTEM image, the interplanar spacing of this phase is 0.43 nm , corresponding to the (110) crystal plane of $\text{Al}_{7.4}\text{Cu}_{9.6}\text{Yb}_2$ phase. According to the results of EDS mapping in Figures 6c-6h, the particle consists mainly of Al, Cu, La and Yb elements and the element distributions are almost the same, suggesting that the $\text{Al}_6\text{Cu}_6\text{La}$ phase may be also formed in addition to forming $\text{Al}_{7.4}\text{Cu}_{9.6}\text{Yb}_2$ phase. According to relevant literature [26,27], the standard formation gibbs free energy of $\text{Al}_6\text{Cu}_6\text{La}$ phase is more negative than that of $\text{Al}_{7.4}\text{Cu}_{9.6}\text{Yb}_2$ phase, resulting in that the order of ability to form $\text{Al}_6\text{Cu}_6\text{La}$ phase is superior to that of $\text{Al}_{7.4}\text{Cu}_{9.6}\text{Yb}_2$ phase. Accordingly, the $\text{Al}_{7.4}\text{Cu}_{9.6}\text{Yb}_2$ phase is formed by covering on the $\text{Al}_6\text{Cu}_6\text{La}$ phase, which makes the $\text{Al}_6\text{Cu}_6\text{La}$ phase unable to be observed. A similar phenomenon was observed in the (Ce+Yb)-modified Al-6Si-0.6Mg-0.6Cu-0.2Cr cast alloy [28]. Additionally, some studies have shown that when adding minor RE elements into the alloy, RE atoms could substitute lattice atoms of particles and adsorb on the growing interface of primary phases, thus changing the growth direction and generating the twins [29,30]. Besides, plenty of high density dislocations exist near $\text{Al}_6\text{Cu}_6\text{La}$ and $\text{Al}_{7.4}\text{Cu}_{9.6}\text{Yb}_2$ particles, as shown in Figure 6a. This is due to the fact that $\text{Al}_6\text{Cu}_6\text{La}$ and $\text{Al}_{7.4}\text{Cu}_{9.6}\text{Yb}_2$ particles can hinder the dislocations motion, resulting in the dislocations pile-up ahead of these particles. The interaction between these particles and dislocations can lead to the second phase strengthening as shown in Figure 6.

Figure 6. TEM analysis results of Al-4.6Cu-1.6Mg-0.6 (La+Yb) alloy: a) Bright field image of $\text{Al}_{7.4}\text{Cu}_{9.6}\text{Yb}_2$ phase; b) HRTEM image of $\text{Al}_{7.4}\text{Cu}_{9.6}\text{Yb}_2$ phase and the corresponding SAED pattern; c) HAADF-STEM image of $\text{Al}_{7.4}\text{Cu}_{9.6}\text{Yb}_2$ phase; d, e, f, g and h EDS mapping analysis of the Al, Zn, Cu, Yb and La.



The DSC curves of Al-4.6Cu-1.6Mg alloys with different contents of La and Yb are displayed in Figure 7. It can be observed that the DSC curves of all alloys contain three endothermic peaks (Peak1, Peak2 and Peak3). Peak1, Peak2 and Peak3 represent the melting temperatures of α -Al dendrites, Al₂CuMg and Al₂Cu phases, respectively as shown in Figure 7.

Figure 7. DSC curves of Al-4.6Cu-1.6Mg alloys with different contents of La and Yb.

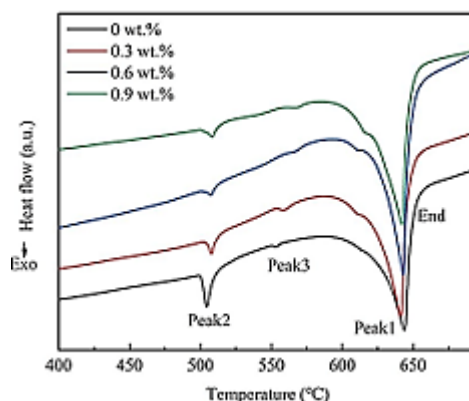


Table 2 presents the analysis results of DSC curves in Figure 7. It can be noted that adding La and Yb into Al-4.6Cu-1.6Mg alloys can decrease the nucleation undercooling of α -Al, which contributes to promoting the nucleation during the solidification process, thus refining the α -Al grain. It is worth noting that the enthalpy of Al₂CuMg phase decreases when adding La and Yb into Al-4.6Cu-1.6Mg alloys, indicating that the number of Al₂CuMg phase is reduced in the modified alloys as shown in Table 2.

