



Five Leg Z-Source Inverter Feeding Two Independent Loads Simultaneously

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ABSTRACT: This paper presents control methods for controlling two independent loads simultaneously by using five-leg Z-Source Inverter and High-Performance Z-Source Inverter. In recent years, five-leg inverter has been proposed. This inverter can control two three-phase loads independently at a time, this inverter has five legs, each leg consists of two switching devices and total ten switching devices. A and B phases of both loads are connected in each leg respectively whereas C phase of both loads is connected in common leg. In five-leg inverter, C phase of the loads are connected in the common leg, it causes difference from a switching pattern of C phase in two loads. For this reason, the modulation methods of a three leg inverter can't be used for the five-leg inverter. Many modulation methods for the five-leg inverter have been proposed, but Voltage Utility Factor is 50% in these methods. This paper proposes a novel structure for Z-source five-leg inverter. First, the construction of five-leg inverter, Z-source five-leg inverter is introduced and then PWM modulation methods for the Z-source five-leg inverter are elaborated. Consequently, it is shown with Z-source one can improve Voltage Utility Factor in five-leg inverter. In the end, the validity of the method is verified by simulations

KEYWORDS: Five-Leg Inverter (FLI); Z-source FLI; High Performance Z-source FLI; PWM techniques

I. INTRODUCTION

In electric trains, electric vehicles and some other industry applications, multiple drive system is needed, in which two or more loads operate in parallel. Generally in multiple drive system, one voltage source inverter (VSI) is needed to feed one three phase load. Therefore, a large number of power electronic devices are required, which means a complex structure and high cost. In recent years, a lot of researches have been conducted to reduce the number of switches. Due to wide spread uses of three-phase loads in industrial applications, control of these loads are a very important thing. In many cases two or many loads need to be controlled independently. Traditionally, often two methods are employed for controlling two three-phase loads. The first method is the use of two inverters separately for each of the loads. This method needs twelve semiconductor switches to control the loads resulting in higher cost and more complexity for the control systems. The second method is the use of only one inverter for two loads. In this manner, two loads are connected in parallel with a single inverter and there is no independent control over each of the loads. The above two methods have some disadvantages i.e., in first method the space requirement is more, high switching losses etc., in second method if fault occurred on any one load total system is completely shut down. The human beings are always looking for ways to control the loads with minimum cost, maximum efficiency and minimum dimensions of the control system. To improve and simplify the control system, five-leg inverter (FLI) has been proposed [1, 5]. FLI is a single inverter that can drive two loads independently. For FLI the PWM techniques used for three-phase or three-leg inverter should not be applied since in FLI inverter one leg is common for both loads. In FLI, since the DC voltage source is shared between the two loads, the voltage across each load is less in the case of a three-leg inverter. In the previous papers different PWM methods Dual voltage modulation, Inverse table method, Modulation block method, two arm modulation method, Double zero sequence injection method etc., are proposed in these methods the voltage utility factor is less than 50% and also control two loads independently at a time is not possible. Therefore, a larger DC voltage source is needed in this method which increases system cost and size. In this paper this is improved by using Z-source structure. In this paper in first section, structure of proposed Z-source inverter is expressed. In second section, the PWM methods for Z-source FLI are illustrated. In third section, structure of the high performance Z-source in FLI for improving the Voltage stability is described. In fourth section, simulations are performed to verify the validity of the statements.

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II. ARRANGEMENT OF THE FIVE-LEG INVERTER

Fig. 1 shows the structure of the FLI. This inverter consists of five legs; each leg consists of two series switches and in the total of 10 semiconductor switches. As can be seen in Fig. 1, C-phase of two loads is connected in a common leg while the other two phases are connected in separate legs. Pulses for this inverter are generated with PWM method; reference signal for each leg is given by (1). In (1) a reference signal to C-phase is zero. This implies that the signal can be considered zero for the common leg in this inverter. In this manner, the Voltage Utility Factor (VUF) for each load can be calculated to be 86.6% which means that the maximum voltage for each load is 86.6% of the DC voltage link. This requires a larger source.

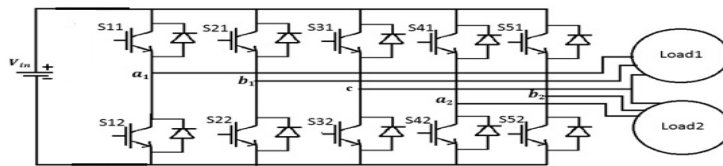


Figure1. Five-Leg Inverter (FLI)

$$V_{a1} = V_m \sin(\omega_1 t) \tag{1.1}$$

$$V_{a2} = V_m \sin(\omega_1 t + \phi) \tag{1.2}$$

$$V_{b1} = V_m \sin(\omega_2 t) \tag{1.3}$$

$$V_{b2} = V_m \sin(\omega_2 t + \phi) \tag{1.4}$$

$$V_c = 0 \tag{1.5}$$

The voltage utility factor (VUF) is defined as

$$VUF(\%) = \frac{\sqrt{3} \cdot \frac{1}{2} \cdot a_{max} \cdot V_{in}}{V_{in}} \tag{2}$$

Where a_{max} is the maximum modulation index

In the functioning of switches, value 1 for switch is in ON state and value 0 for switch is in OFF state are considered.

