



Implementation of High Speed Signed Multiplier Using Compressor

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ABSTRACT: Multipliers play an important role in today's digital signal processing and various other applications. With advances in technology, many researchers have tried and are trying to design multipliers which offer either of the following design targets – high speed, low power consumption, regularity of layout and hence less area for compact VLSI implementation. This work is based on one of the ancient Vedic algorithms (sutras) called Urdhava tiryakbhyam method. These sutras are meant for faster calculation. Though faster when implemented in hardware, it consumes less area. This paper presents a technique to modify the architecture of the Urdhava Tiryakbhyam hardware by using 3_2compressor in order to reduce area and delay to improve overall performance. The coding is done for 16 bit (Q15format), 32 bit (Q31format) and 64 bit (Q63 format) fixed point Q-format by using Verilog HDL and Synthesized by using Xilinx ISE version 9.2i. The performance is compared in terms of area, delay with earlier existing architecture of Urdhava Tiryakbhyam method. The proposed work (compressor based Urdhava Tiryakbhyam method) shows improvements in terms of area and time delay.

KEYWORDS: Compressor, Fixed point format, Q-format, Urdhava Tiryakbhyam.

I.INTRODUCTION

Vedic Mathematics is the ancient system of mathematics which was rediscovered early last century by Sri Bharati Krishna Tirthaji (1884-1960) [1]. The Sanskrit word “Veda” means “knowledge”. He organized and classified the whole of Vedic Mathematics into 16 formulae or also called as sutras. These formulae form the backbone of Vedic mathematics. Great amount of research has been done all these years to implement algorithms of Vedic mathematics on processors. Hence our focus in this work is to develop optimized hardware modules for multiplication operation. Considering fixed point representation, 16 bit Q15 format, 32 bit Q31 format and 64 bit Q63 formats are provide required precision for most of the digital signal processing applications and best suited for implementation on processors. In this paper we propose the implementation of fixed point Q-format [6] high speed multiplier using Urdhava Tiryakbhyam method of Vedic mathematics. Further we have also implemented multipliers using compressor based Urdhava Tiryakbhyam method.

The paper is organized into VI sections. Section II explains fixed point arithmetic III Urdhava Tiryakbhyam method of Vedic mathematics; IV explains the architecture of proposed compressor based Urdhava multipliers; V Presents the simulation results and Comparison of Q format multipliers and lastly VI provides conclusion of the work.

A. Literature Review:

The application which we are considering describes about the information about all the basic Vedic mathematics techniques [1] used for various operations. Among these techniques more preferable method is Urdhva tiryakbhyam method to describe Urdhava tiryakbhyam methodology [3] and their hardware architecture [4] details and implementation [5] presented. The algorithm to architecture mapping using floating point number representation Consumes more hardware which tends to be expensive.Fixed point number representation [6] is a good option to implement at silicon level. Hence our focus in this work is to develop optimized hardware modules for multiplication operation .To performing multiplication operations for various types of Q- formats [2] architectures (Q15, Q31, and Q63 formats) used. In this paper the proposed work is the implementation of compressor [7, 8] based tiryakbhyam methodology to reduce area and time delay to improve overall performance.



International Journal of Advanced Research in Electrical, Electronics and Instrumentation Engineering

(An ISO 3297: 2007 Certified Organization)

Vol. 3, Issue 3, March 2014

II. FIXED POINT ARITHMETIC

An N-bit fixed-point number [6] can be interpreted as either: an integer (i.e.20640), a fractional number (i.e.0.78). In a 16-bit processor dynamic range in between -32,768 to 32,767.

Example for integer fixed-point number: $200 \times 300 = 60000$, this is an overflow. This is difficult to use in processors due to possible overflow. To overcome overflow draw back fractional fixed-Point Representation will be used which is suitable for DSP algorithms. An N-bit fixed point 2's complement representation as follows.

$$A = -b_{n-1}2^{n-1} + b_{n-2}2^{n-2} + \dots + b_12^1 + b_02^0 \dots \text{Equation (1)}$$

Equation (1) shows fractional fixed point representation. Fractional number range is between 1 and -1. Multiplying a fraction by a fraction always results in a fraction and will not produce an overflow (e.g., 0.99×0.9999 less than 1) Successive additions may cause overflow .To represent fractional numbers in-between -1.0 and $1-2^{-n-1}$ where N is the number of bits.