Table 2. Results of DSC curves of Al-4.6Cu-1.6Mg alloys with different contents of La and Yb.

Number	Eutectic phases				α -Al	
	Enthalpy (J/g)	Peak2 (°C)	Peak3 (°C)	Peak1 (°C)	End (°C)	ΔT (°C)
0 wt.%	14.88	504.41	552.75	643.96	648.6	5.22
0.3 wt.%	7.64	507.68	558.52	641.38	645.62	4.24
0.6 wt.%	3.123	507.6	566.7	643.17	646.58	3.41
0.9 wt.%	5.901	508.22	562.77	642.22	646.22	4

Mechanical properties

The mechanical properties of Al-4.6Cu-1.6Mg alloys with different contents of La and Yb are displayed in Figure 8. It can be noted that the yield strength, ultimate tensile strength and elongation of the alloys increase first and then decrease with increasing La and Yb addition. The unmodified alloy exhibits the lowest yield strength, ultimate tensile strength and elongation, which are 128.3 MPa, 182.3 MPa and 3.6%, respectively. While the Al-4.6Cu-1.6Mg-0.6 (La+Yb) alloy shows the optimal yield strength, ultimate tensile strength and elongation of 181.2 MPa, 264.5 MPa and 6.3%, which are 41.2%, 45.1% and 75.0% higher than those of the unmodified alloy, respectively as shown in Figure 8.

Figure 8. Mechanical properties of Al-4.6Cu-1.6Mg alloys with different contents of La and Yb: a) Yield strength, ultimate tensile strength and elongation; b) Stress-strain curves.

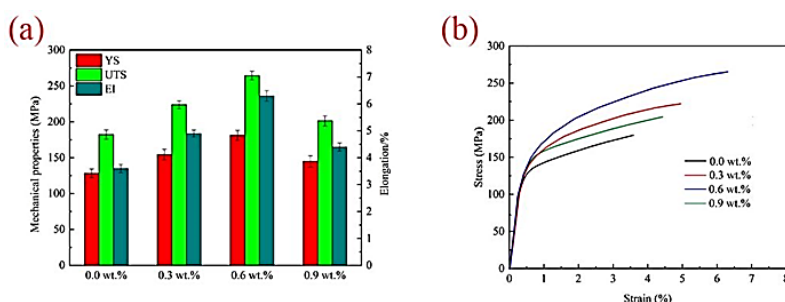
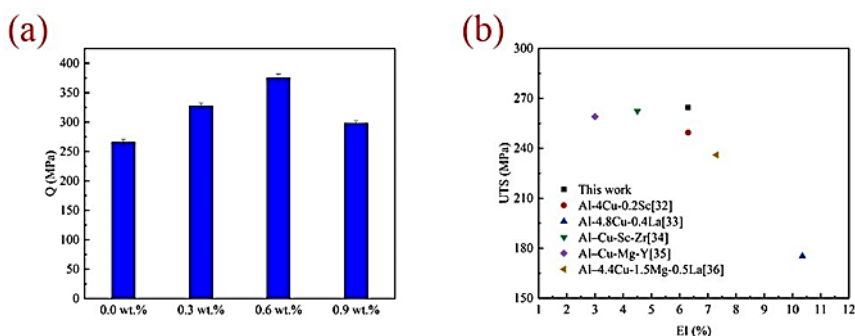


Figure 9a presents the Q values of Al-4.6Cu-1.6Mg alloys with different contents of La and Yb, which is an integrated mechanical properties index combining the strength and elongation of the alloys. The Q value can be expressed as [31].