If S refers to switches:

$$S_{1i} + S_{2i} + S_{3i} = 2 \tag{3}$$

Where i represents load, $i = 1, 2$

The switching restriction in (3) prevents short-circuiting in DC voltage source.

III. ARRANGEMENT OF THE Z-SOURCE FIVE-LEG INVERTER

To improve output voltage for each load, Z-source FLI is proposed. In this inverter Z-network is placed between the FLI and a DC voltage source. By controlling the shoot-through duty ratio of the short circuit mode, this inverter is able to produce any AC voltage in its output. When a rectifier is used as the input, Z-source FLI can reduce current harmonics, improve reliability and increase output voltage range. In this paper, two different structures, normal Z-source and high performance Z-source in FLI are studied. Structure of the normal Z-source is shown in Figure2.

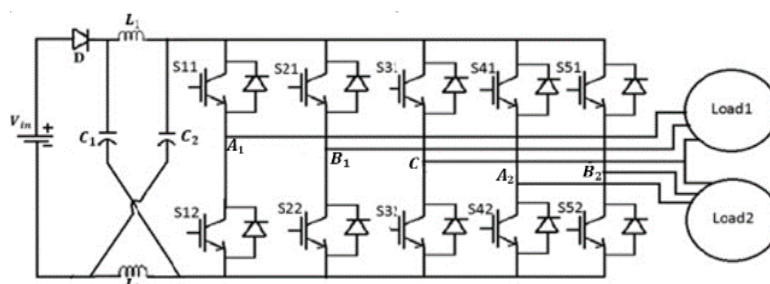


Figure2. Z-source Five-Leg Inverter



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In this architecture, the Z-network is used to connect the DC source and the FLI. The DC source can be a battery, a diode rectifier or a Thyristor converter. For the traditional VSI, both switches of any phase leg cannot be gated on simultaneously otherwise a short circuit (shoot through) would occur and destroy the circuit. But in Z-source inverter, by switching ON the two switches in one leg, the DC voltage can be boosted while the shoot-through state can no longer destroy the inverter. In this method, the switching frequency viewed from the Z-source network is ten times the switching frequency of the main inverter, which greatly reduces the required inductance of the Z-source network. The Z-source network is assumed to be symmetrical network by assuming that the inductors and capacitors have same value. This will reduce the complexity of calculations. With assuming that the T_0 is shoot-through time and T is duty cycle, the peak dc-link voltage across the five leg inverter bridge can be written as:

$$V'_{dc} = \frac{T}{T_1 - T_0} V_{in} = B * V_{in} \quad (4)$$

$$T = T_0 + T_1 \quad (5)$$

In this equation:

$$B = \frac{T}{T_1 - T_0} = \frac{1}{1 - 2\frac{T_0}{T}} \quad (6)$$

Where, B is the boost factor. Boost factor is greater than one. This leads to increase in the peak dc-link voltage across the five leg inverter bridge. Peak output phase voltage for each load can be written as:

$$V'_{ac} = M * B * \frac{V_{in}}{2} \quad (7)$$

Equation (7) shows that by changing the boost factor the output voltage of each load can be changed. Boost factor (B) can be controlled by controlling the duty cycle of short circuit mode. The shoot through state does not affect the PWM control of the five leg inverter, because this state produces the same zero voltage to the load terminal. The available shoot through period is controlled by adjusting the modulation index (M).

IV. MODULATION OF THE Z-SOURCE FIVE-LEG INVERTER

In the before section as we discussed, Z-source FLI utilizes short circuit state or shoot-through state to boost DC link voltage, whereas the conventional five leg inverters do not allow the use of shoot-through state. Therefore, the traditional control methods used for regular five leg inverters should be changed. In this section, three PWM methods for controlling Z-source five leg inverters are explained. These methods include simple-boost PWM, maximum-boost PWM and constant-boost PWM.

1. Simple-Boost PWM of the Z-source Five-Leg Inverter:

In conventional PWM method, four line signals and one zero signal are produced as the reference signals. In Simple-boost PWM methods, like the conventional PWM, the switching signals are generated by comparing five reference waves with the carrier wave. The only difference is that for Z-source inverter modulation this method utilizes two dc signals V_1 and V_2 for providing short circuit states. These dc signals are equal to or greater than the maximum value of the sinusoidal reference signals. When a triangular high frequency carrier signal is greater than V_1 or is smaller than V_2 , all switches are turned off and the circuit turns into shoot-through state as illustrated in Fig. 3. In this method, boost factor can be written as:

$$\frac{T_0}{T} = 1 - V_1 \quad (8)$$

$$B = \frac{1}{1 - 2\frac{T_0}{T}} = \frac{1}{2V_1 - 1} = \frac{1}{1 - 2D_0} \quad (9)$$

D_0 = shoot-through duty ratio

From this equation it is observed that by decreasing V_1 , the value of B can be increased. However, it should be noted that V_1 cannot be smaller than M otherwise it would interfere with a reference wave and convert an active vector to a zero vector.