A.Q- Format Representation:

In general any Q-format representation is denoted by $Q_{m.n}$ notation where m is the number of bits for integer portion ,n denotes number of bits for fractional portion Total number of bits $N = m + n + 1$, for signed numbers.

$$B = -b_{n-1}2^0 + b_{n-2}2^{-1} + \dots + b_12^{-(n-2)} + b_02^{-(n-1)} \dots \text{Equation (2)}$$

Equation (2) shows fractional fixed point Q-format representation.Example for Q-format representation: 16-bit number(N=16) and Q2.13 format 2 bits for integer portion, 13 bits for fractional portion, 1 signed bit (MSB).

Special cases: 16-bit integer number (N=16) => Q15.0 format 16-bit fractional number (N = 16) => Q0.15 format; also known as Q.15 or Q15.

B. Q-Format Multiplication:

When two Q15 numbers are multiplied their product is 32 bits long as illustrated in Fig. 1. The product has a redundant or extended sign bit. Since the product stored in memory should also be a Q15 number we left shift the product by one bit and the most significant 16 bits (including sign bit) is stored in the memory. Product of two Q15 numbers is Q30. So we must remember that the 32-bit product has two bits in front of the binary point. Since $N \times N$ multiplication yields $2N-1$ result Addition MSB sign extension bit typically only the most significant 15 bits (plus the sign bit) are stored back into memory, so the write operation requires a left shift by one. Fig.1. demonstrates multiplication of two Q15 format numbers. The process remains same for Q31format and Q63 format.

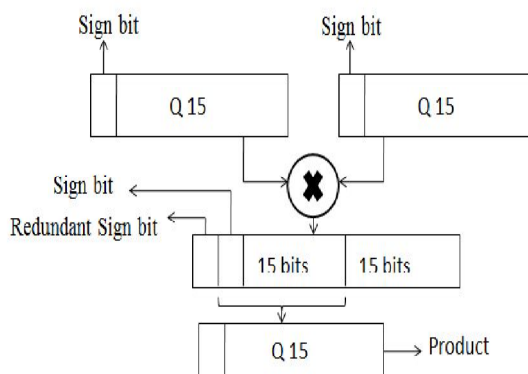


Figure .1 Multiplications of two Q15 format numbers yielding the product in Q15 formats itself. [2]

When we want to convert a fractional number in the range of the desired $Q_{m.n}$ format, we multiply it with 2^n . The resultant value is truncated or rounded off to the nearest integer. Therefore a small amount of precision loss is involved which reduces as the number of bits representing the fractional part increases. We prefer rounding technique since its error bias in both positive and negative direction is same. Therefore the rounded value will be more precise. For e.g. Conversion of 0.2625 to Q15 format is done by multiplying it with 2^{15} which equals to 8601.6 which when rounded gives 8602.This is stored as 0010000110011010 in a 16 bit memory location. The most significant bit indicates sign of



International Journal of Advanced Research in Electrical, Electronics and Instrumentation Engineering

(An ISO 3297: 2007 Certified Organization)

Vol. 3, Issue 3, March 2014

the number. If it is negative then 2's complement method is followed to store the number. Thus a fraction is converted to an integer in a Q-format and the choice of the decimal point lies entirely in the hands of the programmer.

III. URDHAVA TIRYAKBHYAM METHOD

Urdhava Tiryakbhyam [3] is a Sanskrit word which means vertically and crosswire in English. The method is a general multiplication formula applicable to all cases of multiplication. It is based on a novel concept through which all partial products are generated concurrently.

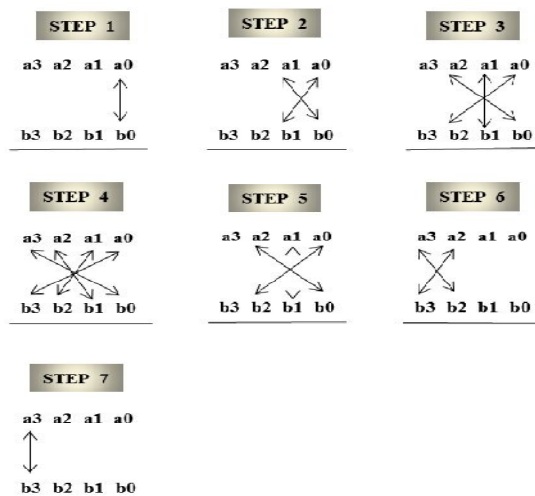


Figure. 2 Multiplications of two 4 bit numbers using Urdhava Tiryakbhyam method. [5]

