

Improvement of Voltage Profile in Distribution Network Using Distributed Generation

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Abstract—This paper presents an efficient methodology for integration of Distributed Generation (DG) power into distribution systems, in order to maximize the voltage limit loadability. The proposed methodology is based on continuation power flow (CPF). The effectiveness of the presented methodology is demonstrated in a test distribution system that consists of 85 nodes with integration of different penetration levels of DG power. The proposed method yields efficiency in obtaining more benefits from the same amount of DG power, decreasing the losses and improving the voltage profile. The simulation of the proposed model was carried out using MATLAB/PSAT and the effective performance was analyzed.

Index Terms—Distributed generation, Distributed network, Continuation Power Flow (CPF) method, Voltage stability, Voltage limits.

I. INTRODUCTION

In general terms, voltage stability is defined as the ability of a power system to maintain steady voltages at all the buses in the system after being subjected to a disturbance from a given initial operating condition. It depends on the ability to maintain equilibrium between load demand and load supply from the power system. Instability that may result appears in the form of a progressive fall or rise of voltages of some buses. Voltage stability problems mainly occur when the system is heavily stressed beyond its capability. While the disturbance leading to voltage collapse may be initiated by a variety of causes, the main problem is the inherent weakness in the power system.

Recently a top priority is given to develop a reliable, sustainable, environment friendly as well as low-cost electrical energy supply. This includes a sensible energy mix and improvements in efficiency of energy generation, transmission and consumption[1]. As a number of events that have been brought to the vulnerability of the current centralized electrical energy supply infrastructure, such as

terrorist threats, natural disasters, geopolitical disruptions, ageing of a highly complex infrastructure, climate change and regulatory and economic risks, DG appears to be one of the key answers for different problems[3]. In the distribution system, the electrical power supply will be transferred from a vertical one to a horizontal system. In the traditional system the electric power industry has been driven by a paradigm where most of the electricity is generated in large power plants, sent to the consumption areas through HV transmission lines, and delivered to the consumers through a passive distribution infrastructure that involves HV, MV and LV networks. In this paradigm power flows only in one direction from the power station to the network and to the consumer.

The DG term is used to describe small distribution system close to the point of consumption. Such generators may be owned by a utility or more likely by a customer who may use the entire portion or perhaps all of it to the local utility combustion turbine generators, internal combustion engines and generators, photovoltaic panels, and fuel cells. Solar thermal conversion, stirling engines, are considered as DG. When the penetration of DG is high, the generated power of DG units not power flow in the distribution network consequence, the connection of DG to the grid may different technical issues, e.g. voltage profiles quality, stability etc..[8] In spite of the benefits of utilizing DG units within of the system efficiency and the improvements in the technical and operational challenge units into MV distribution networks are needed. Moreover, in more details with respect to the generation types. Optimization of the MV distribution networks with a large penetration of DG is also needed therefore the utilities can get more benefits[9].

Many voltage stability indices are based on the eigen value analysis or singular value decomposition of the system power flow Jacobian matrix. The main difficulty in this method is that Jacobian of NR power flow become singular at voltage stability limit (critical point) .A power flow solution near the critical point prone to divergences and error. Singularity in the

Jacobian can be avoided by slightly reformulating the power flow equations and applying a locally parameterized continuation technique. During the resulting continuation power flow, the reformulated set of equations remains well conditioned so that divergence and error due to a singular Jacobian are not encountered.

II. CONTINUATION POWER FLOW

The continuation method is a mathematical path-following methodology used to solve systems of nonlinear equations. Using the continuation method, a solution branch can be tracked around the turning point without difficulty. This makes the continuation method quite attractive in approximations of the critical point in a power system. The CPF captures this path-following feature by means of a predictor-corrector scheme [11]. Moreover, CPF can be used to determine generator reactive

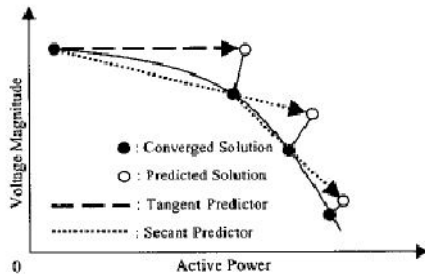


Fig.1. An illustration of the Continuation power flow

power limits, voltage limits and flow limits of transmission lines[2]. Bifurcation analysis requires steady state equation of power system models, as follows