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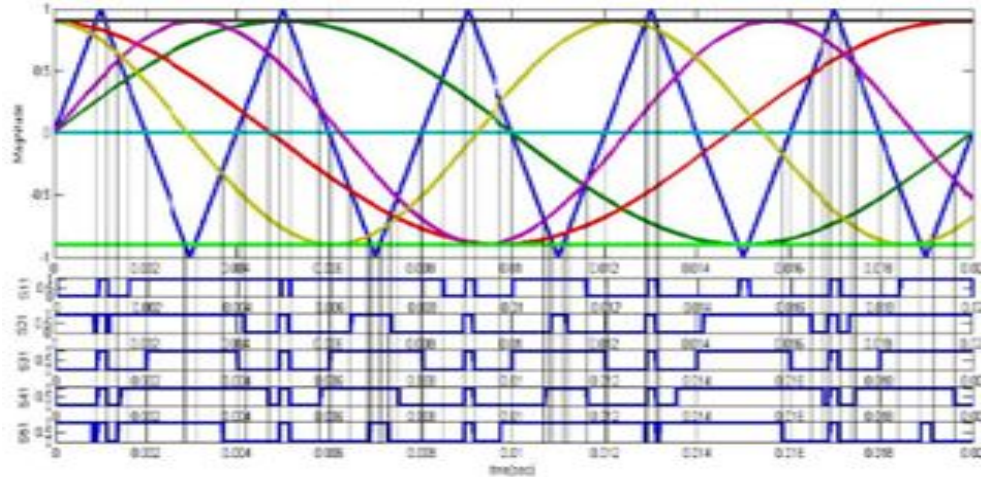


Figure3. Simple-Boost Method

2. Maximum-Boost PWM of the Z-source Five-Leg Inverter:

To use the maximum possible short circuit states, another modulation method can be used which is called maximum-boost PWM method [7]. Like in normal PWM method when the triangular carrier wave is greater than the maximum value of the sinusoidal references or smaller than the minimum value of the sinusoidal references, all switches are turned into active state. There are five references among these with only four sinusoidal reference signals, short circuit time is determined. As can be seen in Fig. 4, therefore, the shoot through duty cycle varies in each cycle. This increases voltage ripple and in some cases may result in voltage instability. In this method, except for the zero reference in common leg all zero vectors are converted to short circuit state. However, this method produces current ripple of a low frequency that is associated with the output frequency in the inductor current and the capacitor voltage. This will cause a higher requirement of the passive dc components when the output frequency becomes very low. Therefore, the maximum boost control is suitable for applications that have a fixed or relatively high output frequency.

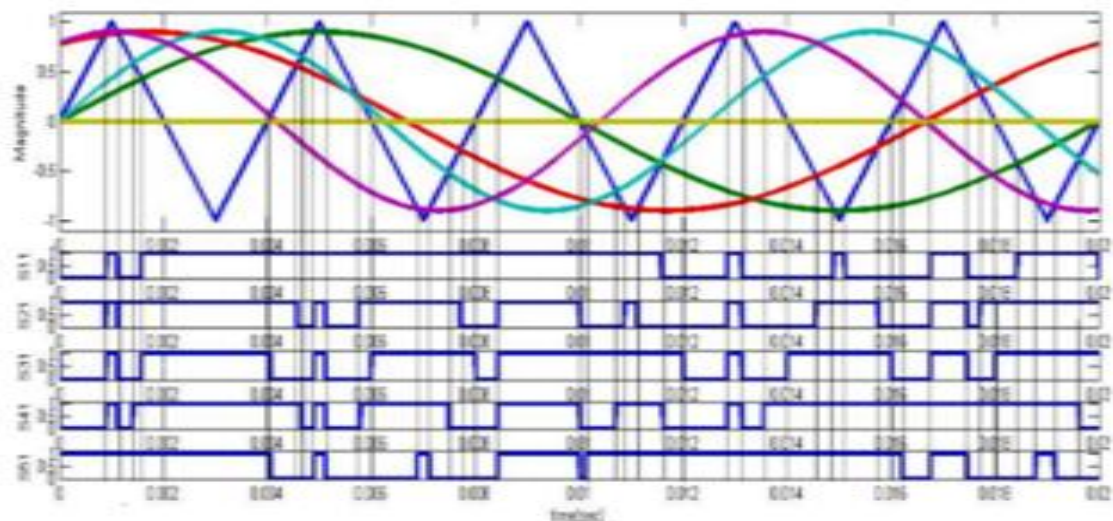


Figure4. Maximum-Boost Method

3. Constant-Boost PWM of the Z-source Five-Leg Inverter:

In order to reduce the size and cost of the Z-source network, we need to eliminate the low-frequency current ripple by using a constant shoot-through duty ratio. At the same time, a greater voltage boost for any given modulation index is desired to reduce the voltage stress across the switches.