$$Q = UTS + a \times \log(EI)$$

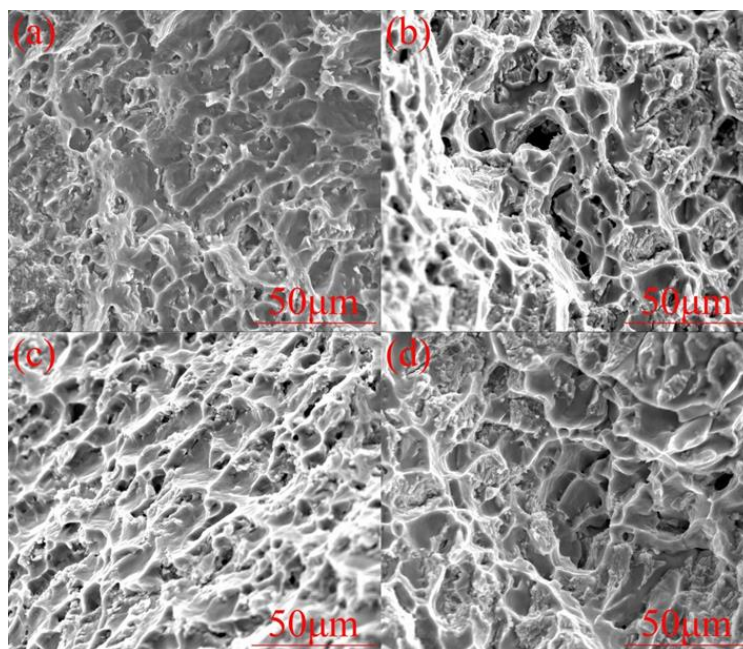
Where UTS is the ultimate tensile strength, EI is the elongation and a is 150 MPa for Al-4.6Cu-1.6Mg alloys [31]. The Q value can better reflect the true mechanical properties of aluminum alloy castings than the elongation or the tensile strength individual. It can be concluded that the Q value of Al-4.6Cu-1.6Mg-0.6 (La+Yb) alloy reaches the maximum, which increases from 265.7 to 384.4, compared to the unmodified alloy, suggesting that La and Yb addition significantly improve the mechanical properties of Al-4.6Cu-1.6Mg alloy. Figure 9b compares the mechanical properties of Al-Cu-(Mg) alloys modified with different RE [32-36]. It can be noted that the Al-4.6Cu-1.6Mg-0.6 (La+Yb) alloy shows a excellent combination of strength and elongation than most other RE modified Al-Cu-(Mg) alloys as shown in Figure 9.

Figure 9. a) Q values of Al-4.6Cu-1.6Mg alloys with different contents of La and Yb; b) Comparison for the mechanical properties of Al-Cu-(Mg) alloys modified with different RE



The fracture morphologies of Al-4.6Cu-1.6Mg alloys with different contents of La and Yb are characterized in Figure 10. It can be seen from Figure 10a that the fracture surface of the unmodified alloy reveals an evident brittle fracture, including numerous cleavage planes, which is in accordance with the low strength and strain of the unmodified alloy. With the increase of La and Yb addition, the number of cleavage planes decrease while the number of dimples increase, which changes the fracture behaviors of the alloys from brittle to ductile. When the La and Yb addition is 0.3 wt.%, the fracture surface of the alloy shows a ductile-brittle mixing fracture, containing some dimples and tearing ridges, as shown in Figure 10b. While the La and Yb addition reaches 0.6 wt.%, the fracture surface of the alloy mainly exhibits a ductile fracture, possessing the highest number of dimples (Figure 10c), which corresponds to the optimal strength and elongation. As the La and Yb addition further increases to 0.9 wt.%, the fracture surface of the alloy also belongs to a ductile-brittle mixing fracture, only including few dimples and tearing ridges (Figure 10d).

Figure 10. Fracture morphologies of Al-4.6Cu-1.6Mg alloys with different contents of La and Yb: a) 0 wt.%; b) 0.3 wt.%; c) 0.6 wt.%; d) 0.9 wt.%.



Grain refinement mechanisms

At present, the widely accepted refinement mechanisms for RE refining the grains of aluminum alloys mainly include heterogeneous nucleation and compositional undercooling theories.

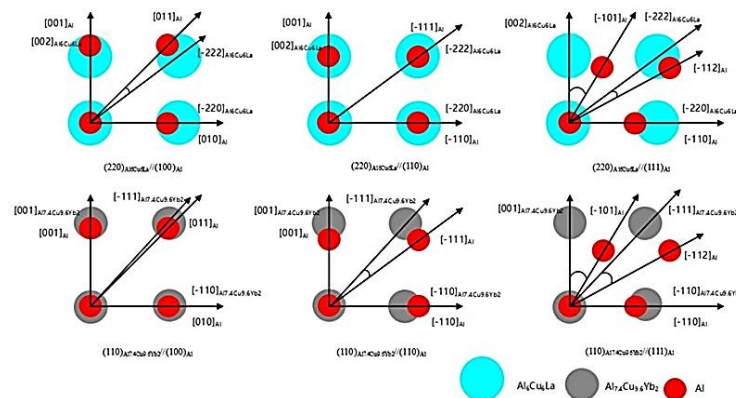
Compared to the homogeneous nucleation, the heterogeneous nucleation can reduce the critical nucleation work of primary α -Al, thus refining the α -Al grain. Combining the results of SEM and TEM, it can be seen that adding La and Yb into Al-4.6Cu-1.6Mg alloy can form $\text{Al}_6\text{Cu}_6\text{La}$ and $\text{Al}_{7.4}\text{Cu}_{9.6}\text{Yb}_2$ particles. Hence, the refinement mechanism depends on the fact that the $\text{Al}_6\text{Cu}_6\text{La}$ and $\text{Al}_{7.4}\text{Cu}_{9.6}\text{Yb}_2$ particles can serve as the effective heterogeneous nucleation substrates for α -Al. The criterion for the nucleation substrate effectively promoting α -Al nucleation is that the disregistry between the substrate and the nucleated solid phase should be less than 12% [37]. Generally, the lattice disregistry between two phases is evaluated by Turnbull-Vonnegut equation. However, the equation imposes a strict constraint on the choice of a crystallographic relationship due to only considering planes of similar atomic arrangements. Thus, Bramfitt modified the Turnbull-Vonnegut equation in the light of angular difference between the crystallographic directions with the planes so that it could be applied to crystallographic combinations of two phases with planes of different lattice arrangements. The modified equation can be expressed as follows.