Fig. 2, the least significant bit (LSB) of the multiplier is multiplied with least significant bit of the multiplicand (vertical multiplication). This result forms the LSB of the product. In step 2 next higher bit of the multiplier is multiplied with the LSB of the multiplicand and the LSB of the multiplier is multiplied with the next higher bit of the multiplicand (crosswire multiplication). These two partial products are added and the LSB of the sum is the next higher bit of the final product and the remaining bits are carried to the next step the Partial products and their sums for every step can be calculated in parallel. Thus every step in fig. 2 has a corresponding expression as Follows:

$$\begin{aligned}
 r_0 &= a_0b_0 \dots\dots\dots \text{step (1)} \\
 c_1r_1 &= a_1b_0 + a_0b_1 \dots\dots\dots \text{step (2)} \\
 c_2r_2 &= c_1 + a_2b_0 + a_1b_1 + a_0b_2 \dots\dots\dots \text{step (3)} \\
 c_3r_3 &= c_2 + a_3b_0 + a_2b_1 + a_1b_2 + a_0b_3 \dots\dots\dots \text{step (4)} \\
 c_4r_4 &= c_3 + a_3b_1 + a_2b_2 + a_1b_3 \dots\dots\dots \text{step (5)} \\
 c_5r_5 &= c_4 + a_3b_2 + a_2b_3 \dots\dots\dots \text{step (6)} \\
 c_6r_6 &= c_5 + a_3b_3 \dots\dots\dots \text{step (7)}
 \end{aligned}$$

With $c_6r_6r_5r_4r_3r_2r_1r_0$ being the final product [5]. Hence this is the general mathematical formula applicable to all cases of multiplication and its hardware architecture is shown in fig.4. In order to multiply two 8-bit numbers using 4-bit multiplier we proceed as follows. When the numbers are multiplied according to Urdhava Tiryakbhyam (vertically and crosswire) method, we get

$$\begin{array}{r}
 AH \ AL \\
 BH \ BL \\
 \hline
 \end{array}$$

$$(AH \times BH) + (AH \times BL + BH \times AL) + (AL \times BL).$$

Thus we need four 4-bit multipliers and two adders to add the partial products and 4-bit intermediate carry generated. Since product of a 4 x 4 multiplier is 8 bits long, in every step the least significant 4 bits correspond to the product and the remaining 4 bits are carried to the next step. This process continues for 3 steps in this case. Similarly, 16 bit multiplier has four 8 x 8 multiplier and two 16 bit adders with 8 bit carry. Therefore we see that the multiplier is highly modular in nature. Hence it leads to regularity and scalability of the multiplier layout.

International Journal of Advanced Research in Electrical, Electronics and Instrumentation Engineering

(An ISO 3297: 2007 Certified Organization)

Vol. 3, Issue 3, March 2014

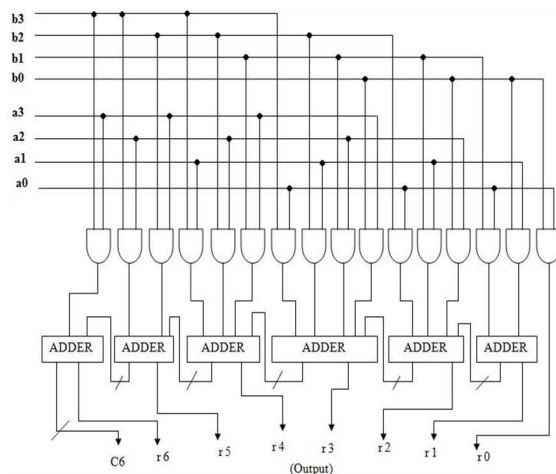


Figure.3. Hardware architecture of 4 X 4 Urdhva Tiryakbhyam multiplier [4]

IV. ARCHITECTURE

Q-format signed multiplier includes Urdhva tiryakbhyam integer multiplier [4] with certain modifications as follows.