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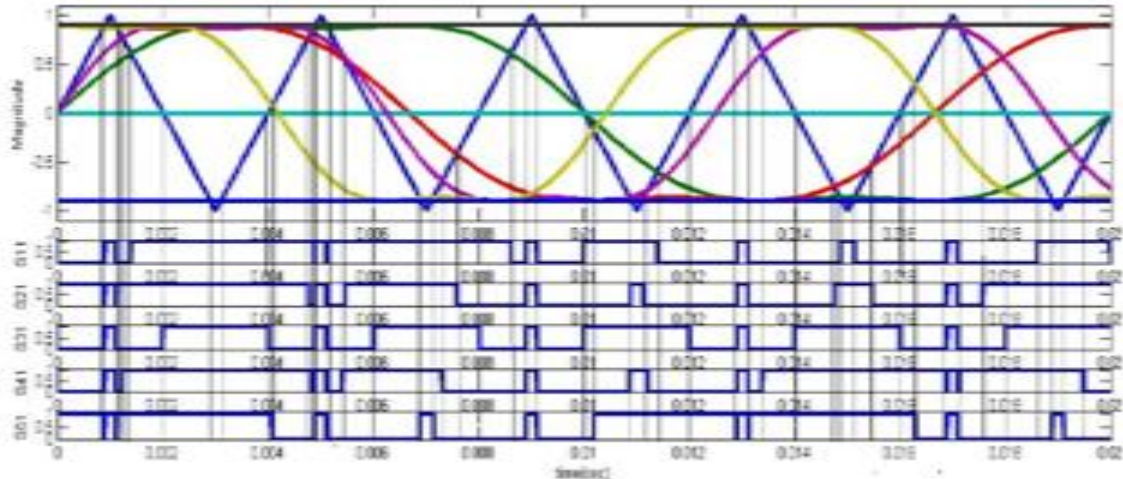


Figure5: Third harmonic injected method

Third harmonic injection method [8] is commonly used to increase the range of modulation index (M) so as to increase system voltage gain range. There are seven modulation curves in this control method: five reference signals, and two shoot-through dc signals, v_p and v_n . A third harmonic component with 1/6th of the fundamental component is injected to the voltage references. When the carrier triangle wave is greater than the upper shoot-through dc signal, v_p , or lower than the lower shoot-through dc signal, v_n , the inverter is turned to a shoot-through zero state. In between, the inverter switches in the same way as in traditional carrier-based PWM control. The sketch map of maximum constant boost control is shown in Figure(5). This method achieves maximum boost while keeping the shoot-through duty ratio always constant; thus it results in low line frequency current ripple through the inductors. With this method, the inverter can buck and boost the voltage from zero to any desired values smoothly within the limit of the device voltage. This method is especially suitable for low-frequency applications, since it minimizes the Z-source network. Table I shows the summary of all relations for different PWM control methods.

Table I
Summary of different PWM control methods expressions

Parameter	Different PWM control methods		
	Simple boost	Maximum boost	Third-harmonic
D_o	$1 - M$	$\frac{2\Pi - 3\sqrt{3}M}{2\Pi}$	$\frac{2 - \sqrt{3}M}{2}$
B	$\frac{1}{2M - 1}$	$\frac{\Pi}{3\sqrt{3}M - \Pi}$	$\frac{1}{\sqrt{3}M - 1}$
G	$\frac{M}{2M - 1}$	$\frac{\Pi M}{3\sqrt{3}M - \Pi}$	$\frac{M}{\sqrt{3}M - 1}$
M_{max}	$\frac{G}{2G - 1}$	$\frac{\Pi G}{3\sqrt{3}G - \Pi}$	$\frac{G}{\sqrt{3}G - 1}$
V_s	$(2G - 1) V_{in}$	$\frac{3\sqrt{3}G - \Pi}{\Pi} V_{in}$	$(\sqrt{3}G - 1) V_{in}$

The above table shows that the comparisons of different PWM methods of various parameters. Among these methods Maximum-boost method produces more voltage but it has some limitations discussed above and more significantly third-Harmonic or constant-boost PWM method is used.

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V.HIGH PERFORMANCE Z-SOURCE FIVE-LEG INVERTER

The Z-source inverter operating with small inductance has some limitations as following:

1. When the inductance of the z-network is small, the inductor current can become high ripple or even discontinuous.
2. The Z-source network inductor has the limited value to guarantee the input current $i_{in} > 0$. In some applications, the inductance should be minimized in order to reduce cost, size, and weight. The design of Z-source network inductor and system control become very complex, and the output voltage becomes uncontrollable with small inductor even operate in full load.
3. Light-load operation is the problem in Z-source inverter. The dc-link voltage is increasing infinitely when the system operated with light-load, which causes voltage-drops at the dc-link. The voltage will be uncontrollable and the system is unstable.

To overcome these limitations, high-performance Z-source structure is employed [9, 10]. While maintaining all the benefits of conventional Z-source inverters, this structure can be used for a wide range of load changes (even no-load mode), operates with smaller inductors in Z-source network, eliminate the possibility of the dc-link voltage drops, and simplify the inductor design and system control. The structure of a high-performance Z-source inverter is shown in figure 6.

