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Comparison of Optimistic and Pessimistic MTTF Bounds of NIASN with ABN

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ABSTRACT The reliability can be measured in terms of MTTF i.e. Mean Time To Failure. It is defined as expected time elapsed before some source is disconnected from some destination. In this paper Optimistic and Pessimistic MTTF Bounds of proposed Multistage Interconnection Network (MIN) New Irregular Augmented Shuffle Exchange Network (NIASN) have been evaluated and compared with existing similar class of MINs Augmented Baseline Network (ABN).

KEYWORDS Optimistic MTTF Bound, Pessimistic MTTF Bound, Network size, Fault Tolerance.

I. INTRODUCTION

The optimistic and pessimistic MTTF bounds are the markers of the reliability of the MIN. These values have been calculated by considering the series and parallel connections of the components in the MIN.

II. LITERATURE SURVEY

Different types of Multistage Interconnection Networks have been reviewed. The studied MINs have been categorized on the basis of their design and structure. The categories which have been studied include Fault-free and Fault-Tolerant MINs. On the basis of the mathematical and analytical models, the performance measures of these MINs have also been studied. The study helps to design new MINs with better performance.

III. ARCHITECTURE OF NIASN

The proposed MIN has been designed by using less number of SEs in the intermediate stages and with changed connection patterns in existing MIN Irregular Augmented Shuffle Exchange Network (IASN) Sadawarti et al. (2007) The proposed MIN consists of $k-1$ stages ($k=\log_2 N$). The network Comprises of two identical groups of switching elements (SEs), named as G^0 and G^1 . There are $N/2$ sources and $N/2$ destinations in each group. Both the groups are connected to the N inputs and N outputs. The inputs are connected through N multiplexers of 4:1 size, and the outputs are connected through the same number of demultiplexers of 1:2 size. The multiplexers and demultiplexers have been numbered as 0, 1, ---, $N/2$. In this network the switches are of size $2*2$ in all the stages except the first stage where the switches are of size $3*3$. The NIASN network of size $N*N$ has $(2*k)$ no. of switches of size $3*3$ and $[(2*k) +3]$ number of switches of size $2*2$. Each source is connected to one switching element in each

group with the help of multiplexers. The multiplexers and demultiplexers have been given the numbers as 0, 1, ---, $N/2-1$. The switches in the first stage have been assigned the numbers from 0, 1, ---, $N/2-1$, connected to each other through links called as auxiliary links. The auxiliary links are used when the SE in the next stage is busy or faulty. This makes the network more Fault-Tolerant and reliable. The switches in the middle stage have been given the number as $N/2, --, N/2+2$. Like wise the switches in the last stage are identified with the numbers from $N/2+3, ----, N/2+10$.

IV. OPTIMISTIC AND PESSIMISTIC MTTF BOUNDS OF NIASN AND TRIANGLE MIN

The optimistic and pessimistic MTTF bounds have been calculated by considering the series and parallel connections of the components in the MIN.

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Optimistic MTTF Bound

The network is operational if the critical set of switches is operational. The critical set is the set of k SEs, each from different module such that a failure occurs if all k SEs are faulty simultaneously. The NIASN network is in operation as long as one of the two multiplexers attached to the source in any of the groups is operational. The block diagram of this bound has been shown in Fig 2.

The functions of the stages in the network are given below

$$f1 = [1 - \{1 - e^{-\lambda_m t}\}^2]^{N/2}$$

$$f2 = [1 - \{1 - e^{-\lambda_2 t}\}^2]^{(N/4-1)+(N/8 * + \dots - 1)}$$

$$f3 = [1 - \{1 - e^{-\lambda_{2d} t}\}^2]^{N/4}$$

The expression for optimistic Bound Reliability is

$$R_{Optimistic}(t) = [1 - (1 - e^{-\lambda_m t})^2]^{N/2} [1 - (1 - e^{-\lambda_2 t})^2]^{(N/4-1)+ N/8 * + \dots - 1} [1 - (1 - e^{-\lambda_{2d} t})^2]^{N/4}$$

$$MTTF = \int_0^{\infty} R_{Optimistic}(t) dt$$

The optimistic MTTF bound of the proposed NIASN network has been evaluated. Table 1 shows the values of this MTTF analysis.

The equations of Optimistic MTTF Bound of the Triangle Network are

$$f1 = [1 - \{1 - e^{-\lambda_m t}\}^2]^{N/4}$$

$$f2 = [1 - \{1 - e^{-\lambda_3 t}\}^2]^{(N/8-2)+(N/8+N/16)}$$

$$f3 = [1 - \{1 - e^{-\lambda_{2d} t}\}^2]^{N/4}$$

The Optimistic MTTF Bound is calculated as

$$R_{UB-Triangle} = \int_0^{\infty} f1 * f2 * f3(t) dt$$

The Table 2 shows the values of the Optimistic MTTF Bound of Triangle Network

PESSIMISTIC MTTF BOUND

In the pessimistic MTTF Bound analysis, the input side SEs and their corresponding multiplexers are considered as a series system and failure of any component leads to the failure of all three. The functions of the stages in the network are given below

$$f1 = [1 - \{1 - e^{-\lambda_{3m} t}\}^2]^{N/4}$$

$$f2 = [1 - \{1 - e^{-\lambda_2 t}\}^2]^{(N/8 * + \dots - 1)}$$

$$f3 = [1 - \{1 - e^{-\lambda_{2d} t}\}^2]^{N/4+1}$$

The expression for pessimistic MTTF Reliability is

$$R_{Pessimistic}(t) = [1 - (1 - e^{-\lambda_{3m} t})^2]^{N/4} [1 - (1 - e^{-\lambda_2 t})^2]^{N/8 * + \dots - 1} [1 - (1 - e^{-\lambda_{2d} t})^2]^{N/4 + 1}$$

$$MTTF = \int_0^{\infty} R_{pessimistic}(t) dt$$

The reliability block diagram for the pessimistic MTTF bound has been shown in Fig. 3.