A.3_2 Compressor:

High speed multipliers use 3-2, 4-2 and 5-2 compressors to lower the latency of partial product reduction part [7, 8]. Compressors are used to minimize delay and area which leads to increase the performance of the overall system. Compressors are generally designed by XOR-XNOR gates and multiplexers. A compressor is a device which is used to reduce the operands while adding terms of partial products in multipliers. The most widely and the simplest used compressor is the 3-2 compressor which is also known as a full adder. A 3-2 compressor has three inputs X1, X2, X3 and generates two Outputs they are sum and the carry bits. The block diagram of 3-2 compressor is shown in figure.4. (a) And truth table for 3-2 compressor is shown in figure.4. (b).

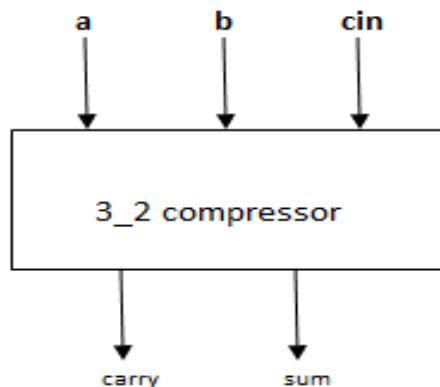


Figure.4. (a) Block diagram of 3_2 compressor

International Journal of Advanced Research in Electrical, Electronics and Instrumentation Engineering

(An ISO 3297: 2007 Certified Organization)

Vol. 3, Issue 3, March 2014

a	b	C _{in}	sum	carry
0	0	0	0	0
0	0	1	1	0
0	1	0	1	0
0	1	1	0	1
1	0	0	1	0
1	0	1	0	1
1	1	0	0	1
1	1	1	1	1

Figure.4. (b) 3_2 compressor truth table

Figure 4. (c) Has two XOR gates in the critical path. The sum output is generated by the second XOR and carry output is generated by the multiplexer (MUX). The equations (3, 4, and 5) governing the conventional 3-2 compressor outputs are shown below.

The conventional architectures of 3-2 compressor shown in figure 4. (c).

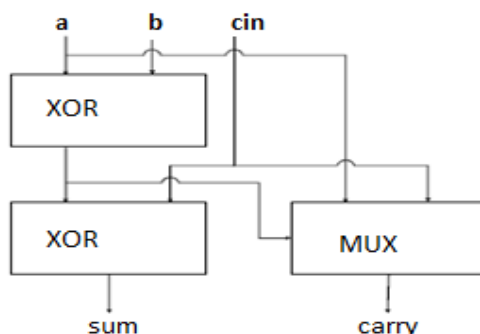


Figure.4. (c) Conventional 3_2 compressor

$$a + b + C_{in} = \text{sum} + 2 \cdot \text{carry} \dots \text{Equation (3)}$$

$$\text{Sum} = a \oplus b \oplus C_{in} \dots \text{Equation (4)}$$

$$\text{Carry} = (a \oplus b) \cdot C_{in} + (a \oplus b) \cdot a \dots \text{Equation (5)}$$

Considering a 16 bit Q15 multiplier, the product is also a Q15 number which is 16 bits long.

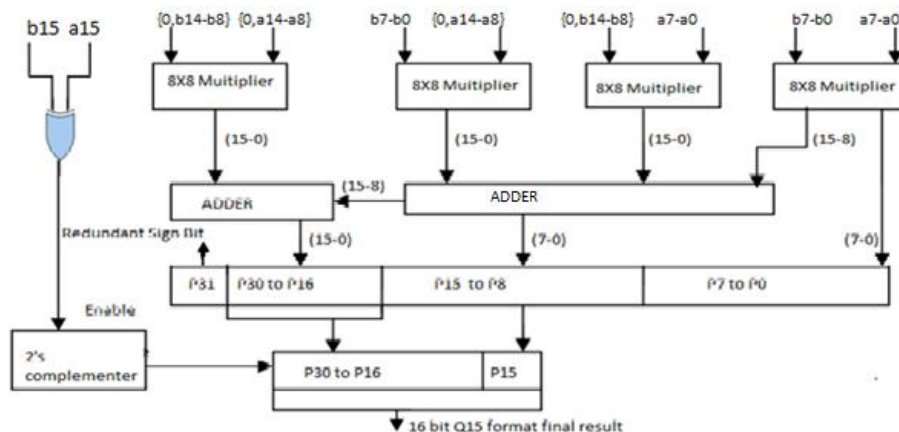


Figure.5. Architecture of a Q15 format multiplier. Multiplication of two Q15 numbers a and b results in a Q15 product Denoted by P in the figure.