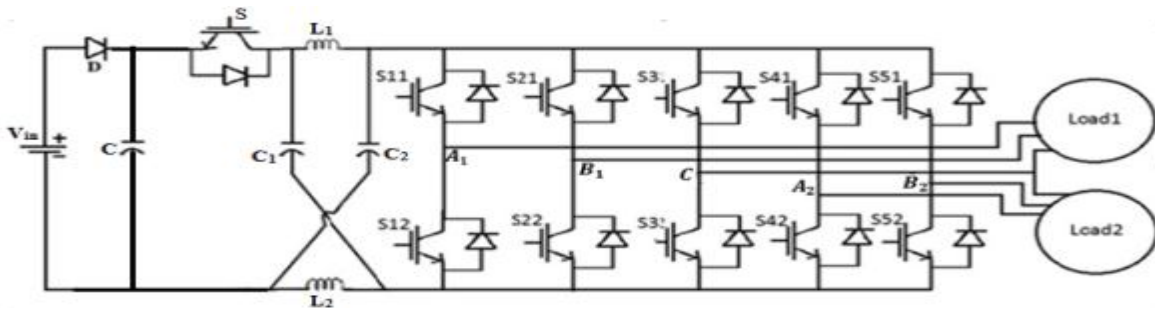


Figure6: High-Performance Z- Source Five-Leg Inverter

The high-performance Z-source inverter has two modes of operations and is explained below. In this method the peak value of ac output phase voltage for each load can be written as:

$$V'_{ac} = \frac{M * V_{in}}{2(1-2D_0)} \tag{10}$$

The voltage across each Z-source capacitor is

$$V_{C1} = V_{C2} = \frac{1-D_0}{1-2D_0} V_{in} \tag{11}$$

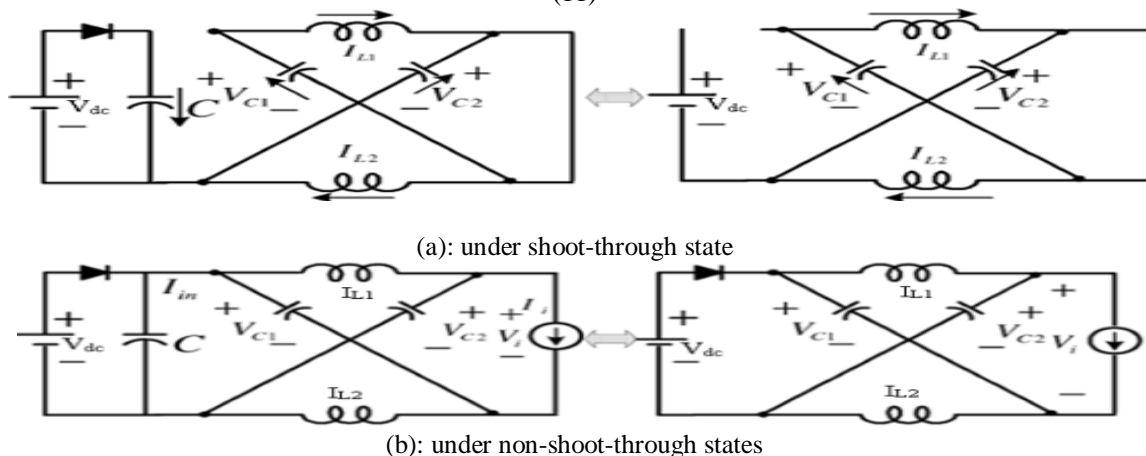


Fig7: operation modes of high-performance z-source inverter

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The switch 's' is controlled in such a way that it is in OFF state when inverter is in shoot-through state and switch is in ON state when inverter is in non-shoot through state. In this structure, the gate signal for switch 's' can be generated with both modulation methods of simple-boost and maximum-boost. The pulses for switch 's' is generated by using simple boost method shown in Fig.8.

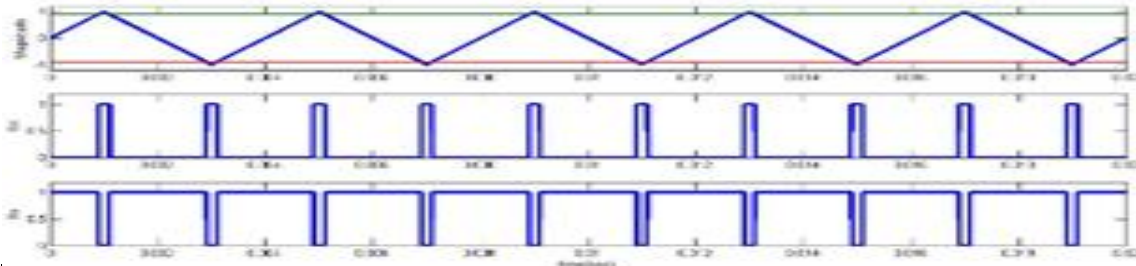


Figure8: pulses of switch 's' with simple boost method

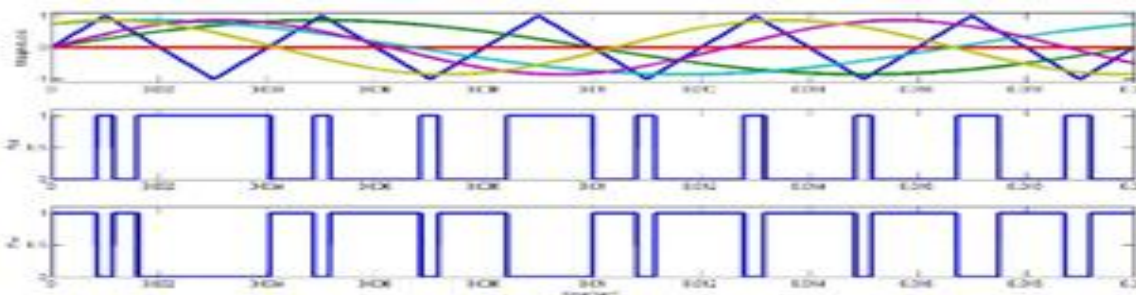


Figure9: pulses of switch 's' with maximum-Boost method

VI.SIMULATION RESULTS

To verify the validity of these methods as explained above various simulations are performed. The simulation parameters are given in Table II. In order to show that the Z-source Five-Leg inverter is able to control each load independently, the load frequencies are assumed to be different.