Table 3 shows the values of the pessimistic MTTF bound of the proposed NIASN network.

If two multiplexers are grouped with each switch in the source and considered as a series system, then Pessimistic MTTF Bound of Triangle MIN can be equated as below

The functions of the stages in the Triangle MIN are given below

$$f1 = [1 - \{1 - e^{-\lambda_{3m} t}\}^2]^{N/2}$$

$$f2 = [1 - \{1 - e^{-\lambda_3 t}\}^2]^{(N/4+2)}$$

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$$f3 = [1 - \{1 - e^{-\lambda_{2d} t}\}^2]^{N/2}$$

The Pessimistic MTTF expression is calculated as

$$R_{LB-Triangle} = \int_0^{\infty} f1 * f2 * f3(t) dt$$

Table 4, shows the values of the Pessimistic MTTF Bound of Triangle Network.

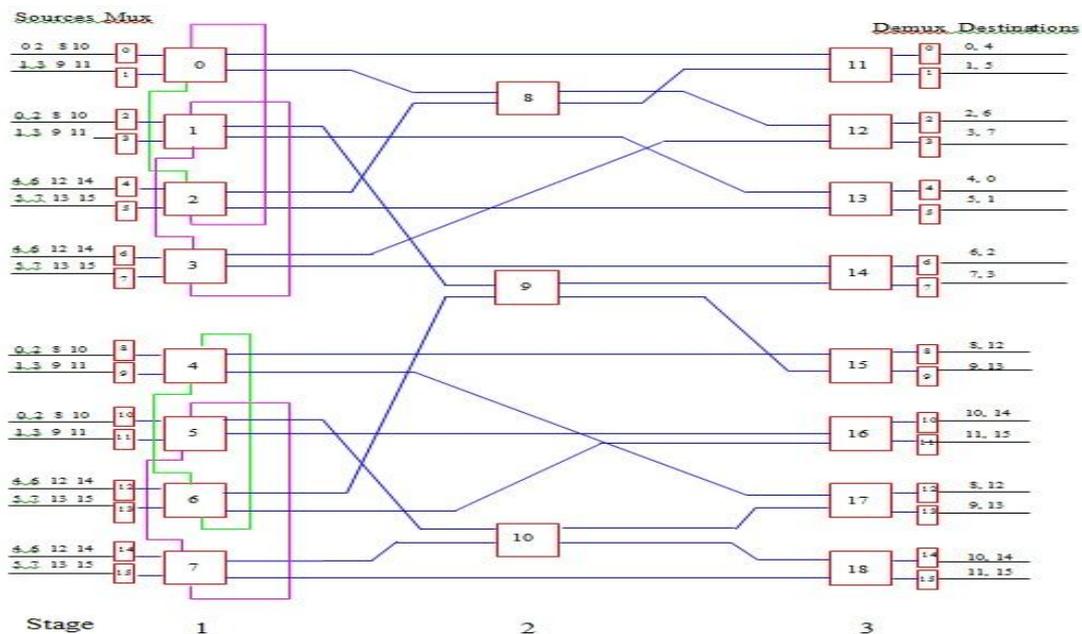


Fig 1: Design of NIASN of size 16 * 16

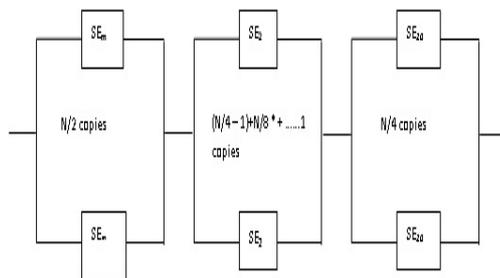


Fig 2: Block diagramme of Optimistic MTTF Bound of NIASN

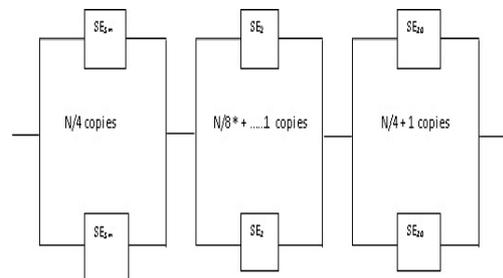


Fig 3: Block diagramme of Pessimistic MTTF Bound of NIASN

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Table 1: Optimistic MTTF Bound of NIASN

Network Size	16*16	32*32	64*64	128*128	256*256	512*512	1024*1024
Optimistic MTTF bound	215548	145114	99013	68242	47415	33516	26428

Table 2: Optimistic MTTF Bound of Triangle Network

Size N*N	Upper Bound
16*16	190591.34
32*32	117404.91
64*64	77106.12
128*128	52251.53
256*256	36252.73
512*512	27335.08
1024*1024	25111.5

Table 3: Pessimistic MTTF Bound of NIASN

Network Size	16*16	32*32	64*64	128*128	256*256	512*512	1024*1024
Pessimistic MTTF Bound	100810	69750	48247	33971	26603	25052	22040

Table 4: Pessimistic MTTF Bound of Triangle Network

Size N*N	Lower Bound
16*16	98440.49
32*32	69120.2
64*64	48386.57
128*128	34253.58
256*256	26713.97
512*512	25060.09
1024*1024	25000.07

V. CONCLUSION

The NIASN MIN shows significant improvement in MTTF Bounds as compared to similar class of Network i.e. Triangle MIN. It is clear that the NIASN MIN is reliable for small size of network and is comparable to Triangle MIN as the network size grows.

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BIOGRAPHY



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