International Journal of Advanced Research in Electrical, Electronics and Instrumentation Engineering

(An ISO 3297: 2007 Certified Organization)

Vol. 3, Issue 3, March 2014

Firstly, if the MSB of input is 1 then it is a negative number. Therefore 2's complement of the number is taken before proceeding with multiplication. Since the MSB denotes sign it is excluded and a '0' is placed in this position while multiplying. A Q15 format multiplier consists of four 8 x 8 Urdhava multipliers and the resulting product is 32 bits Long as shown in fig. 5.

Therefore the 32 bit product is left shifted by 1 bit to remove the redundant sign bit and only the most significant 16 bits of this product are considered which constitute the final product. An xor operation is performed on the input sign bits to determine the sign of the result. If the output is '1' it enables the conversion of the 16 bit final result to its 2's compliment format indicating a negative product.

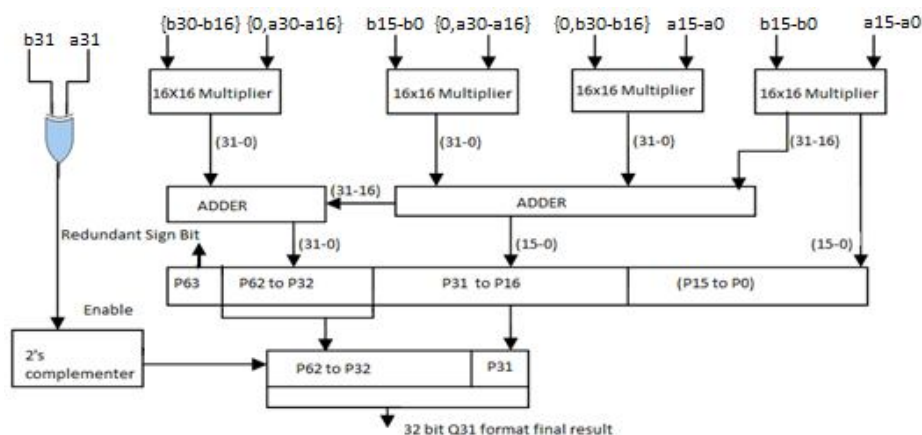


Figure.6. Architecture of a Q31 format multiplier. Multiplication of two Q31 numbers a and b results in a Q31 product Denoted by P in the figure

In fig. 6 but the product of a Q31 number is also a Q31 number which should be 32 bits long. Therefore the 64 bit product is left shifted by 1 bit to remove the redundant sign bit and only the most significant 32 bits of this product are considered which constitute the final product. A xor operation is performed on the input sign bits to determine the sign of the result. If the output is '1' it enables the conversion of the 32 bit final result to its 2's compliment format indicating a negative product.

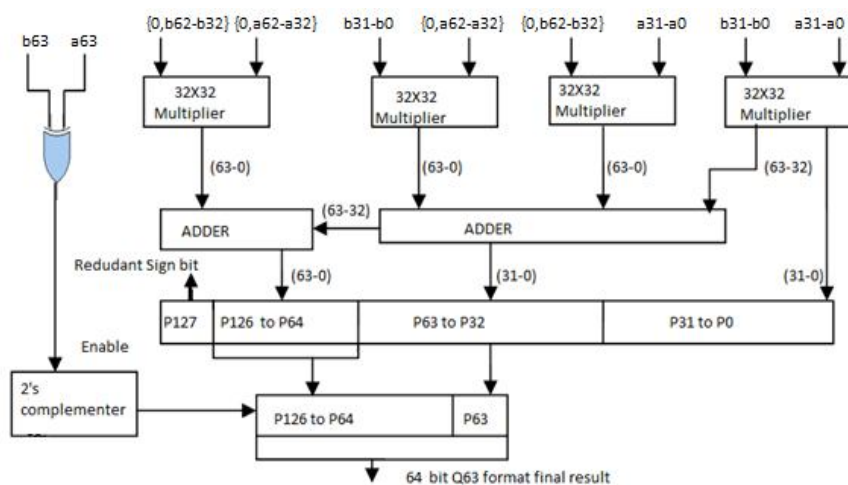


Figure.7. Architecture of a Q63 format multiplier. Multiplication of two Q63 numbers a and b results in a Q63 product Denoted by P in the figure.