A. Power Flow Equations

The power mismatch equations at buses except generator internal buses are given by

$$\Delta P_i^p = -Pd_i^p - V_i^p \sum_{j \in i} \sum_{m=a,b,c} V_j^m (G_{ij}^{pm} \cos \theta_{ij}^{pm} + B_{ij}^{pm} \sin \theta_{ij}^{pm}) = 0 \quad (1)$$

$$\Delta Q_i^p = -Qd_i^p - V_i^p \sum_{j \in i} \sum_{m=a,b,c} V_j^m (G_{ij}^{pm} \sin \theta_{ij}^{pm} - B_{ij}^{pm} \cos \theta_{ij}^{pm}) = 0 \quad (2)$$

Where $i = 1, 2, \dots, N$, Pd_i^p and Qd_i^p are the active and reactive load powers of phase p at bus i , respectively. $G_{ij}^{pm} + jB_{ij}^{pm}$ ($i, j = 1, 2, \dots, N$) is the element of the system admittance matrix.

The power mismatch equations at generator internal buses are presented as follows

$$\Delta P_{gi} = -Pg_i - \sum_{p=a,b,c} \sum_{m=a,b,c} [V_i^p V_i^m (Gg_i^{pm} \cos \theta_i^{pm} + Bg_i^{pm} \sin \theta_i^{pm}) + \sum_{p=a,b,c} \sum_{m=a,b,c} [V_i^p E_i^p (Gg_i^{pm} \cos(\theta_i^{pm} - \delta_i^m) + Bg_i^{pm} \sin(\theta_i^{pm} - \delta_i^m))] \quad (3)$$

$$\Delta Q_{gi} = -Qg_i - \sum_{p=a,b,c} \sum_{m=a,b,c} [V_i^p V_i^m (Gg_i^{pm} \sin \theta_i^{pm} - Bg_i^{pm} \cos \theta_i^{pm})] + \sum_{p=a,b,c} \sum_{m=a,b,c} [V_i^p E_i^p (Gg_i^{pm} \sin(\theta_i^p - \delta_i^m) - Bg_i^{pm} \cos(\theta_i^p - \delta_i^m))] \quad (4)$$

Where $i = 1, 2, \dots, Ng$. Ng is the number of generators. In three-phase power flow calculations, P_{gi} and Q_{gi} , which are specified, are the active and reactive generation powers of the generator at bus i , respectively. $G_{ij}^{pm} + jB_{ij}^{pm}$ are the elements of the generator admittance matrix. For the case of PV machine, the reactive power constraint equation (4) can be replaced by voltage control constraint[15].

The nonlinear equations (1) – (4) can be combined and expressed in compact form

$$F(x) = 0 \quad (5)$$

where represents the whole set of power flow mismatch and machine terminal constraint equations. is the state variable vector and given by $X = [\theta^a, V^a, \theta^b, V^b, \theta^c, V^c, \delta^a, E^a]^t$. The Newton equation is given by:

$$J(x)\Delta x = -F(x) \quad (6)$$

Where

$$F(x) = [\Delta P^a, \Delta Q^a, \Delta P^b, \Delta Q^b, \Delta P^c, \Delta Q^c, \Delta P^g, \Delta Q^g]^t$$

$J(x) = \frac{dF(x)}{dx}$ is the system Jacobian matrix.

B. Continuation Power Flow Equations

The three phase continuation three phase power flow can be formulated based on the nonlinear power flow equations given by (5). In principle, a continuation three-phase power flow solution consists of two steps, namely Predictor Step and Corrector Step[16].

B.1. Predictor Step

To simulate three-phase load change, Pd_i^p and Qd_i^p which are shown in (1) and (2), may be represented by

$$Pd_i^p = Pd_i^p (1 + \lambda * KPd_i^p) \quad (7)$$

$$Qd_i^p = Qd_i^p (1 + \lambda * KQd_i^p) \quad (8)$$

Where PdO_i^p and QOd_i^p are the base case active and reactive load powers of phase p at bus i . λ is the loading factor, which characterizes the change of load. The ratio of KPd_i^p/KQd_i^p is constant to maintain constant power factor.

Similarly, to simulate generation changes, P_{gi} and Q_{gi} shown in (3) and (4), are represented by:

$$P_{gi} = P_{g0i}(1 + \lambda * KP_{gi}) \quad (9) \quad Q_{gi} = Q_{g0i}(1 + \lambda * KQ_{gi}) \quad (10)$$

Where P_{g0i} and Q_{g0i} are the total active and reactive powers of the generator of the base case. The ratio of KPd_i^p/KQd_i^p is constant to maintain a constant power factor for a PQ machine.