$$\delta_{(hkl)_n}^{(hkl)_s} = \frac{\sum_{i=1}^3 \frac{(d_{[uvw]_s^i} \cos \theta) - d_{[uvw]_n^i}}{d_{[uvw]_n^i}}}{3} \times 100\%$$

Where $(hkl)_s$ is denoted as a low index plane of the substrate, $(hkl)_n$ is denoted as a low index plane of the nucleated solid phase, $[uvw]_s$ represents a low index direction in $(hkl)_s$, $[uvw]_n$ represents a low index direction in $(hkl)_n$, $d_{[uvw]_s}$ denotes the atomic distance along $[uvw]_s$, $d_{[uvw]_n}$ denotes the atomic distance along $[uvw]_n$, θ is denoted as the angle between $[uvw]_s$ and $[uvw]_n$. The α -Al phase has a face centered cubic crystal structure with the lattice constant $a=b=c=0.4049$ nm. $\text{Al}_6\text{Cu}_6\text{La}$ has also a face centered cubic crystal structure with the lattice constant $a=b=c=1.1899$ nm. While $\text{Al}_{7.4}\text{Cu}_{9.6}\text{Yb}_2$ belongs to a trigonal system, with the lattice constant $a=b=0.8691$ nm.

nm, $c=1.2698$ nm and $\alpha=\beta=90^\circ$, $\gamma=120^\circ$. For this study, the (220) of $\text{Al}_6\text{Cu}_6\text{La}$ phase and the (110) of $\text{Al}_{7.4}\text{Cu}_{9.6}\text{Yb}_2$ phase are selected as the nucleating planes, respectively. Meanwhile, three low index planes (100), (110) and (111) of $\alpha\text{-Al}$ are selected as the matching planes. The crystallographic relationships between $\alpha\text{-Al}$ and $\text{Al}_6\text{Cu}_6\text{La}$, $\text{Al}_{7.4}\text{Cu}_{9.6}\text{Yb}_2$ used for planar disregistry calculations are depicted in Figure 11.

Figure 11. Crystallographic relationships between $\alpha\text{-Al}$ and $\text{Al}_6\text{Cu}_6\text{La}$, $\text{Al}_{7.4}\text{Cu}_{9.6}\text{Yb}_2$ used for planar disregistry calculations.



The parameters for the planar disregistry equation between $\alpha\text{-Al}$ and $\text{Al}_6\text{Cu}_6\text{La}$, $\text{Al}_{7.4}\text{Cu}_{9.6}\text{Yb}_2$ are presented in Tables 3 and 4, respectively.