TABLE II
PARAMETERS OF SIMULATION

DC Voltage source	150 V
Carrier frequency	10 kHz
Load resistance	11 Ω
Load inductance	20mH
Frequency load 1	50 Hz
Frequency load 2	80 Hz
Z- source capacitor	500μF
Z- source inductor	500mH

The simulation results of five-leg z-source inverter with simple-boost modulation method are shown in figure 10. The impedance or Z- network boost this DC voltage to 215V (peak) for Modulation index of 0.85. It can be seen that the voltage stress on the switches is increased. For example, when switch S_{11} is OFF, the voltage across this switch increases to about 215 volts. According to these results, the Z-source five leg-Inverter with the simple boost modulation method can independently control the frequency for each of two loads. But in this method all the shoot-through states are not fully utilized and boosted voltage is also relatively low.

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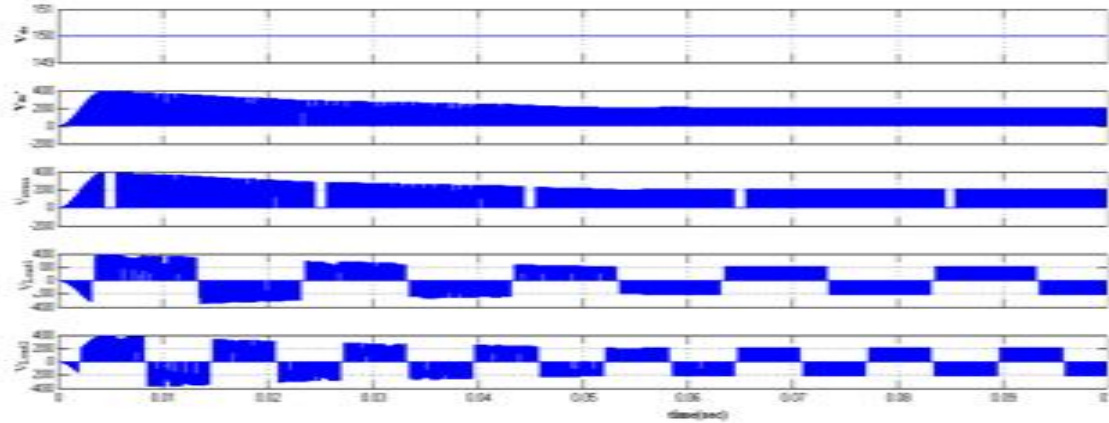


Figure10: Simulation Results for Simple-Boost Modulation

At the same condition, to increase the inverter DC link voltage, maximum boost method is employed. With the same parameters used for the simple-boost method, DC link voltage is unstable. The reason is that instead of three reference waves, two waves are producing short circuit signals for each load and zero reference does not have any effect on short circuit signals. This causes the increase in the short circuit time. To compensate this and stabilize the system, a limit for short-circuit time is considered. In this simulation, a maximum short-circuit time of 20% was assumed in each half-period. Simulation results are shown in Figure 11.

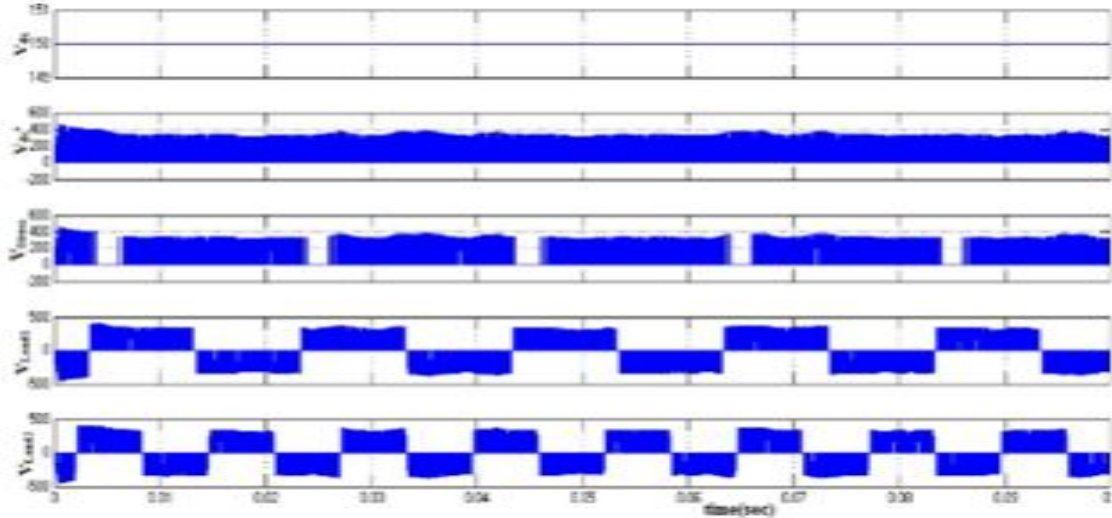


Figure11: DC Voltage in Maximum Boost Modulation (20%)

In Figure 11, with DC input Voltage equal 150V, DC voltage of Z-source network is boosted to a value of around 340V which is more than twice that of the input voltage. Also, like in the previous method, the voltage stress on the switches is increased. For example, when switch S_{11} is OFF, voltage S_{11} increases to about 340V. In this figure, turn-on time of the switches is increased which results in more conduction loss in the switches. According to these results, the Z-source FLI utilizing the maximum boost modulation method can independently control the frequency for each of two loads.