The nonlinear power flow equations (5) are augmented by an extra variable λ as follows

$$F(x, \lambda) = 0 \quad (11)$$

Where $F(x, \lambda)$ represents the whole set of power flow mismatch equations.

The predictor step is used to provide an approximate point of the next solution. A prediction of the next solution is obtained by taking an appropriately sized step in the direction tangent to the solution path. To solve (11), the continuation algorithm with predictor and corrector steps can be used. Linearizing (11), we have:

$$dF(x, \lambda) = F_x dx + F_\lambda d\lambda = 0 \quad (12)$$

In order to solve (12), one more equation is needed. With choosing a non-zero magnitude for one of the tangent vector and keep its change as ± 1 , one extra equation can be obtained:

$$t_k = \pm 1 \quad (13)$$

Where t_k is a non-zero element of the tangent vector dx . A set of linearized equations can be obtained by combining (12) and (13) where the tangent vector dx and $d\lambda$ are unknown variables:

$$\begin{bmatrix} F_x & F_\lambda \\ e_k & 0 \end{bmatrix} \begin{bmatrix} dx \\ d\lambda \end{bmatrix} = \begin{bmatrix} 0 \\ \pm 1 \end{bmatrix} \quad (14)$$

Where e_k is a row vector with all elements zero except for k^{th} element, which equals one. In (14), whether +1 or -1 is used depends on how the k^{th} state variable is changing as the solution is being traced. After solving (14), the prediction of the next solution can be determined by:

$$\begin{bmatrix} x^* \\ \lambda^* \end{bmatrix} = \begin{bmatrix} x \\ \lambda \end{bmatrix} + \sigma \begin{bmatrix} dx \\ d\lambda \end{bmatrix} \quad (15)$$

where * denotes the estimated solution of the next step while σ is a scalar, which represents the step size.

B.2 Corrector Step

The corrector step is to solve the augmented Newton power flow equation with the predicted solution in (15) as the initial point fig. 1. In the augmented Newton power flow algorithm an extra equation is included and λ is taken as a variable. The augmented Newton power flow equation may be given by:

$$\begin{bmatrix} F(x, \lambda) \\ x_k - \eta \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix} \quad (16)$$

where η , which is determined by (15), is the predicted value of the continuation parameter x_k . The determination of the continuation parameter is shown in the following solution procedure. The corrector equation (16), which consists a set of augmented nonlinear equations, can be solved iteratively by Newton's approach as follows:

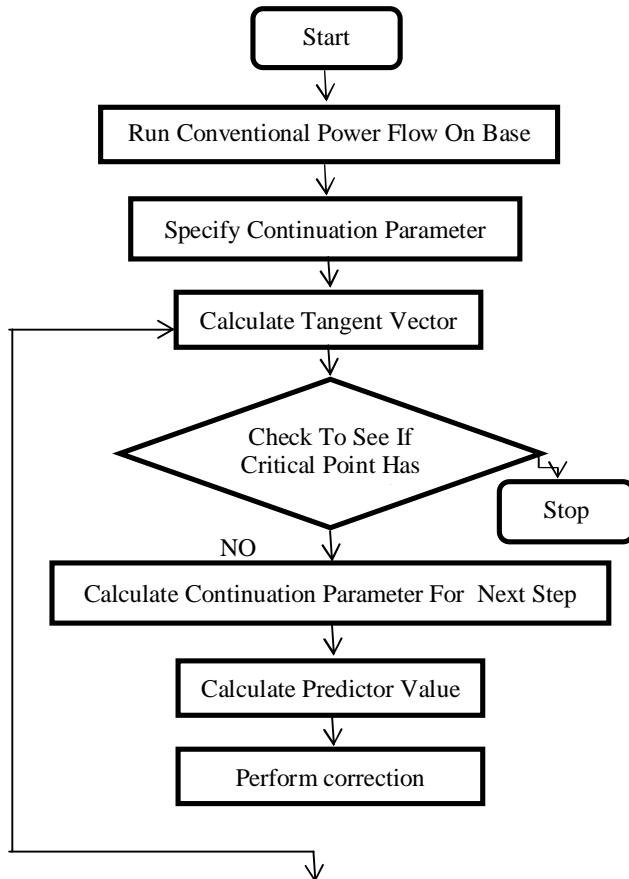
$$\begin{bmatrix} F_x & F_\lambda \\ e_k & 0 \end{bmatrix} \begin{bmatrix} \Delta x \\ \Delta \lambda \end{bmatrix} = - \begin{bmatrix} F(x, \lambda) \\ x_k - \eta \end{bmatrix} \quad (17)$$