According to the results, the planar disregistry of $(220)_{\text{Al}_6\text{Cu}_6\text{La}} // (100)_{\text{Al}}$, $(220)_{\text{Al}_6\text{Cu}_6\text{La}} // (110)_{\text{Al}}$, $(220)_{\text{Al}_6\text{Cu}_6\text{La}} // (111)_{\text{Al}}$ are 12.05%, 2.04% and 19.67, respectively. Meanwhile, the planar disregistry of $(110)_{\text{Al}_{7.4}\text{Cu}_{9.6}\text{Yb}_2} // (100)_{\text{Al}}$, $(110)_{\text{Al}_{7.4}\text{Cu}_{9.6}\text{Yb}_2} // (110)_{\text{Al}}$, $(110)_{\text{Al}_{7.4}\text{Cu}_{9.6}\text{Yb}_2} // (111)_{\text{Al}}$ are 2.86%, 16.82% and 7.75%, respectively. The planar disregistry of $(220)_{\text{Al}_6\text{Cu}_6\text{La}} // (110)_{\text{Al}}$, $(110)_{\text{Al}_{7.4}\text{Cu}_{9.6}\text{Yb}_2} // (100)_{\text{Al}}$ and $(110)_{\text{Al}_{7.4}\text{Cu}_{9.6}\text{Yb}_2} // (111)_{\text{Al}}$ are less than 12%, indicating good orientation relationships between $\alpha\text{-Al}$ and $\text{Al}_6\text{Cu}_6\text{La}$, $\text{Al}_{7.4}\text{Cu}_{9.6}\text{Yb}_2$, which is consistent with the result of HRTEM image. Based on the crystallographic relationships, the $\text{Al}_6\text{Cu}_6\text{La}$ and $\text{Al}_{7.4}\text{Cu}_{9.6}\text{Yb}_2$ phases can be regarded as the effective heterogeneous nucleation substrates for $\alpha\text{-Al}$, thus refining grains as shown in Tables 3 and 4.

Table 3. Parameters for the planar disregistry equation between $\alpha\text{-Al}$ and $\text{Al}_6\text{Cu}_6\text{La}$.

Matching interfaces	$[\text{uvw}]_s$	$[\text{uvw}]_n$	$d_{[\text{uvw}]_s}$	$d_{[\text{uvw}]_n}$	θ	$d_{[\text{uvw}]_s} \cos \theta$	$\delta(\%)$
$(220)_{\text{Al}_6\text{Cu}_6\text{La}} // (100)_{\text{Al}}$	$[-220]$	$[010]$	$2\sqrt{2} \times 1.1899$	7×0.4049	0	3.3655	12.05
	$[-222]$	$[011]$	$2\sqrt{3} \times 1.1899$	$7 \times \sqrt{2} \times 0.4049$	9.72	4.0628	
	$[002]$	$[001]$	2×1.1899	7×0.4049	0	2.3798	
	$[-220]$	$[-110]$	$2\sqrt{2} \times 1.1899$	$6 \times \sqrt{2} \times 0.4049$	0	3.3655	
$(220)_{\text{Al}_6\text{Cu}_6\text{La}} // (110)_{\text{Al}}$	$[-222]$	$[-111]$	$2\sqrt{3} \times 1.1899$	$6 \times \sqrt{3} \times 0.4049$	0	4.1219	2.04
	$[002]$	$[001]$	2×1.1899	6×0.4049	0	2.3798	
	$[-220]$	$[-110]$	$2\sqrt{2} \times 1.1899$	$4 \times \sqrt{2} \times 0.4049$	0	3.3655	
$(220)_{\text{Al}_6\text{Cu}_6\text{La}} // (111)_{\text{Al}}$	$[-222]$	$[-112]$	$2\sqrt{3} \times 1.1899$	$4 \times \sqrt{6} \times 0.4049$	19.48	3.886	19.67
	$[002]$	$[-101]$	2×1.1899	$4 \times \sqrt{2} \times 0.4049$	30	2.061	

Table 4. Parameters for the planar disregistry equation between $\alpha\text{-Al}$ and $\text{Al}_{7.4}\text{Cu}_{9.6}\text{Yb}_2$.

Matching interfaces	$[\text{uvw}]_s$	$[\text{uvw}]_n$	$d_{[\text{uvw}]_s}$	$d_{[\text{uvw}]_n}$	θ	$d_{[\text{uvw}]_s} \cos \theta$	$\delta(\%)$
$(110)_{\text{Al}_{7.4}\text{Cu}_{9.6}\text{Yb}_2} // (100)_{\text{Al}}$	$[-110]$	$[010]$	1.2291	3×0.4049	0	1.2291	2.86
	$[-111]$	$[011]$	1.7672	$3 \times \sqrt{2} \times 0.4049$	0.96	1.767	
	$[001]$	$[001]$	1.2698	3×0.4049	0	1.2698	
	$[-110]$	$[-110]$	1.2291	$3 \times \sqrt{2} \times 0.4049$	0	1.2291	

$(110)_{Al7.4Cu9.6Yb2} // (110)_{Al}$	[-111]	[-111]	1.7672	$3 \times \sqrt{3} \times 0.4049$	10.67	1.7366	16.82
	[001]	[001]	1.2698	3×0.4049	0	1.2698	
	[-110]	[-110]	1.2291	$2 \times \sqrt{2} \times 0.4049$	0	1.2291	
$(110)_{Al7.4Cu9.6Yb2} // (111)_{Al}$	[-111]	[-112]	1.7672	$2 \times \sqrt{6} \times 0.4049$	8.81	1.7463	7.75
	[001]	[-101]	1.2698	$2 \times \sqrt{2} \times 0.4049$	30	1.0997	