International Journal of Advanced Research in Electrical, Electronics and Instrumentation Engineering

(An ISO 3297: 2007 Certified Organization)

Vol. 3, Issue 3, March 2014

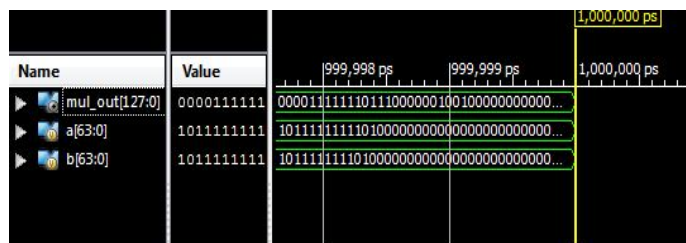


Figure.10. Simulation Result for Q63 Multiplication

B.RTL Schematics for Q-format Multipliers:

Fig.11.The outputs of 8X8 bit multipliers are added accordingly to obtain the 32 bits final product. Thus, in the final stage two adders are also required. The implemented RTLView of 16x16 bits Q-format Multiplier by using 8x8 blocks with the help of ModelSim Tool 6.1e.

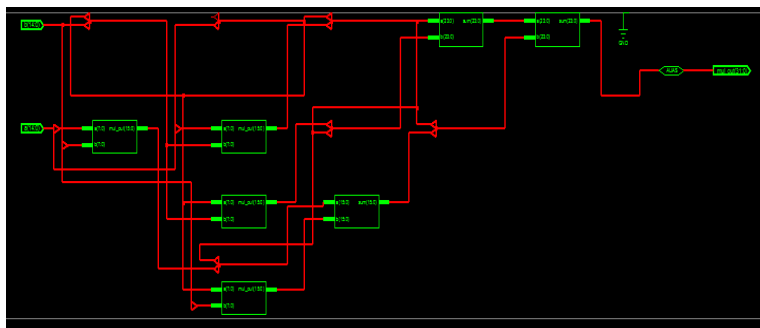


Figure.11. RTL Schematic of Q15 format multiplier.

Fig.12.The outputs of 16X16 bit multipliers are added accordingly to obtain the 64 bits final product. Thus, in the final stage two adders are also required. The implemented RTL View of 32x32 bits Q-format Multiplier by using 16x16 blocks with the help of ModelSim Tool 6.1e.

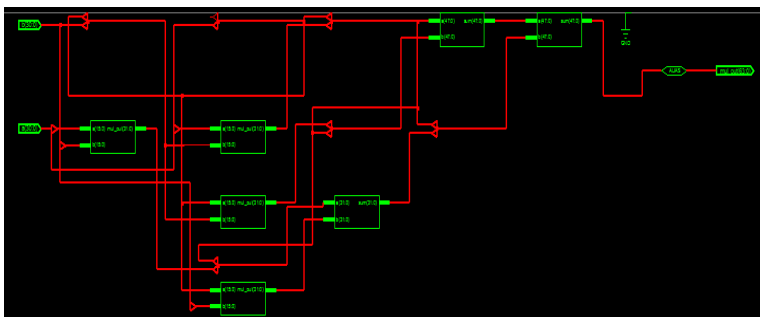


Figure. 12. RTL Schematic of Q31 format multiplier

Fig.13.The outputs of 32X32 bit multipliers are added accordingly to obtain the 128 bits final product. Thus, in the final stage two adders are also required. The implemented RTL View of 64x64 Q-format Multiplier by using 32x32 blocks with the help of ModelSim Tool 6.1e.