III. PLACEMENT ALGORITHM

Different recommended locations for integration of DG for increasing the amount of loads which can be supplied from the system through enhancing the VLL of the system are the main objective of the suggested methodology. The proposed algorithm is depicted in Fig. 2. The methodology starts with execution of CPF to specify the VLL of the base case of the system and identify the first node which reached the low voltage limit. Then the DG unit with a certain power is integrated at that node and after that the CPF is executed. Therefore, another node can be obtained and then the DG units' power is dispersed between the resulted nodes according to their loads, then the VLL is checked. This process is continued until no improvement is obtained and as a result the methodology will be ended. Different steps of the proposed algorithm are summarized as follows:

- Step 1: Identifying the first node reached the low voltage limit in the network using CPF.
- Step 2: Integrating the DG units at that node and examine the VLL of the network.
- Step 3: Running the CPF with DG.
- Step 4: Identifying another node which reached the low voltage limit using CPF.
- Step 5: Dispersing the DG power between the recommended nodes according to their loads.
- Step 6: Running the CPF with DG.
- Step 7: Examining the VLL with the existence of the different number of DG units.

Step 8: Go to step 4 if an improvement in VLL is achieved otherwise go to step 9.
 Step 9: End.



IV. SIMULATION STUDY

The placement methodology is implemented on an 85 node radial distribution network[8](seeFig. 2). The data of the system is given in Table. I. The system was built into PSAT and as a first step the CPF is executed where the limit was identified to be the low voltage limit. That means the loading parameter (λ) will be increased at all nodes with the same value till the voltage at one node reaches the minimum voltage limit. The VLL can be specified based on the value of k which has been found in this step to be 1.1515 which means that the load at each node can be increased to be 115.2% of its base case while the voltage at all nodes are within the limits. Node no. 54 was found to be the first node reached the low voltage limit. According to the methodology all the DG units (6 X240 kW) are integrated at this node. With integration of the DG units at node no. 54 the CPF is executed for the second time till the voltage at another node reaches the low minimum value. The loading factor (λ) in this step was found to be 1.8229, which means that the VLL is 3.3 MW[15]. Moreover, it has