According to Hume-Rothery theory, when the difference of atomic radius of two elements is more than 15%, it is difficult to form solid solution [38]. Table 5 presents the atomic radius and electronegativity of some alloying elements [39-41]. As can be seen, the atomic radius differences between La, Yb and Al are 30.8% and 35.7%, respectively. Therefore, the solubility of La and Yb atoms in the α -Al is very low, thus resulting in that La and Yb atoms enrich at solid-liquid interface front during the solidification process, which generates the local compositional undercooling as shown in Table 5.

Table 5. Atomic radius and electronegativity of the alloying elements.

Alloy elements	Al	Cu	Mg	La	Yb
Atomic radius (nm)	0.143	0.128	0.16	0.187	0.194
Electronegativity (V)	1.61	1.9	1.31	1.11	1.26

The generation of compositional undercooling zone at the solid-liquid interface front can hinder the continuous growth of the α -Al grains, thus refining the α -Al grains. The criterion for generating compositional undercooling at the solid-liquid interface front can be given as follows [42].

$$\frac{G_L}{R} < \frac{mC_0(1-K_0)}{D K_0}$$

Where G_L devotes the temperature gradient of solid-liquid interface front, R is the advance speed of solid-liquid interface, m devotes the line slope of the liquid phase, C_0 is the initial composition concentration of the solute, K_0 represents equilibrium distribution coefficient, D is diffusion coefficient.

Accordingly, the favorable conditions of compositional undercooling are low temperature gradient, fast solidification speed and high solute concentration of liquid phase for the given aluminum alloy. The influences of different solute atoms on the undercooling zone at the solid-liquid interface are evaluated. The parameters of compositional undercooling criterion for different solute atoms are presented in Table 6. Among them, the slope of the liquid us m and equilibrium distribution coefficient K_0 of solute La and Yb can be obtained by the Al-La and Al-Yb binary phase diagrams [43]. The calculated results of compositional undercooling criterion for different solute atoms are shown in Table 6. According to the calculated results, it can be concluded that La and Yb atoms can obviously generate compositional undercooling during the solidification process, thus refining the grains as shown in Tables 6 and 7.

Table 6. Calculated results of compositional undercooling criterion for different solute atoms.

Elements	GL/R	$mC_0(1-K_0)/(DK_0)$
La in Al	0.75~23.04	1.15×10^7
Yb in Al		2.11×10^8
Cu in Al		37.8
Mg in Al		9.63

Table 7. Parameters of compositional undercooling criterion for different solute atoms [43-49].

Elements	G_L (K/cm)	R (cm/s)	m	K_0	C_0 (wt.%)	D (cm ² /s)
La in Al	3.0-14.4	0.625~4	-1.7	0.004	0.3	1.1×10^{-5}

Yb in Al			-1.7	0.005	0.3	4.8×10^{-7}
Cu in Al			-3.4	0.17	4.6	2.02
Mg in Al			-6.2	0.51	1.6	0.99

Interaction intensity

The interaction intensity between atoms can evaluate the effect of La and Yb addition on Al-4.6Cu-1.6Mg alloys, which reflects the stability of the alloy compounds and solid solubility. According to Darken-Gurry theory, the interaction intensity between solvent A and solute B may be calculated from the atomic radius and electronegativity (Table 5), which can be defined as [50].

$$W_{A-B} = [(r_A - r_B)/(0.15 \times r_A)]^2 + [(N_A - N_B)/4]^2$$

Where r_A , r_B and N_A , N_B are the atomic radius and electronegativity of solvent element A and solute element B, respectively. According to Equation, the interaction strength of Al-Cu and Al-Mg are 1.01 and 1.19, respectively. When RE elements are added into Al-4.6Cu-1.6Mg alloys, the interaction intensity can be expressed as.

$$W_{(Al-X)-RE} = W_{Al-X} + W_{X-RE} - 8.8$$

Based on Equation, the interaction strength of Al-Cu-La, Al-Cu-Yb, Al-Mg-La, and Al-Mg-Yb are 5.55, 6.59, -6.09 and -5.59, respectively. It is clearly that the addition of La and Yb can increase the interaction between Al and Cu, while decrease the interaction between Al and Mg. Therefore, adding La and Yb into Al-4.6Cu-1.6Mg alloys can promote the formation of new RE phases of Al_6Cu_6La and $Al_{7.4}Cu_{9.6}Yb_2$, and suppress the formation of Al_2CuMg phase, which is consistent with the results of DSC curves.