International Journal of Advanced Research in Electrical, Electronics and Instrumentation Engineering

(An ISO 3297: 2007 Certified Organization)

Vol. 3, Issue 3, March 2014

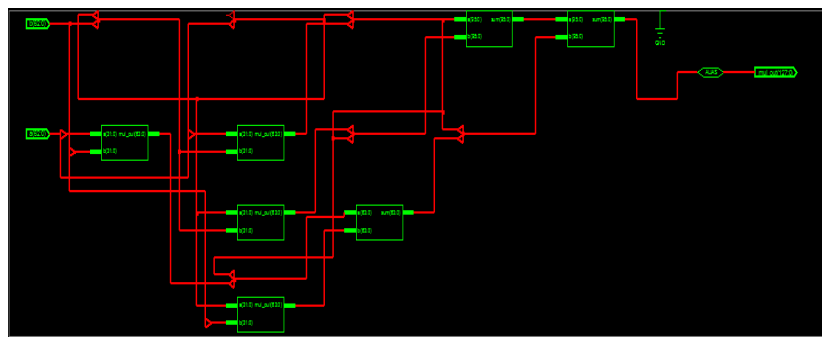


Figure. 13. RTL Schematic of Q63 format multiplier

It can be clearly noted from Table.1. That in terms of speed, the compressor based Urdhwa tiryakbhyam performs exceptionally well and is almost 1.39 times faster than the existing Urdhwa tiryakbhyam.

Table. 1. Comparison of 16 bit Q15 format multiplier

Algorithm used	LUT's used	Total LUT's present	% of area occupied	Frequency (MHZ)	Time (ns)
Urdhwa tiryakbhyam	425	28800	1.47	70.24 MHZ	14.236 ns
Compressor based Urdhwa tiryakbhyam	421	28800	1.46	77.88 MHZ	12.840 ns

It can be clearly noted from Table.2.that in terms of speed, the compressor based Urdhwa tiryakbhyam performs exceptionally well and is almost 1.39 times faster than the existing Urdhwa tiryakbhyam.

Table. 2. Comparison of 32 bit Q31 format multiplier

Algorithm used	LUT's used	Total LUT's present	% of area occupied	Frequency (MHZ)	Time (ns)
Urdhwa tiryakbhyam	1804	28800	6.26	55.93 MHZ	17.879 ns
Compressor based Urdhwa tiryakbhyam	1787	28800	6.20	60.48 MHZ	16.483 ns

It can be clearly noted from Table.3.that in terms of speed; the compressor based Urdhwa tiryakbhyam performs exceptionally well and is almost 1.19 times faster than the existing Urdhwa tiryakbhyam.



International Journal of Advanced Research in Electrical, Electronics and Instrumentation Engineering

(An ISO 3297: 2007 Certified Organization)

Vol. 3, Issue 3, March 2014

Table. 3. Comparison of 64 bit Q63 format multiplier

Algorithm used	LUT's used	Total LUT's present	% of area occupied	Frequency (MHZ)	Time (ns)
Urdhwa tiryakbhyam	7432	28800	25.80	45.34 MHZ	22.054 ns
Compressor based Urdhwa tiryakbhyam	7363	28800	25.56	47.93 MHZ	20.863 ns

From table1, table2, table3 it can be clearly noted that in terms of area and time delay proposed compressor based Urdhwa tiryakbhyam gives good performance compare with Urdhwa tiryakbhyam method because by using compressor we are reducing the number of operations comparing with adders. Compressors are also used in multiplier architectures. Multipliers are structured into three functions: Partial-product generation, Partial-product accumulation and Final addition. The main source of power, delay and area came from the partial-product accumulation stage Compressors usually implement this stage because they contribute to the reduction of the partial products (reducing the number of adders at the final stage) and also contribute to reduce the critical path which is important to maintain the circuit's performance. As per the requirements we are increasing the compressor sizes (4-2compressor, 5-2 compressor etc) it gives maximum good performance.

VI.CONCLUSION AND FUTURE WORK

The proposed fast multiplier architecture for signed Q-format multiplications using compressor based Urdhava Tiryakbhyam method of Vedic mathematics. Since Q-format representation is widely used in Digital Signal Processors. The proposed compressed Urdhava Tiryakbhyam method can substantially speed up the multiplication operation which is the basic hardware block. They occupy less area and faster than the Urdhava Tiryakbhyam method. Therefore the compressed Urdhava Tiryakbhyam Q-format multiplier is best suited for digital signal processing applications requiring faster multiplications. As a future work, the multiplier's performance could be tested within an ALU and also compared with several other existing multipliers.

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