Fig. 2 Flow Chart for Continuation Power Flow

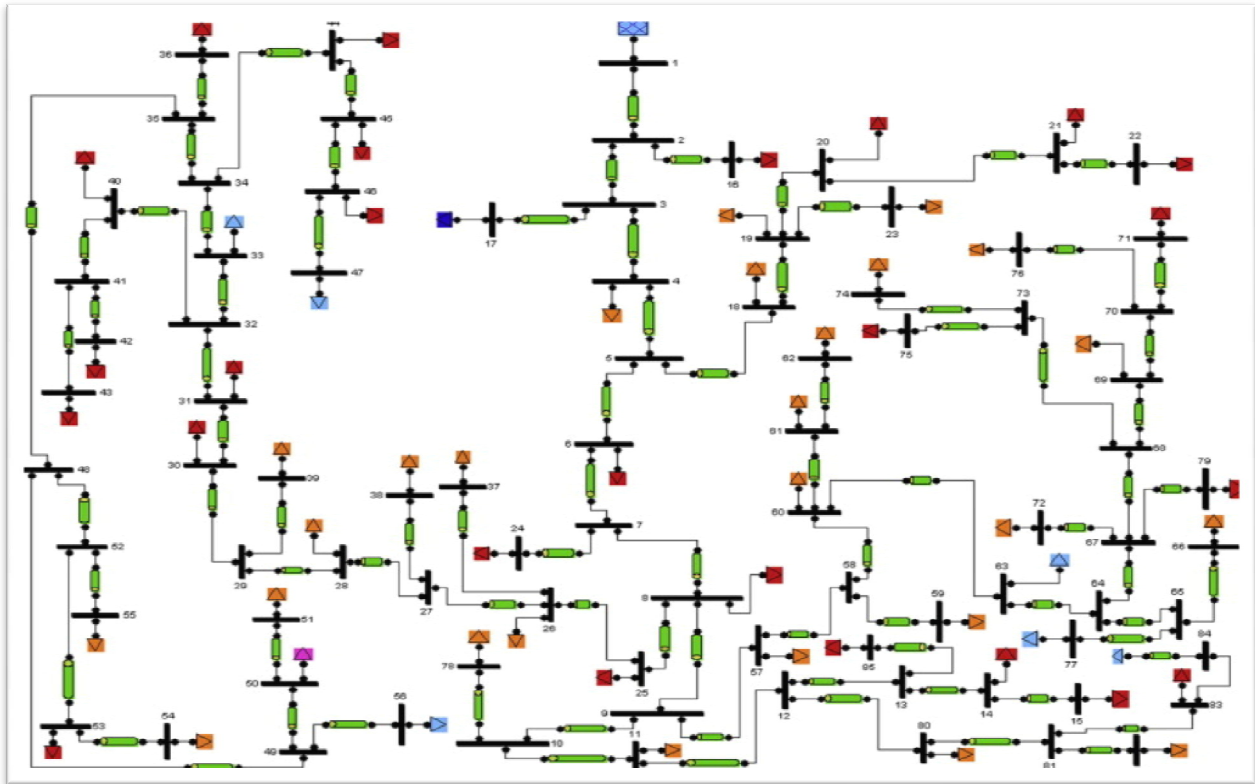


Fig. 3. One line diagram of 85 node distribution network in PSAT Space

Been found that node no. 76 is the node which reaches the minimum voltage limit. Then according to the procedure of the algorithm the DG power were dispersed between nodes No. 54 and 76. That means at each node three DG units were integrated. Then, with the existence of the DG units at nodes No. 54, and 76 the CPF is executed for the third time. In this case the VLL is improved to be 3.68MW with a maximum loading factor of 2.0419. Through this step node No. 47 was the node which first reached the low voltage limit. Therefore, the six DG units were dispersed at the three nodes 54, 76, and 47 with two DG units at each node. The network with presence of the DG units at the three nodes is tested with CPF and in this step the VLL was 3.8MW with a maximum loading factor of 2.1093.

The loading factor (k) in this step was found to be 1.8229, which means that the VLL is 3.3 MW.

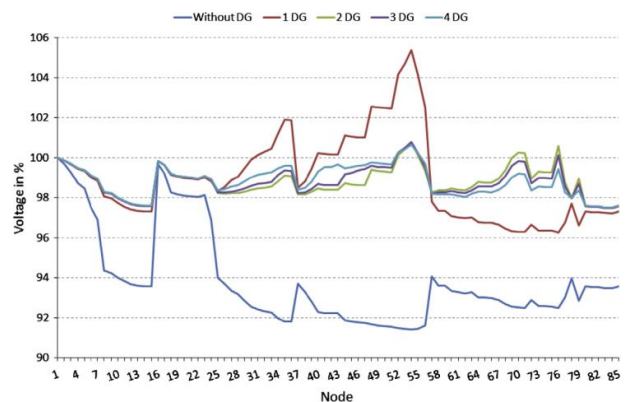


Fig. 4. Voltage Profiles with (0.9 Power Factor) For Different DG Units

Then according to the procedure of the algorithm the DG power were dispersed between nodes No. 54 and 76. (Fig.4) That means at each node three DG units were integrated. Then, with the existence of the DG units at nodes No. 54, and 76 the CPF is executed for the third time. In this case the VLL is improved to be

3.68MW with a maximum loading factor of 2.0419. Through this step node No. 47 was the node which first reached the low voltage limit.

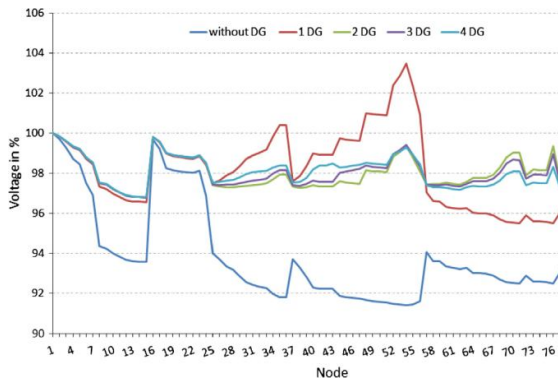


Fig. 5.

Voltage Profiles with (Unity Power Factor) For Different DG Units' Number.