Strength mechanisms

According to precious studies, the strengthening effect of La and Yb on the Al-4.6Cu-1.6Mg alloys should be mainly due to the refinement strengthening $\Delta\sigma_{HP}$, solid solution strengthening $\Delta\sigma_{SS}$ and second phase strengthening $\Delta\sigma_{SP}$ [51-53]. Thus, the yield strength of Al-4.6Cu-1.6Mg-0.6 (La+Yb) alloy can be estimated by the following equation.

$$\sigma_{YS} = \sigma_0 + \Delta\sigma_{HP} + \Delta\sigma_{SS} + \Delta\sigma_{SP}$$

Where σ_0 is the yield strength of the unmodified Al-4.6Cu-1.6Mg alloy and the value is 128.3 MPa. The grain refinement is attributed to comprehensive effect of heterogeneous nucleation and compositional undercooling. With the grain size decreases, the number of grain boundary increases, thus increasing the resistance to dislocation motion, which results in refinement strengthening. The refinement strengthening can be described by Hall-Petch equation.

$$\Delta\sigma_{HP} = K(d_1^{-1/2} - d_0^{-1/2})$$

Where K is the grain boundary strengthening coefficient ($150 \text{ MPa } \mu\text{m}^{1/2}$), d_1 and d_0 are denoted as the average grain size of Al-4.6Cu-1.6Mg-0.6 (La+Yb) alloy and Al-4.6Cu-1.6Mg alloy, respectively. Thus, the value of $\Delta\sigma_{HP}$ for the Al-4.6Cu-1.6Mg-0.6 (La+Yb) alloy is $\sim 24.9 \text{ MPa}$.

In this study, solute elements Cu and Mg are easy to form solid solution with Al solvent. And, Cu and Mg are the first and second solute elements, respectively. Based on above analysis, adding La and Yb into Al-4.6Cu-1.6Mg alloy can suppress the formation of Al_2CuMg , which leads to increasing the amount of solid solution of the alloying elements. Cu and Mg solute elements in the solid solutions result in lattice distortion, which increase the resistance to dislocation motion and makes it difficult to slip, thus increasing the strength of the alloys. The solid solution strengthening results from the interaction between solute atoms and dislocations, which can be expressed by the Fleischer equation [54].

$$\Delta\sigma_{SS} = MGb\varepsilon_{SS}^{3/2}(C_1^{1/2} - C_2^{1/2})$$

Where M is the Taylor factor (3.06), G is the shear modulus of the matrix (26.9 MPa for Al), b is the Burgers vector (0.286 nm), $\varepsilon = (r_x - r_{Al})/r_{Al}$ is the lattice strain causing by the difference in atomic radius between the solute and solvent elements, C_1 and C_2 are the concentration of solute elements in the Al-4.6Cu-1.6Mg-0.6(La+Yb) and Al-4.6Cu-1.6Mg alloys, respectively. According to SEM statistical analysis results, C_1 and C_2 for solute Cu are 1.6 wt.% and 1.2 wt.%, respectively. And, C_1 and C_2 for solute Mg are 1.2 wt.% and 0.8 wt.%, respectively. Table 8 presents the parameters for the solute atoms and theoretical contributions to the yield strength from these solute atoms [54]. Thus, the increase in yield strength provided from solid solution strengthening is calculated to be ~12.9 MPa as shown in Table 8.

Table 8. Parameters for the solute atoms and theoretical contributions to the yield strength from these solute atoms.

Elements	Yield strength addition (MPa wt.%-1)	C_1 (wt.%)	C_2 (wt.%)	Contribution to YS (MPa)
Cu	13.8	1.6	1.2	5.5
Mg	18.6	1.2	0.8	7.4