In the above two methods the voltage across the switch is more this results in high cost because we require high rating switches. So to decrease voltage stress and to increase the modulation index range another method is used i.e., Third Harmonic injected PWM method. The simulation results are shown in figure 12. With DC input voltage of 150V is boosted to around 315V.

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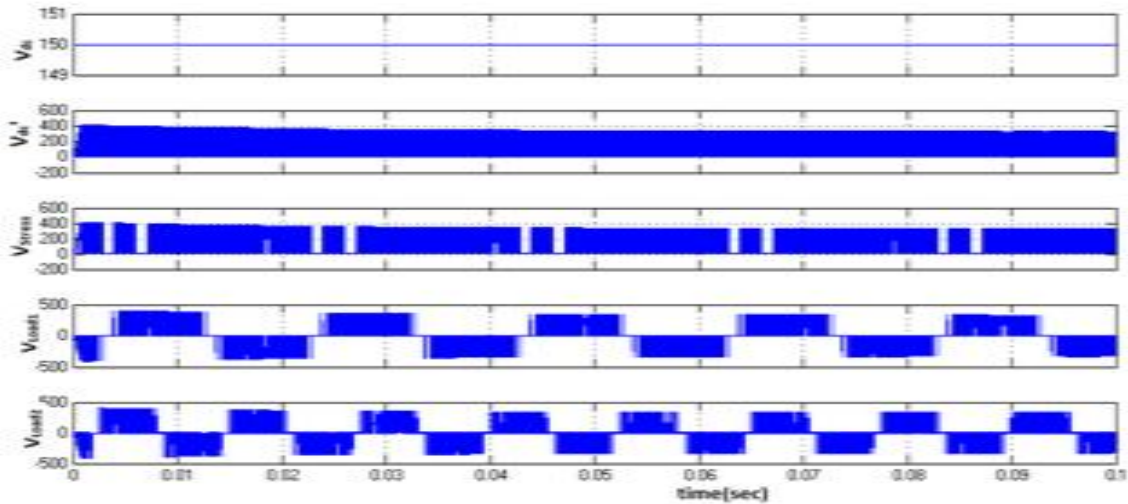


Figure12: Simulation results of Third Harmonic Injected modulation

TABLE III
Simulation results summary of Z-Source Five-Leg Inverter for different PWM control methods

Control method	FLI	Simple-boost method	Max.-boost method	Third-harmonic method
$V_{LL(RMS)}$	78.02	110.2	143.4	121.3
$I_L(RMS)$	2.05	2.43	3.93	3.163

At the same condition, to increase the stability, high-performance method is used. Simulations for high-performance Z-source FLI are performed with simple boost and maximum-boost modulation methods. Simulation results for simple-boost are shown in Figure 13. Again, with DC input voltage equal to 150V, DC voltage of Z-source network is increased to about 280V, but as it is clear in Fig. 13, the voltage ripple is decreased in this case. According to these results, the high performance Z-source five-leg inverter with the simple boost modulation method can independently control the frequency for each of two loads. At the same condition, to increase the inverter DC link voltage, maximum boost modulation method in high-performance Z-source five leg inverter is used. Simulation results are shown in Figure 14. In this figure, with DC input voltage equal to 150V, DC voltage Z-source network is boosted to 300V and system becomes stable.