Moreover, it has been found that node no. 76 is the node which reaches the minimum voltage limit [13] (see fig 3). Therefore, the six DG units were dispersed at the three nodes 54, 76, and 47 with two DG units at each node. The network with presence of the DG units at the three nodes is tested with CPF and in this step the VLL was 3.8MW with a maximum loading factor of 2.1093. The improvement in percentage is calculated relative to the base case. It can be demonstrated that VLL is improved when the DG power is dispersed between the resulted nodes (Fig.5). A 515 kW is the difference in VLL of the system between integrating two units at each node of the three resulted nodes and integrating the six units at one node. This means that the network can be loaded by 15.7% more than the case of concentrated DG units at node No. 54 (Fig.6) while the voltages are kept within the limits.

**TABLE I
LINE AND LOAD DATA OF 85 BUS SYSTEM**

Line No	Send. Node	Rece. Node	R (Ω)	X (Ω)	P (MV A)
1	1	2	0.108	0.075	0
2	2	3	0.163	0.112	0
3	3	4	0.217	0.149	56
4	4	5	0.108	0.074	0
5	5	6	0.435	0.298	0
6	6	7	0.272	0.186	0

7	7	8	1.197	0.82	35.28
8	8	9	0.108	0.074	0
9	9	10	0.598	0.41	0
10	10	11	0.544	0.373	56
11	11	12	0.544	0.373	0
12	12	13	0.598	0.41	0
13	13	14	0.272	0.186	35.28
14	14	15	0.326	0.223	35.28
15	2	16	0.728	0.302	35.28
16	3	17	0.455	0.189	112
17	5	18	0.82	0.34	56
18	18	19	0.637	0.264	56
19	19	20	0.455	0.189	35.28
20	20	21	0.819	0.34	35.28
21	2	22	1.548	0.642	35.28
22	19	23	0.182	0.075	56
23	7	24	0.91	0.378	35.28
24	8	25	0.455	0.189	35.28
25	25	26	0.364	0.151	56
26	26	27	0.546	0.226	0
27	27	28	0.273	0.113	56
28	28	29	0.546	0.226	0
29	29	30	0.546	0.226	35.28
30	30	31	0.273	0.113	35.28
31	2	32	1.548	0.642	35.28
32	19	33	0.182	0.075	56
33	7	34	0.91	0.378	35.28
34	8	35	0.455	0.189	35.28
35	25	36	0.364	0.151	56
36	26	37	0.546	0.226	0
37	27	38	0.273	0.113	56
38	28	39	0.546	0.226	0
39	29	40	0.546	0.226	35.28
40	30	41	0.273	0.113	35.28
41	32	42	1.548	0.642	35.28
42	19	43	0.182	0.075	14
43	7	44	0.91	0.378	0
44	8	45	0.455	0.189	0
45	25	46	0.364	0.151	0
46	26	47	0.546	0.226	0
47	27	48	0.273	0.113	0
48	28	49	0.546	0.226	0
49	29	50	0.546	0.226	35.28
50	30	51	0.273	0.113	35.28
51	32	52	1.548	0.642	35.28
52	19	53	0.182	0.075	14
53	7	54	0.91	0.378	0
54	8	55	0.455	0.189	0
55	25	56	0.364	0.151	0
56	26	57	0.546	0.226	0
57	27	58	0.273	0.113	0
58	28	59	0.546	0.226	0
59	29	60	0.546	0.226	35.28
60	30	61	0.273	0.113	35.28
61	32	62	1.548	0.642	35.28
62	19	63	0.182	0.075	14
63	7	64	0.91	0.378	0
64	8	65	0.455	0.189	0
65	25	66	0.364	0.151	0
66	26	67	0.546	0.226	0
67	27	68	0.273	0.113	0
68	28	69	0.546	0.226	0
69	29	70	0.546	0.226	35.28
70	30	71	0.273	0.113	35.28
71	32	72	1.548	0.642	35.28
72	19	73	0.182	0.075	14
73	7	74	0.91	0.378	0
74	8	75	0.455	0.189	0
75	25	76	0.364	0.151	0
76	26	77	0.546	0.226	0
77	27	78	0.273	0.113	0
78	28	79	0.546	0.226	0
79	29	80	0.546	0.226	35.28
80	30	81	0.273	0.113	35.28
81	32	82	1.548	0.642	35.28
82	19	83	0.182	0.075	14
83	7	84	0.91	0.378	0
84	8	85	0.455	0.189	0
85	25	86	0.364	0.151	0
86	26	87	0.546	0.226	0
87	27	88	0.273	0.113	0