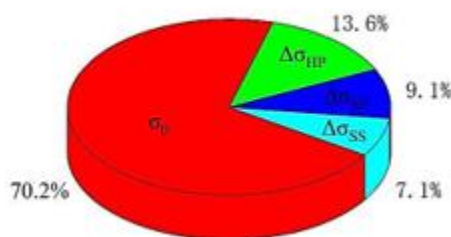
Some studies have indicated that the formation of Al-RE intermetallic could improve the mechanical properties of the aluminum alloys. These fine particles distributed in the matrix can hinder dislocations motion, thus increasing the strength of the alloys. This strengthening effect is known as the second phase strengthening. According to the interaction between the second phase and dislocations, the second phase strengthening mechanisms can be divided into Orowan cutting mechanism and Orowan bypassing mechanism. Generally, Orowan cutting mechanism works for the deformable particles (particles size less than 1 μm), while Orowan bypassing mechanism dominates for the non-deformable particles. As shown in Figure 6a, there are evident interactions between $\text{Al}_{7.4}\text{Cu}_{9.6}\text{Yb}_2$ particle and dislocations such as dislocation pile-up, indicating that $\text{Al}_{7.4}\text{Cu}_{9.6}\text{Yb}_2$ particle has strong structure stability. The $\text{Al}_{7.4}\text{Cu}_{9.6}\text{Yb}_2$ particle with 1.5 μm belongs to a non-deformable particle. Thus, Orowan bypassing mechanism can be used to calculate the contribution to yield strength from the second phase strengthening here, which can be expressed by [55].

$$\Delta\sigma_{SP} = \frac{2MGb}{1.18 \times 4\pi \times |\lambda - d|} \ln \frac{d}{2b}$$

Where r represents the mean particle radius, λ represents particle interspacing and can be take to be the lattice distance in parallel planes [56]. Thus, the yield strength increment attributed to the second phase strengthening is estimated to be ~16.7 MPa for Al-4.6Cu-1.6Mg-0.6 (La+Yb) alloy.

According to equation, the theoretical yield strength of Al-4.6Cu-1.6Mg-0.6 (La+Yb) alloy is ~182.8 MPa, which agrees well with the experimental value (181.2 MPa). Figure 12 displays the contribution ratios of different strengthening mechanisms to yield strength in Al-4.6Cu-1.6Mg-0.6 (La+Yb) alloy. It can be seen from Figure 12 that refinement strengthening is the main strengthening mechanism. This is because adding La and Yb into Al-4.6Cu-1.6Mg has evident grain refining effect, owing to synergistic effect of heterogeneous nucleation and compositional undercooling.

Figure 12. Contribution ratios of different strengthening mechanisms to yield strength in Al-4.6Cu-1.6Mg-0.6 (La+Yb) alloy.



CONCLUSIONS

The combined effect of La and Yb on the microstructure and mechanical properties of Al-4.6Cu-1.6Mg alloys was investigated in this work. The main conclusions can be drawn as follows.

1. Adding La and Yb into Al-4.6Cu-1.6Mg alloy can form $\text{Al}_6\text{Cu}_6\text{La}$ and $\text{Al}_{7.4}\text{Cu}_{9.6}\text{Yb}_2$ phases, while suppress the formation of Al_2CuMg phase at the same time.
2. Based on the calculated results of crystallographic relationships, the planar disregistry of $(220)_{\text{Al}_6\text{Cu}_6\text{La}}// (110)_{\text{Al}}$, $(110)_{\text{Al}_{7.4}\text{Cu}_{9.6}\text{Yb}_2} // (100)_{\text{Al}}$ and $(110)_{\text{Al}_{7.4}\text{Cu}_{9.6}\text{Yb}_2} // (111)_{\text{Al}}$ are less than 12%, indicating that $\text{Al}_6\text{Cu}_6\text{La}$ and $\text{Al}_{7.4}\text{Cu}_{9.6}\text{Yb}_2$ can serve as the effective heterogeneous nucleation substrates for $\alpha\text{-Al}$ and thus refine grains.
3. According to the calculated results of compositional undercooling criterion for different solute atoms, La and Yb atoms can obviously generate compositional undercooling during the solidification process, thus refining grains.
4. The yield strength, ultimate tensile strength and elongation of Al-4.6Cu-1.6Mg-0.6 (La+Yb) alloy are 181.2 MPa, 264.5 MPa and 6.3%, which are 41.2%, 45.1% and 75.0% higher than those of the unmodified alloy, respectively.
5. The strengthening mechanisms of Al-4.6Cu-1.6Mg-0.6 (La+Yb) alloy are attributed to the refinement strengthening, solid solution strengthening and second phase strengthening, in which the main strength mechanism comes from the refinement strengthening.

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AUTHORSHIP CONTRIBUTIONS

XLZ: Software, investigation, writing original draft, validation. LJY: Tensile Testing, investigation. ZJC: Investigation. HY: Conceptualization, review & editing, validation.

DATA AVAILABILITY

The data are available by the reasonable request.

DECLARATIONS

- **Conflict of interest:** The authors declare that they have no conflicts of interest in this work.
- **Ethical approval:** This study does not have ethical issues.

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