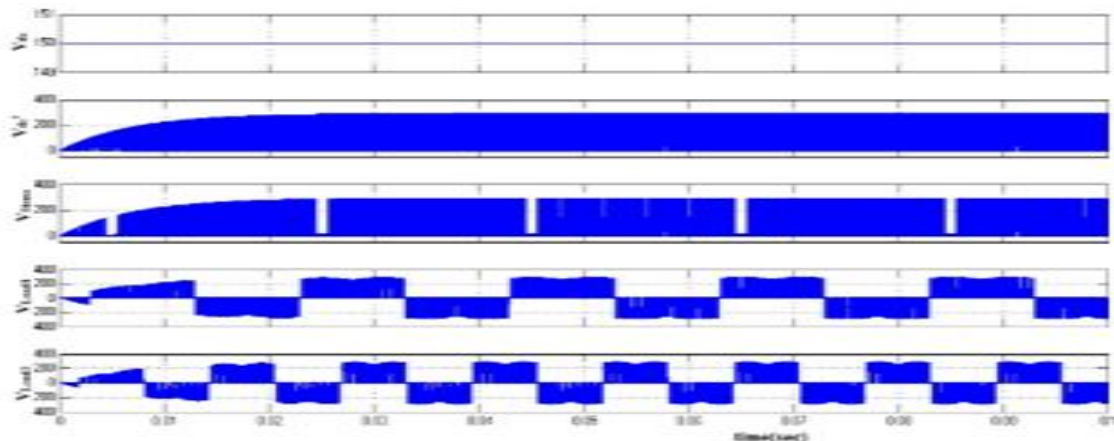


Figure13. High Performance with Simple-Boost Modulation

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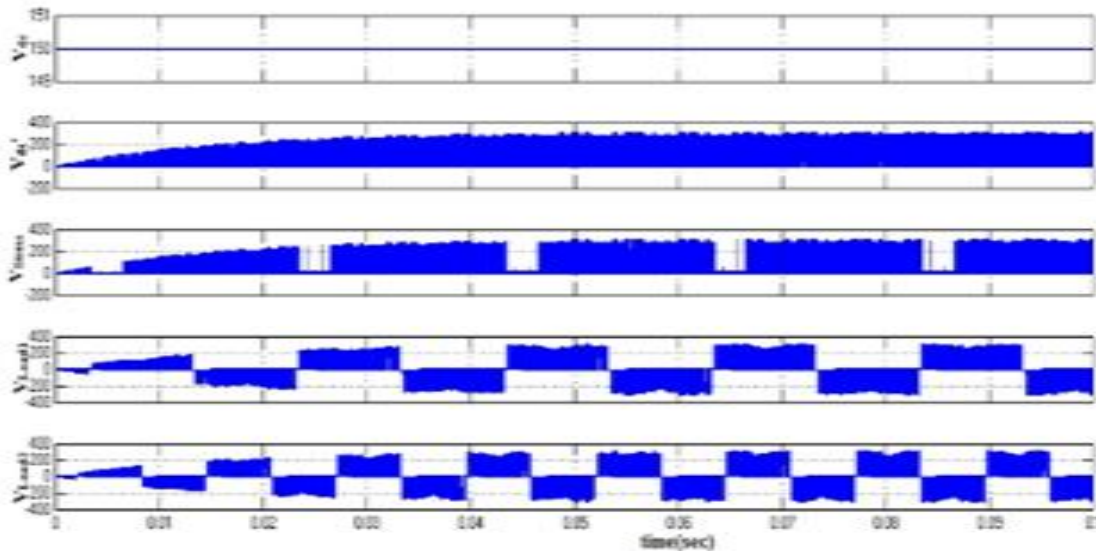


Figure14. High Performance with Maximum-Boost Modulation

The following figure15 shows that the comparison of rms line voltage versus modulation index (M) for different methods of Five-Leg inverter. Among these methods Maximum-Boost PWM method produces the highest output voltage because in this method all zero states are utilized fully.

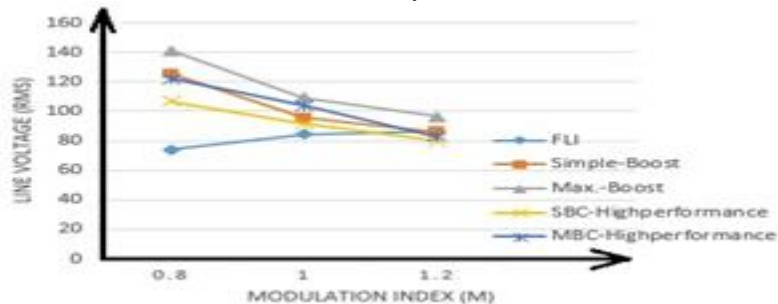


Figure15: Line rms voltage (Volts) Vs modulation index (M)

Total Harmonic Distortion is an important parameter to determine the quality of a wave form. In this section, the value of THD is calculated for output load current. Figure16 shows the value of THD for different methods. As can be seen in this figure, the FLI has the lowest THD while maximum-boost modulation in Z-source FLI results in the highest THD.

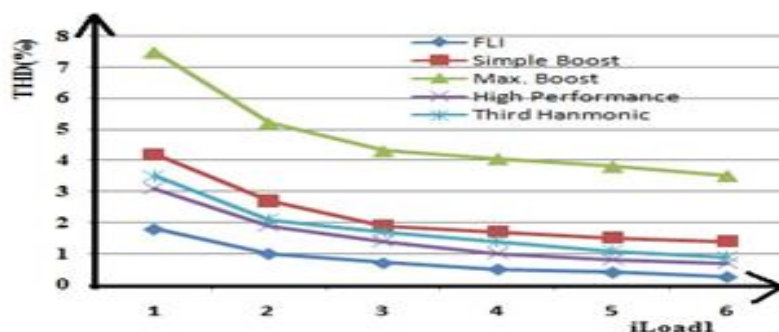


Figure16: Total Harmonic Distortion for different methods



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VII.CONCLUSION

This paper presents control methods for controlling two independent loads simultaneously by using Five-leg Z-Source inverter and High-Performance Z-Source Inverter. The Z-Source Five-Leg inverter to overcome the limitations of the traditional five-leg inverter, however it has some limitations when operating at light-loads or with small Z-source network inductor. To overcome these limitations High-Performance Z-source inverter is proposed. Moreover it also has lower harmonics, less stress across the switches, removes DC link voltage drops, simplifies the design of inductor and stability can be improved. Finally, simulation results verified for the validity of various control methods.

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