88	28	89	0.546	0.226	0
89	29	90	0.546	0.226	35.28
90	30	91	0.273	0.113	35.28
91	32	92	1.548	0.642	35.28
92	19	93	0.182	0.075	14
93	7	94	0.91	0.378	0
94	8	95	0.455	0.189	0
95	25	96	0.364	0.151	0
96	26	97	0.546	0.226	0
97	27	98	0.273	0.113	0
98	28	99	0.546	0.226	0
99	29	100	0.546	0.226	35.28
100	30	101	0.273	0.113	35.28
101	32	102	1.548	0.642	35.28
102	19	103	0.182	0.075	14
103	7	104	0.91	0.378	0
104	8	105	0.455	0.189	0
105	25	106	0.364	0.151	0
106	26	107	0.546	0.226	0
107	27	108	0.273	0.113	0
108	28	109	0.546	0.226	0
109	29	110	0.546	0.226	35.28
110	30	111	0.273	0.113	35.28
111	32	112	1.548	0.642	35.28
112	19	113	0.182	0.075	14
113	7	114	0.91	0.378	0
114	8	115	0.455	0.189	0
115	25	116	0.364	0.151	0
116	26	117	0.546	0.226	0
117	27	118	0.273	0.113	0
118	28	119	0.546	0.226	0
119	29	120	0.546	0.226	35.28
120	30	121	0.273	0.113	35.28
121	32	122	1.548	0.642	35.28
122	19	123	0.182	0.075	14
123	7	124	0.91	0.378	0
124	8	125	0.455	0.189	0
125	25	126	0.364	0.151	0
126	26	127	0.546	0.226	0
127	27	128	0.273	0.113	0
128	28	129	0.546	0.226	0
129	29	130	0.546	0.226	35.28
130	30	131	0.273	0.113	35.28
131	32	132	1.548	0.642	35.28
132	19	133	0.182	0.075	14
133	7	134	0.91	0.378	0
134	8	135	0.455	0.189	0
135	25	136	0.364	0.151	0
136	26	137	0.546	0.226	0
137	27	138	0.273	0.113	0
138	28	139	0.546	0.226	0
139	29	140	0.546	0.226	35.28
140	30	141	0.273	0.113	35.28
141	32	142	1.548	0.642	35.28
142	19	143	0.182	0.075	14
143	7	144	0.91	0.378	0
144	8	145	0.455	0.189	0
145	25	146	0.364	0.151	0
146	26	147	0.546	0.226	0
147	27	148	0.273	0.113	0
148	28	149	0.546	0.226	0
149	29	150	0.546	0.226	35.28
150	30	151	0.273	0.113	35.28
151	32	152	1.548	0.642	35.28
152	19	153	0.182	0.075	14
153	7	154	0.91	0.378	0
154	8	155	0.455	0.189	0
155	25	156	0.364	0.151	0
156	26	157	0.546	0.226	0
157	27	158	0.273	0.113	0
158	28	159	0.546	0.226	0
159	29	160	0.546	0.226	35.28
160	30	161	0.273	0.113	35.28
161	32	162	1.548	0.642	35.28
162	19	163	0.182	0.075	14
163	7	164	0.91	0.378	0
164	8	165	0.455	0.189	0
165	25	166	0.364	0.151	0
166	26	167	0.546	0.226	0
167	27	168	0.273	0.113	0
168	28	169	0.546	0.226	0
169	29	170	0.546	0.226	35.28
170	30	171	0.273	0.113	35.28
171	32	172	1.548	0.642	35.28
172	19	173	0.182	0.075	14
173	7	174	0.91	0.378	0
174	8	175	0.455	0.189	0
175	25	176	0.364	0.151	0
176	26	177	0.546	0.226	0
177	27	178	0.273	0.113	0
178	28	179	0.546	0.226	0
179	29	180	0.546	0.226	35.28
180	30	181	0.273	0.113	35.28
181	32	182	1.548	0.642	35.28
182	19	183	0.182	0.075	14
183	7	184	0.91	0.378	0
184	8	185	0.455	0.189	0
185	25	186	0.364	0.151	0
186	26	187	0.546	0.226	0
187	27	188	0.273	0.113	0
188	28	189	0.546	0.226	0
189	29	190	0.546	0.226	35.28
190	30	191	0.273	0.113	35.28
191	32	192	1.548	0.642	35.28
192	19	193	0.182	0.075	14
193	7	194	0.91	0.378	0
194	8	195	0.455	0.189	0
195	25	196	0.364	0.151	0
196	26	197	0.546	0.226	0
197	27	198	0.273	0.113	0
198	28	199	0.546	0.226	0
199	29	200	0.546	0.226	35.28
200	30	201	0.273	0.113	35.28
201	32	202	1.548	0.642	35.28
202	19	203	0.182	0.075	14
203	7	204	0.91	0.378	0
204	8	205	0.455	0.189	0
205	25	206	0.364	0.151	0
206	26	207	0.546	0.226	0

47	35	48	0.637	0.264	0
48	48	49	0.182	0.075	0
49	49	50	0.364	0.151	36.28
50	50	51	0.455	0.189	56
51	48	52	1.366	0.567	0
52	52	53	0.455	0.189	35.28
53	53	54	0.546	0.226	56
54	52	55	0.546	0.226	56
55	49	56	0.546	0.226	14
56	9	57	0.273	0.113	56
57	57	58	0.819	0.34	0
58	58	59	0.182	0.075	56
59	58	60	0.546	0.226	56
60	60	61	0.728	0.302	56
61	61	62	1.002	0.415	56
62	60	63	0.182	0.075	14
63	63	64	0.728	0.302	0
64	64	65	0.182	0.075	0
65	65	66	0.182	0.075	56
66	64	67	0.455	0.189	0
67	67	68	0.91	0.378	0
68	68	69	1.092	0.453	56
69	69	70	0.455	0.189	0
70	70	71	0.546	0.226	35.28
71	67	72	0.182	0.075	56
72	68	73	1.184	0.491	0
73	73	74	0.273	0.113	56
74	73	75	1.002	0.416	35.28
75	70	76	0.546	0.226	56
76	65	77	0.091	0.037	14
77	10	78	0.637	0.264	56
78	67	79	0.546	0.226	35.28
79	12	80	0.728	0.302	56
80	80	81	0.364	0.151	0
81	81	82	0.091	0.037	56
82	81	83	1.092	0.453	35.28
83	83	84	1.002	0.34	14
84	13	85	0.819	0.34	35.28

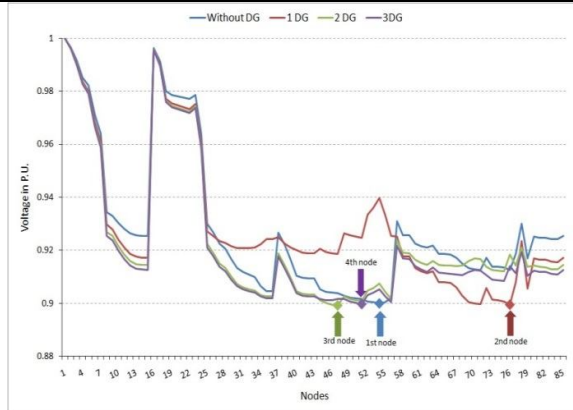


Fig.6.Voltage Profiles of DG Units at the End of Different Iterations

V. CONCLUSION

Above all results show that voltage stability margin can be found easily by CPF. The Weakest bus identification is done by without excessive calculation. Placement of distributed generation power sources we get the following conclusions.

Dispersing the same amount of the DG power at different nodes of the network enhances the VLL of the network more than concentrating this power at one node.

More loads can be supplied with lower dispersed power of the DG when it compared with higher concentrated DG power.

Dispersing the same power of the DG does not approximately affect the VLL of the network when it compared with integration of the same DG power at the weakest node.

Integrating the DGs at the recommended nodes helps to get more decreasing of the active and reactive power losses.

This result is same accurate as to find Bus participation act or using QV modal analysis. This CPF method is more accurate and simple for Voltage stability analysis.

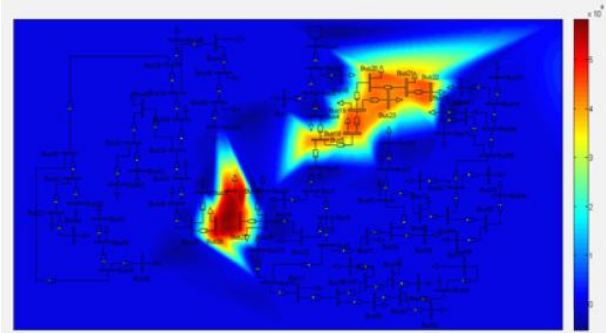


Fig. 7. Voltage Magnitude of the 85 Node Distribution Network From PSAT Space

ACKNOWLEDGMENT

The authors would like to thank the editor and anonymous reviewers whose comments and suggestions have improved the quality of this paper.

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